## **Chapter 6: Heapsort**

Here is the psuedocode assuming arrays start at index 0. So an n element array has indices  $0, \ldots, n-1$ .

```
PARENT(i)
1. return (i - 1)/2 // integer division
LEFT(i)
1. return 2i + 1
RIGHT(i)
1. return 2i + 2
MAX-HEAPIFY(A, i) // heapification downward
   Pre-condition: Both the left and right subtrees of node i are max-heaps
                   and i is less than or equal to heap-size[A]
   Post-condition: The subtree rooted at node i is a max-heap
1. l = LEFT(i)
2. r = RIGHT(i)
3. if l < A.heap-size and A[l] > A[i]
      largest = 1
5. else largest = i
6. if r < A.heap-size and A[r] > A[largest]
      largest = r
8. if largest != i
      exchange A[i] with A[largest]
10.
      MAX-HEAPIFY(A, largest)
BUILD-MAX-HEAP (A)
//A[0:n-1] is an unsorted array
1. A.heap-size = n
2. for i = n/2 - 1 downto 0 //skip the leaves
3.
       MAX-HEAPIFY(A, i)
HEAPSORT (A)
// array A[0:n-1] is unsorted
1. BUILD-MAX-HEAP (A)
2. for i = n-1 downto 2
      exchange A[1] with A[i]
4.
       A.heap-size = A.heap-size - 1
       MAX-HEAPIFY(A, 0)
```

```
MAX-HEAP-MAXIMUM (A)
//0(1) time
1. if A.heap-size < 1</pre>
2. error "heap underflow"
3. return A[0]
MAX-HEAP-EXTRACT-MAX (A)
//O(lq n) time
1. max = MAX-HEAP-MAXIMUM(A)
2. A[0] = A[A.heap-size - 1]
3. A.heap-size = A.heap-size - 1
4. MAX-HEAPIFY(A, 0)
5. return max
MAX-HEAP-INCREASE-KEY(A, i, key)
//O(lg n) time
1. if newKey < A[i].key</pre>
    then error "new key must be larger than current key"
3. A[i].key = newKey
4. while i > 0 and A[PARENT(i)].key < A[i].key
5.
       exchange A[i] and A[PARENT(i)] (and update the object to index map)
6.
       i = PARENT(i)
MAX-HEAP-INSERT(A, x, n)
//O(\log n) time
1. if A.heap-size == n
2.
      error "heap overflow"
3. A.heap-size = A.heap-size + 1
4. k = x.key
5. x.key = -infinity //Integer.MIN_VALUE, for example
6. A[A.heap-size - 1] = x
7. MAX-HEAP-INCREASE-KEY(A, A.heap-size - 1, k)
```