## Завдання:

Розпаралелити процес обчислення визначеного інтегралу, використовуючи редукцію.

Обчислити значення визначеного інтеграла відповідно до варіанту.

# Варіант 3

 $\int_{1}^{9} 3\sqrt{x}(1+\sqrt{x}) dx$  Метод Сімпсона

• Метод Сімпсона 
$$\int_{a}^{b} f(x) dx \approx \frac{h}{3} \left( \frac{1}{2} f(x_0) + \sum_{i=1}^{n-1} f(x_i) + 2 \sum_{i=1}^{n} f\left(\frac{x_{i-1} + x_i}{2}\right) + \frac{1}{2} f(x_n) \right)$$
$$h = \frac{b-a}{n}, x_i = a+i \cdot h$$

### Реалізація

Посилання на гітхаб репозиторій: <a href="https://github.com/Bohdan628318ylypchenko/parallel-programming-lab3-.git">https://github.com/Bohdan628318ylypchenko/parallel-programming-lab3-.git</a>

```
main.c
#include "integral.h"
#include <omp.h>
#include <math.h>
#include <stdio.h>
#include <stdlib.h>
#define A_TEST 1.0
#define B_TEST 9.0
#define S_EXPECTED 172.0
#define TEST_COUNT 5
#define USAGE_MSG "Usage: [s]ingle-threaded segment_count:int | [m]ulti-threaded segment_count:int thread_count:int\n"
static double f_test(double x);
static void test(double (*simpson)(double(*)(double), double, double, int));
static int n = 0;
int main(int argc, char ** argv)
       if (argc < 3)
              puts(USAGE_MSG);
              return 0;
       switch (argv[1][0])
              case 's':
                    if (argc != 3)
                           puts(USAGE_MSG);
                           return 0;
                    }
                    n = atoi(argv[2]);
                    if (n <= 1)
                           printf("Invalid segment count: %s\n", argv[2]);
                           return 0;
                    test(simpson_1t);
                    break;
              case 'm':
                    if (argc != 4)
                           puts(USAGE_MSG);
                           return 0;
                    n = atoi(argv[2]);
                    if (n <= 1)
                           printf("Invalid segment count: %s\n", argv[2]);
                    int num_threads = atoi(argv[3]);
                    if (num_threads <= 0)</pre>
                           printf("Invalid thread count: %s\n", argv[3]);
                           return 0;
                    omp_set_num_threads(num_threads);
                    test(simpson_mt);
                    break;
              default:
                    puts(USAGE_MSG);
                    return 0;
       return 0;
static void test(double (*simpson)(double(*)(double), double, double, int))
       double s_time, e_time, time, avg_time = 0;
       double integral;
       for (int i = 0; i < TEST_COUNT; i++)</pre>
              // Calculating integral
              s_time = omp_get_wtime();
              integral = simpson(f_test, A_TEST, B_TEST, n);
              e_time = omp_get_wtime();
              // Asserting
              time = e_time - s_time;
              printf("s_actual = %lf, time = %lf, diff = %lf\n", integral, time, fabs(integral - S_EXPECTED));
              // Saving
              avg_time += time;
       avg_time /= (double)TEST_COUNT;
       printf("avg_time = %lf\n", avg_time);
static double f_test(double x)
       double sqrt_x = sqrt(x);
       return 3.0 * sqrt_x * (1 + sqrt_x);
```

```
integral.h
#pragma once
/// <summary>
/// Numeric integration Simpson method
/// single-thread implementation.
/// </summary>
/// <param name="f"> Function to integrate as fpointer. </param>
/// <param name="a"> Integration segment start. </param>
/// <param name="b"> Integration segment end. </param>
/// <param name="n"> Elementary segment count. </param>
/// <returns> Integral value as double. </returns>
double simpson_1t(double (*f)(double x), double a, double b, int n);
/// <summary>
/// Numeric integration Simpson method
/// multi-thread implementation.
/// </summary>
/// <param name="f"> Function to integrate as fpointer. </param>
/// <param name="a"> Integration segment start. </param>
/// <param name="b"> Integration segment end. </param>
/// <param name="n"> Elementary segment count. </param>
/// <returns> Integral value as double. </returns>
double simpson_mt(double (*f)(double x), double a, double b, int n);
integral.c
#include "pch.h"
#include "integral.h"
#include <omp.h>
/// <summary>
/// Numeric integration Simpson method
/// single-thread implementation.
/// </summary>
/// <param name="f"> Function to integrate as fpointer. </param>
/// <param name="a"> Integration segment start. </param>
/// <param name="b"> Integration segment end. </param>
/// <param name="n"> Elementary segment count. </param>
/// <returns> Integral value as double. </returns>
double simpson_1t(double (*f)(double x), double a, double b, int n)
       // Calculation storage
       double p1 = 0, p2 = \overline{0}, p3 = 0, p4 = 0;
       // h value
       double h = (b - a) / (double)(n);
       // 1st part
       p1 = 0.5 * f(a);
       // 2nd part
       for (int i = 1; i <= n - 1; i++)
             p2 += f(a + (double)i * h);
       // 3rd part
       for (int i = 1; i <= n; i++)
             p3 += f((2.0 * a + (2 * (double)i - 1) * h) / 2.0);
       p3 *= 2.0;
       // 4th part
       p4 = 0.5 * f(b);
       // Return
       return (h / 3.0) * (p1 + p2 + p3 + p4);
/// <summary>
/// Numeric integration Simpson method
/// multi-thread implementation.
/// </summary>
/// <param name="f"> Function to integrate as fpointer. </param>
/// <param name="a"> Integration segment start. </param>
/// <param name="b"> Integration segment end. </param>
/// <param name="n"> Elementary segment count. </param>
/// <returns> Integral value as double. </returns>
double simpson_mt(double (*f)(double x), double a, double b, int n)
       // Calculation storage
       double p1 = 0, p2 = \bar{0}, p3 = 0, p4 = 0;
       int i;
       // h value
       double h = (b - a) / (double)(n);
       // 1st part
       p1 = 0.5 * f(a);
       // 2nd part
       #pragma omp parallel for reduction(+:p2) schedule(static)
       for (i = 1; i <= n - 1; i++)
             p2 += f(a + (double)i * h);
       #pragma omp parallel for reduction(+:p3) schedule(static)
       for (i = 1; i <= n; i++)
             p3 += f((2.0 * a + (2 * (double)i - 1) * h) / 2.0);
       p3 *= 2.0;
       // 4th part
       p4 = 0.5 * f(b);
       // Return
       return (h / 3.0) * (p1 + p2 + p3 + p4);
```

## Дослідження швидкодії

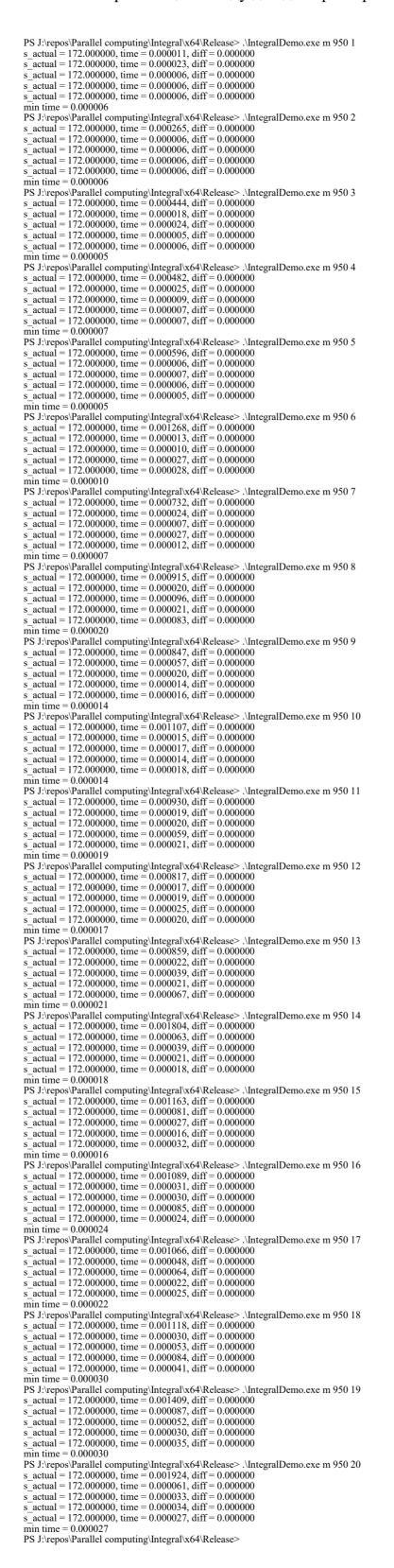
В дослідженні порівнюється швидкодія однопоточної та багатопоточної реалізацій методу для двох розмірностей розбиття: n1 = 950, n2 = 1100500. Кількість потоків для багатопоточної реалізації змінюється у межах [1; 20].

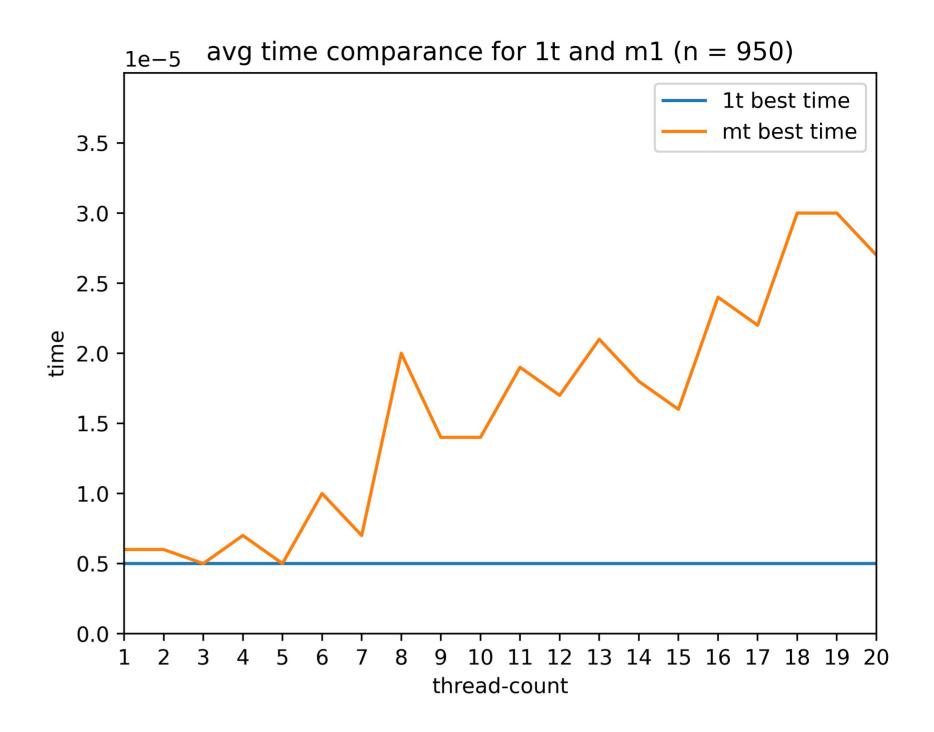
```
PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe s 950
     s_actual = 172.000000, time = 0.000005, diff = 0.000000
    s_actual = 172.000000, time = 0.000005, diff = 0.000000
s_actual = 172.000000, time = 0.000005, diff = 0.000000
     s actual = 172.000000, time = 0.000005, diff = 0.000000
     s actual = 172.000000, time = 0.000005, diff = 0.000000
     \min \text{ time} = 0.000005
    PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe s 1100500 s_actual = 172.000000, time = 0.005521, diff = 0.000000 s_actual = 172.000000, time = 0.005827, diff = 0.000000
     s actual = 172.000000, time = 0.005524, diff = 0.000000
     s_{actual} = 172.000000, time = 0.005753, diff = 0.000000
     s_{actual} = 172.000000, time = 0.005588, diff = 0.000000
    PS J:\repos\Parallel computing\Integral\x64\Release>
PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 1 s_actual = 172.000000, time = 0.005714, diff = 0.000000
  s actual = 172.000000, time = 0.005625, diff = 0.000000
 s_{\text{actual}} = 172.000000, time = 0.005648, diff = 0.000000
 s actual = 172.000000, time = 0.006128, diff = 0.000000
 s_{\text{actual}} = 172.000000, time = 0.005680, diff = 0.000000
PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 2 s_actual = 172.000000, time = 0.002988, diff = 0.000000 s_actual = 172.000000, time = 0.002832, diff = 0.000000
 s actual = 172.000000, time = 0.002945, diff = 0.000000
 s actual = 172.000000, time = 0.002892, diff = 0.000000
 s actual = 172.000000, time = 0.002842, diff = 0.000000
   \min_{\text{min time}} = 0.002832
PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 3 s actual = 172.000000, time = 0.002304, diff = 0.000000
 s actual = 172.000000, time = 0.001920, diff = 0.000000
 s_{actual} = 172.000000, time = 0.003713, diff = 0.000000
 s_{actual} = 172.000000, time = 0.003526, diff = 0.000000
 s actual = 172.000000, time = 0.003540, diff = 0.000000
 min time = 0.001920
PS J\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 4 s_actual = 172.000000, time = 0.002465, diff = 0.000000
 s_{actual} = 172.000000, time = 0.001757, diff = 0.000000
 s_{actual} = 172.000000, time = 0.001515, diff = 0.000000
 s actual = 172.000000, time = 0.001563, diff = 0.000000
 s actual = 172.000000, time = 0.001431, diff = 0.000000
  \overline{\text{min}} \text{ time} = 0.001431
 PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 5
 s actual = 172.000000, time = 0.002986, diff = 0.000000
 s_{actual} = 172.000000, time = 0.002237, diff = 0.000000
 s_actual = 172.000000, time = 0.002146, diff = 0.000000
s_actual = 172.000000, time = 0.002132, diff = 0.000000
 s actual = 172.000000, time = 0.002132, diff = 0.000000
 \overline{\text{min}} \text{ time} = 0.002132
 PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 6
s_actual = 172.000000, time = 0.002709, diff = 0.000000
s_actual = 172.000000, time = 0.001775, diff = 0.000000
 s actual = 172.000000, time = 0.002129, diff = 0.000000
 s actual = 172.000000, time = 0.001770, diff = 0.000000
 s_{actual} = 172.000000, time = 0.001837, diff = 0.000000
 \overline{\text{min}} \text{ time} = 0.001770
PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 7 s_actual = 172.000000, time = 0.003040, diff = 0.000000 s_actual = 172.000000, time = 0.001679, diff = 0.000000
 s actual = 172.000000, time = 0.001857, diff = 0.000000
 s actual = 172.000000, time = 0.001616, diff = 0.000000
 s_{actual} = 172.000000, time = 0.001671, diff = 0.000000
  min time = 0.001616
PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 8 s_actual = 172.000000, time = 0.002403, diff = 0.000000
 s actual = 172.000000, time = 0.001394, diff = 0.000000
 s_{actual} = 172.000000, time = 0.001389, diff = 0.000000
 s_{actual} = 172.000000, time = 0.001415, diff = 0.000000
 s actual = 172.000000, time = 0.002725, diff = 0.000000
  \frac{1}{1} min time = 0.001389
PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 9 s_actual = 172.000000, time = 0.003458, diff = 0.000000
 s actual = 172.000000, time = 0.002631, diff = 0.000000
 s_{actual} = 172.000000, time = 0.002648, diff = 0.000000
 s_{\text{actual}} = 172.000000, time = 0.002686, diff = 0.000000
 s actual = 172.000000, time = 0.002974, diff = 0.000000
 \overline{\text{min}} \text{ time} = 0.002631
PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 10 s_actual = 172.000000, time = 0.003445, diff = 0.000000
 s_actual = 172.000000, time = 0.002701, diff = 0.000000
 s actual = 172.000000, time = 0.002254, diff = 0.000000
 s actual = 172.000000, time = 0.002503, diff = 0.000000
 s actual = 172.000000, time = 0.002129, diff = 0.000000
  \overline{\text{min}} \text{ time} = 0.002129
 PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 11
 s actual = 172.000000, time = 0.002680, diff = 0.000000
  s actual = 172.000000, time = 0.002146, diff = 0.000000
 \bar{s} actual = 172.000000, time = 0.002188, diff = 0.000000
 s_{actual} = 172.000000, time = 0.002726, diff = 0.000000
 s_{actual} = 172.000000, time = 0.002190, diff = 0.000000
min time = 0.002146
PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 12
s_actual = 172.000000, time = 0.002488, diff = 0.000000
 s actual = 172.000000, time = 0.001989, diff = 0.000000
 s_{actual} = 172.000000, time = 0.001981, diff = 0.000000
 s actual = 172.000000, time = 0.002100, diff = 0.000000
 \bar{s} actual = 172.000000, time = 0.002117, diff = 0.000000
  min time = 0.001981
PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 13 s_actual = 172.000000, time = 0.002706, diff = 0.000000
 s_actual = 172.000000, time = 0.001922, diff = 0.000000
 s_{actual} = 172.000000, time = 0.002132, diff = 0.000000
s_actual = 172.000000, time = 0.002793, diff = 0.000000
s_actual = 172.000000, time = 0.002510, diff = 0.000000
 \overline{\text{min time}} = 0.001922
 PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 14
 s_actual = 172.000000, time = 0.002395, diff = 0.000000
 s_{actual} = 172.000000, time = 0.001715, diff = 0.000000
 s actual = 172.000000, time = 0.001648, diff = 0.000000
 s actual = 172.000000, time = 0.001874, diff = 0.000000
 s actual = 172.000000, time = 0.001749, diff = 0.000000
 \min_{\text{min time}} = 0.001648
PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 15 s_actual = 172.000000, time = 0.002636, diff = 0.000000
 s actual = 172.000000, time = 0.001691, diff = 0.000000
 s actual = 172.000000, time = 0.001565, diff = 0.000000
 s actual = 172.000000, time = 0.001589, diff = 0.000000
 s_{actual} = 172.000000, time = 0.001572, diff = 0.000000
 \overline{\text{min}} \text{ time} = 0.001565
PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 16 s_actual = 172.000000, time = 0.002284, diff = 0.000000
 s actual = 172.000000, time = 0.001495, diff = 0.000000
 s_{actual} = 172.000000, time = 0.002151, diff = 0.000000
 s_{actual} = 172.000000, time = 0.002187, diff = 0.000000
 s_{actual} = 172.000000, time = 0.001628, diff = 0.000000
  \min \text{ time} = 0.001495
PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 17 s_actual = 172.000000, time = 0.002716, diff = 0.000000
 s_{actual} = 172.000000, time = 0.002027, diff = 0.000000
 s_{actual} = 172.000000, time = 0.002025, diff = 0.000000
 s_{actual} = 172.000000, time = 0.001951, diff = 0.000000
 s actual = 172.000000, time = 0.001949, diff = 0.000000
 \overline{\text{min}} \text{ time} = 0.001949
PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 18 s_actual = 172.000000, time = 0.002724, diff = 0.000000
 s_actual = 172.000000, time = 0.001833, diff = 0.000000
s_actual = 172.000000, time = 0.001909, diff = 0.000000
s_actual = 172.000000, time = 0.002013, diff = 0.000000
 \bar{s} actual = 172.000000, time = 0.001907, diff = 0.000000
 \overline{min} time = 0.001833
 PS J:\repos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 19
 s_actual = 172.000000, time = 0.002554, diff = 0.000000
s_actual = 172.000000, time = 0.001781, diff = 0.000000
s_actual = 172.000000, time = 0.001763, diff = 0.000000
 \bar{s} actual = 172.000000, time = 0.001757, diff = 0.000000
 s_{actual} = 172.000000, time = 0.002273, diff = 0.000000
 \overline{\text{min}} \text{ time} = 0.001757
PS J:\tepos\Parallel computing\Integral\x64\Release> .\IntegralDemo.exe m 1100500 20 s_actual = 172.000000, time = 0.003139, diff = 0.000000
```

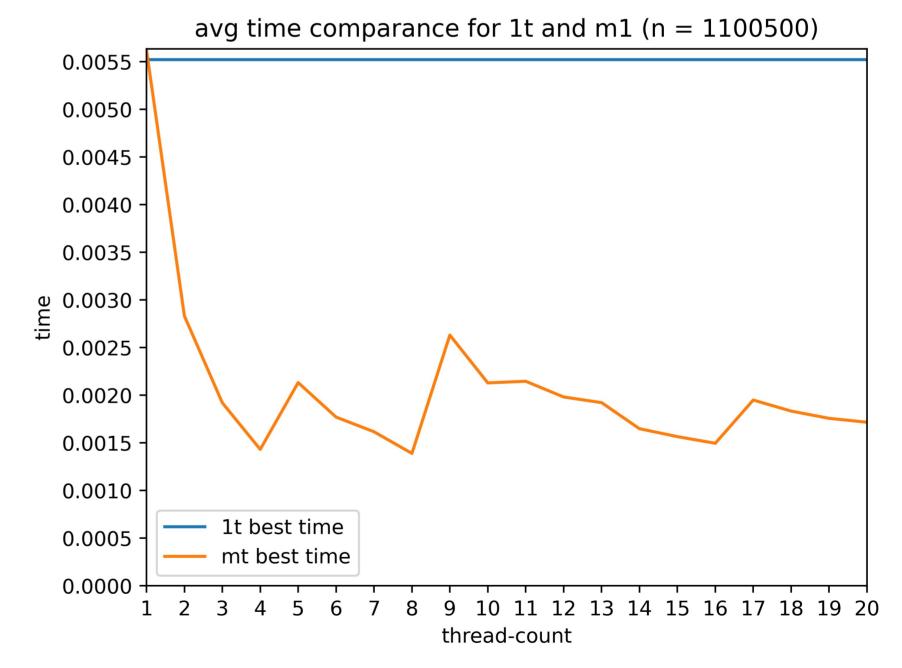
s\_actual = 172.000000, time = 0.001752, diff = 0.000000 s\_actual = 172.000000, time = 0.001716, diff = 0.000000 s\_actual = 172.000000, time = 0.001727, diff = 0.000000 s\_actual = 172.000000, time = 0.001793, diff = 0.000000

PS J:\repos\Parallel computing\Integral\x64\Release>

 $\sin time = 0.001716$ 







#### Висновки:

- Паралелізм значно погіршує швидкодію для малої розмірності задачі (n = 950).
- Паралелізм значно покращує швидкодію для великої розмірності задачі (n = 1100500).
- Найшвидше багатопоточна реалізація (n=1100500) працює при thread\_count = 8 (0.001389), 4 (0.001431), 16 (0.001495). Процесор, на якому здійснювалось тестування—Intel Core i5-8250U, має 4 ядер, 8 потоків. Таким чином доцільно обирати значення thread\_count, кратне кількості фізичних потоків системи.