## **B-Tree Psuedocode**

The pseudocode for BTree with arrays starting at 1 instead of 0.

#### **Definition of a B-Tree**

Belowe, we rewrite definition of B-Tree to use arrays starting with 0 instead of 1.

A B-tree is a rooted tree (whose root is T.root) having the following properties.

- 1. Every node *x* has:
  - (a) x.n, the number of keys currently stored in x
  - (b) x.n keys:  $x.key_0 < x.key_1 < ... < x.key_{n-1}$
  - (c) x.leaf, a Boolean which is true if x is a leaf and otherwise false
- 2. Each internal node x also contains x.n + 1 points  $x.c_0, x.c_1, \dots, x.c_{n-1}, x.c_n$  to its children. Leaf nodes have no children so their  $c_i$  values are null.
- 3. The keys  $x.key_i$  separate the ranges of keys stored in each subtree. If  $k_i$  is any key stored in the subtree with root  $x.c_i$ , then

$$k_0 < x.key_0 < k_1 < x.key_1 < ... < x.key_{n-1} < k_n$$

- 4. All leafs have the same depth, which is the height h of the tree.
- 5. The value  $t \ge 2$ , is called the minimum degree of the B-tree, helps define the structure of the tree as follows:
  - (a) Every note other than the root must have at least t-1 keys. Every internal node other than the root has at least t children. If the tree is non-empty, the root must have at least one key.
  - (b) Every node may contain at most 2t 1 keys. Thus an internal node may have at most 2t children. We say that a node is full if it contains exactly 2t 1 keys.

#### Some observations

• The root of the B-tree is always in main memory, so we never need to perform a DISK-READ on the root but we do need to perform a DISK-WRITE when the root node is changed.

- Any nodes that are passed as parameters already have had a DISK-READ operation performed on them.
- All procedures are "one-pass" algorithms that proceed downward from the root, without having to back up.
- We will access the key values and the child pointers using arrays inside the node x. They would need to be declared so they can hold a full node, so 2t 1 keys and 2t child pointers: x.key[0:2t-1] and x.c[0:2t] but we will access only the following values:

```
x.key[0]...x.key[x.n-1] and x.c[0]...x.c[x.n]
```

# **B-tree operations**

## Searching in a B-tree

- Generalization of binary tree search except at node x we make an  $(x \cdot n + 1)$ -way branching decision.
- The return value is a 2-tuple (y,i) consisting of a node y and an index i such that  $y.key_i = k$ , where we are searching for key k. If not found, the search returns NIL.

## **Creating an empty B-tree**

```
B-TREE-CREATE(T)
1. x = ALLOCATE-NODE()
2. x.leaf = TRUE
3. x.n = 0;
4. DISK-WRITE(x)
5. T.root = x
```

### Inserting into a B-tree

```
B-TREE-INSERT(T, k)
1. r = T.root
  if r.n == 2t-1
3.
       s = B-TREE-SPLIT-ROOT(T)
       B-TREE-INSERT-NONFULL(s, k)
5. else B-TREE-INSERT-NONFULL(r, k)
B-TREE-SPLIT-ROOT (T)
1. s = ALLOCATE-NODE()
2. s.leaf = FALSE
3. s.n = 0
4. s.c[0] = T.root
5. T.root = s
6. B-TREE-SPLIT-CHILD(s, 0)
7. return s
B-TREE-SPLIT-CHILD(x, i)
1. y = x.c[i] //full node to split
2. z = ALLOCATE-NODE() //z will take half of y
3. z.leaf = y.leaf
4. z.n = t - 1
5. for j = 0 to t - 2
                                 // z gets y greates keys
6. z.key[j] = y.key[j + t]
7. if not y.leaf
8.
    for j = 0 to t - 1
                                 // and it's corresponding children
9.
          z.c[j] = y.c[j + t]
10. y.n = t - 1
                                 // y keeps t - 1 keys
11. for j = x.n downto i+1
                                 // shift x's children to the right...
12. x.c[j + 1] = x.c[j]
13. x.c[i + 1] = z
                                 // to make room for z as a child
14. for j = x.n - 1 downto i
                                 // shift the corresponding keys in x
     x.key[j + 1] = x.key[j]
                                // insert y's median key
16. x.key[i] = y.key[t - 1]
17. x.n = x.n + 1
                                 // x has gained a child
18. DISK-WRITE(y)
19. DISK-WRITE(z)
20. DISK-WRITE(x)
```

```
B-TREE-INSERT-NONFULL(x, k)
1. i = x.n - 1
2. if x.leaf
                                     //inserting into a leaf
3.
       while i \ge 0 and k < x.key[i] //shift keys in x to make room for k
           x.key[i + 1] = x.key[i]
4.
5.
           i = i - 1
      x.key[i + 1] = k
6.
                                    //insert k in x
                                    //now x has 1 more key
7.
       x.n = x.n + 1
8.
       DISK-WRITE(x)
9. else while i \ge 0 and k < x.key[i] //find the child where k belongs
10.
            i = i - 1
11.
       i = i + 1
12.
       DISK-READ(x.c[i])
        if x.c[i].n = 2t - 1
13.
                             //splt the child if it is full
14.
            B-TREE-SPLIT-CHILD(x, i)
15.
            if k > x.key[i]
                                    //does k go into x.c[i] or x.c[i+1]
16.
                i = i + 1
17. B-TREE-INSERT-NONFULL(x.c[i], k)
```