

# Distributed Coordination



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- ▶ Topics:
  - ▶ Notion of *global time*: absolute time versus relative time
  - ▶ *Election algorithms*: for electing a *coordinator* on-the-fly
  - ▶ *Distributed mutual exclusion*

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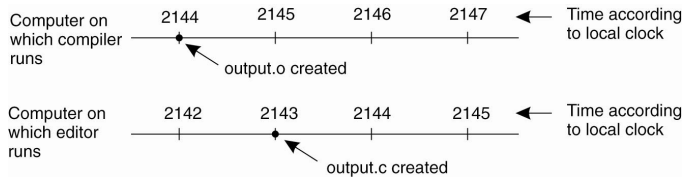
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- ▶ The time is stored on a battery-backed CMOS RAM. At every clock tick, the interrupt service procedure adds one to the stored time.
- ▶ With one computer even if the time is off it is usually not a problem. With  $n$  computers, all  $n$  crystals will run at slightly different rates, causing the software clocks to gradually get out of sync. This difference in time values is called **clock skew**.



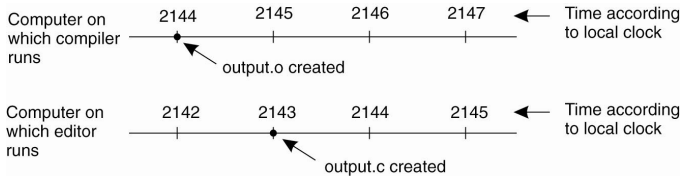
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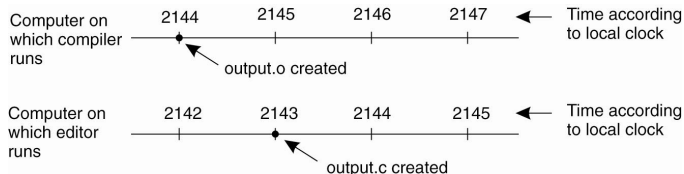
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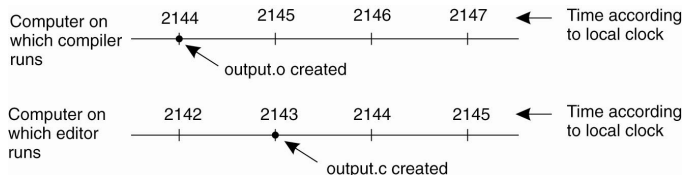
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- ▶ **In-class Exercise:** Come up with an example where clock skew causes a build system to compile a file unnecessarily.
- ▶ **In-class Exercise:** Come up with another scenario where a build system misses that a file has changed due to clock skew.

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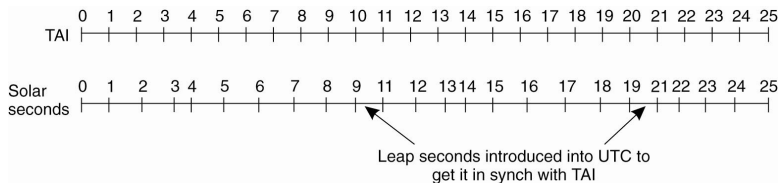
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- ▶ UTC is broadcast over short-wave by NIST on station WWV (and from satellites). See <http://www.nist.gov>.



# Leap Seconds



- ▶ TAI seconds are of constant length, unlike solar seconds. Leap seconds are introduced when necessary to keep in phase with the sun.

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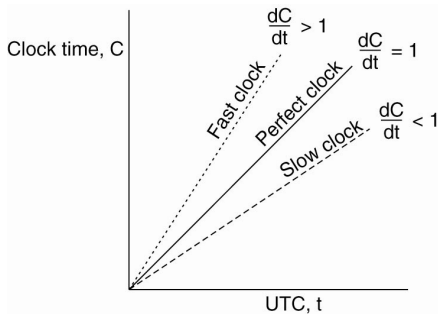
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- ▶ Typical accuracy is 1-5m but can be as good as less than one foot

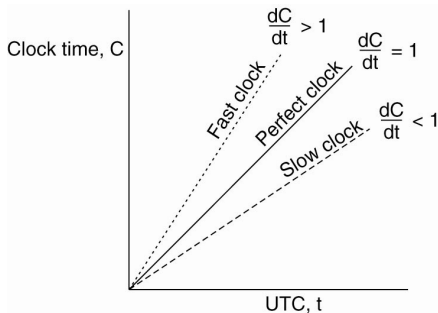
GPS Animation

# Clock Synchronization Algorithms



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- ▶ Let maximum drift rate be  $\rho$ . Then  $1 - \rho \leq dC/dt \leq 1 + \rho$  where  $dC/dt$  is the rate of drift of the clock relative to UTC. Ideally, we want  $dC/dt$  to be 1. To ensure two clocks never differ more than  $\delta$ , the clocks must be synchronized at least every  $\delta/2\rho$  seconds.



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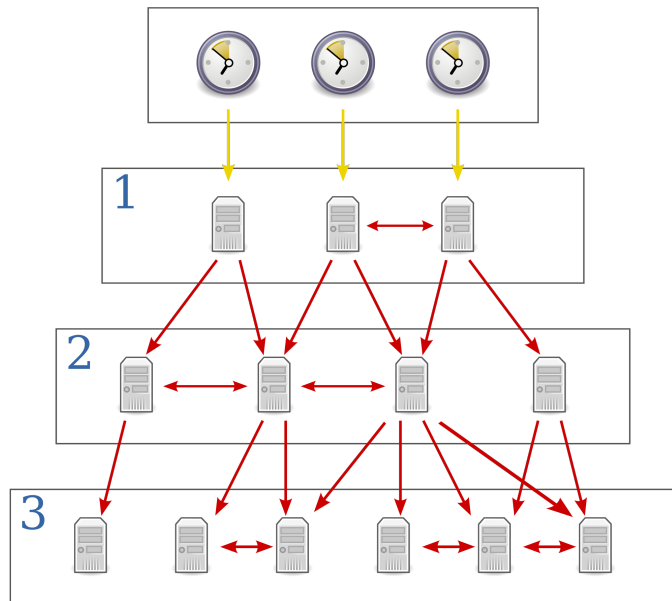
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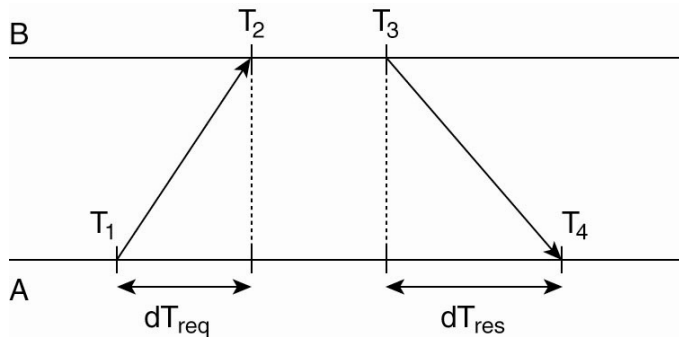
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- ▶ Clients need to slow down or speed up local clocks to sync up gradually with a server.

# Network Time Protocol (2)



## Network Time Protocol (3)



- ▶ Getting the current time from a time server. Relative offset  $\theta = T_3 + ((T_2 - T_1) + (T_4 - T_3))/2 - T_4$

# Network Time Protocol (4)

- ▶ NTP can be setup pair-wise between servers. Both servers ask each other for time and calculate the  $\theta$  and  $\delta$ , where

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- ▶ A server with a reference clock such as a WWV receiver or an atomic clock is a stratum-1 server. When A contacts B it will only adjust its clock if its stratum number is higher than B. Moreover, after the synchronization, A's stratum level becomes one more than B's level

# Synchronized Time in the Lab

- ▶ The command `pdsh` runs a parallel/distributed shell across the nodes.

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[amit@onyx ~]$ pdsh -w onyxnode[01-63] date | sort
onyxnode01: Wed Mar  9 06:18:26 MST 2020
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.
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- ▶ Try `pdsh -w onyxnode[01-60] date --rfc-3339=ns | sort` to see time in nanoseconds resolution.

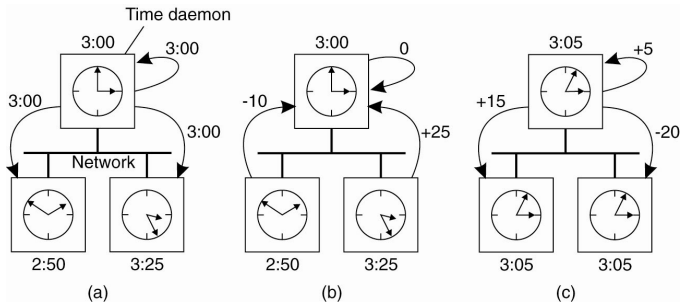
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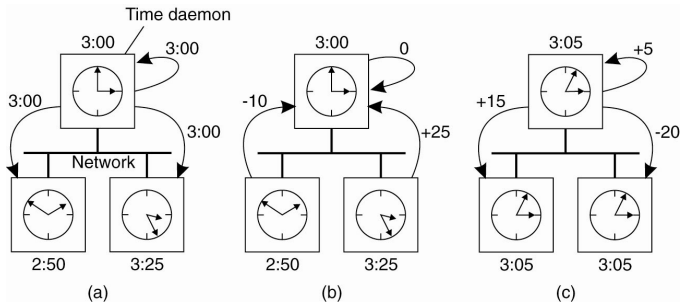
- ▶ Try `pdsh -w onyxnode[01-60] date --rfc-3339=ns | sort` to see time in nanoseconds resolution.
- ▶ The cluster uses **NTP** (Network Time Protocol) daemons on each node to keep the machines synchronized. To see the daemon processes, try the command `pdsh -w node[01-60] ps aux | grep ntpd`. On some Linux systems `ntpd` has been replaced by `chronyd`.

# Berkeley Time Algorithm



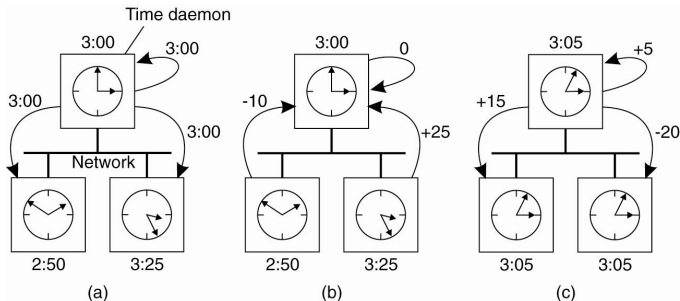
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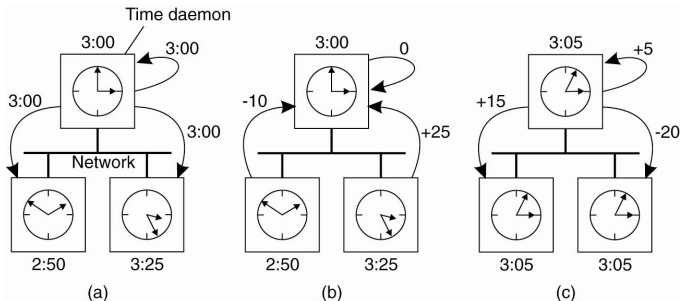
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- ▶ **In-class Exercise.** How would you implement the Berkeley Time Algorithm?

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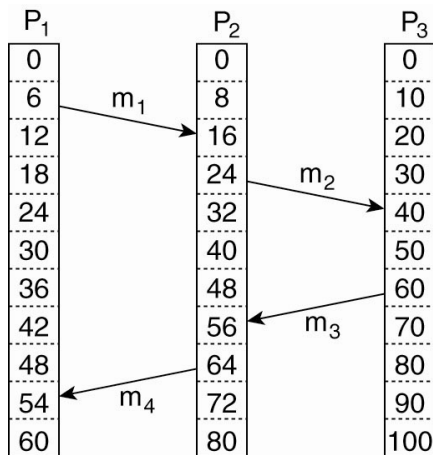
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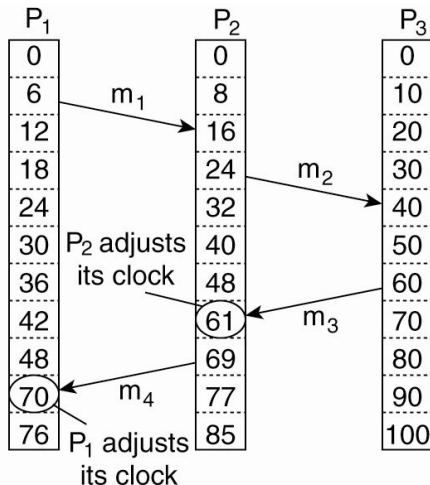
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- ▶ Some noteworthy logical clock algorithms:
  - ▶ **Lamport timestamps**, which are monotonically increasing software counters.
  - ▶ **Vector clocks**, that allow for partial ordering of events in a distributed system.
  - ▶ **Version vectors**, order replicas, according to updates, in an optimistic replicated system.
  - ▶ **Matrix clocks**, an extension of vector clocks that also contains information about other processes' views of the system.

# Lamport's Logical Clocks (1)



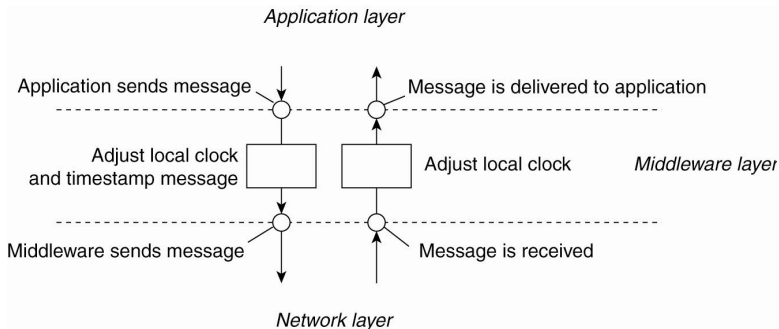
- ▶ Three processes, each with its own clock.

## Lamport's Logical Clocks (2)



- Lamport's algorithm corrects the clock by adjusting the timestamps.

# Lamport's Logical Clocks (3)



- ▶ The positioning of Lamport's logical clocks in a distributed system.



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- ▶ In addition, between every two events the clock must tick at least once.
- ▶ No two events ever occur at exactly the same time. Tag process ids to low bits of time to make time be unique since process ids are unique.



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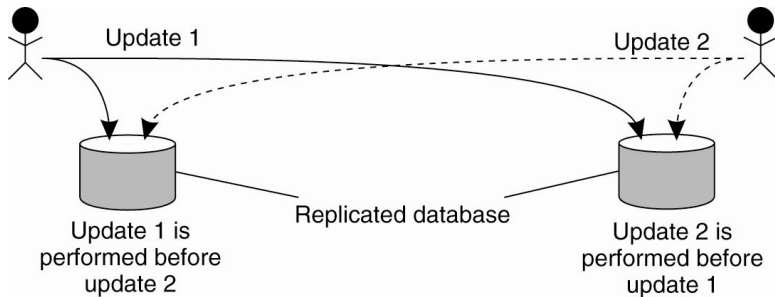
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Step 3. Upon the receipt of a message  $m$ , process  $P_j$  adjusts its own local counter as

$$C_j \leftarrow \max\{C_j, ts(m)\}$$

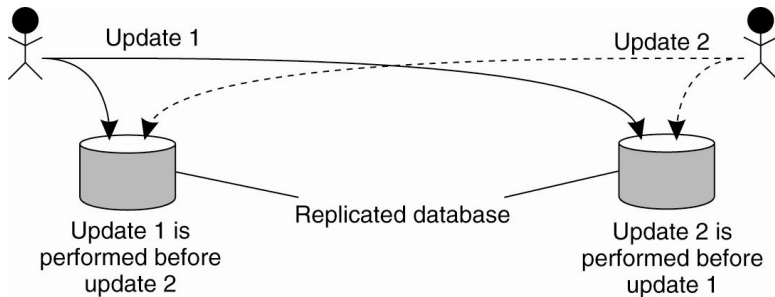
after which it then executes the first step and delivers the message to the application.

## Example: Totally Ordered Multicasting (1)



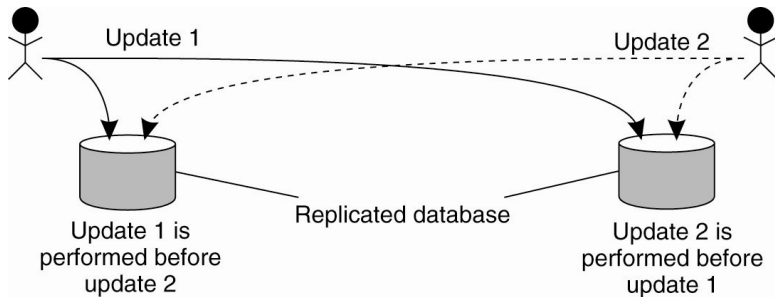
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- ▶ Updating a database and leaving it in an inconsistent state. Consider two transactions on an account with a balance of \$1,000.
  - ▶ *Transaction A*: Customer wants to deposit \$100 to the account in Boise.
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- ▶ Lamport timestamps can be used to fix this problem.

## Example: Totally Ordered Multicasting (2)

- ▶ **Totally Ordered Multicast:** A multicast operation by which all messages are delivered in the same order to each receiver.



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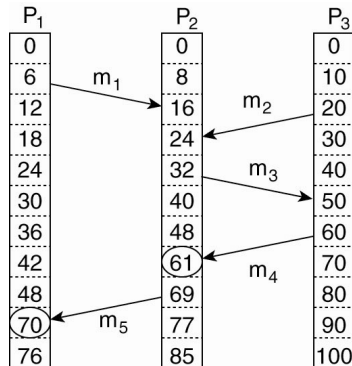
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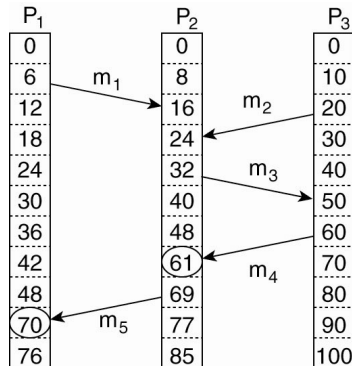
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- ▶ A process puts received messages into a queue ordered by timestamps. It acknowledges the messages with a multicast to all other processes. Eventually the local queues are the same at all processes.
- ▶ A process can deliver a queued message to an application only if it is at the head of queue and has been acknowledged by each other process.

# Vector Clocks (1)



- Concurrent message transmission using Lamport logical clocks. Knowing that  $m_1$  was received before  $m_2$  doesn't tell us if they are connected. Knowing that  $m_3$  was sent after receiving  $m_1$  means that they are likely causally connected.

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- ▶ Lamport clocks do not capture **causality**. We need *vector clocks* to capture causality.

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- ▶ **Vector clock:** A vector clock  $VC(a)$  assigned to an event  $a$  has the property that if  $VC(a) < VC(b)$  for some event  $b$ , then event  $a$  is known to causally precede event  $b$ .



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  - Step 2. If  $VC_i[j] = k$  then  $P_i$  knows that  $k$  events have occurred at  $P_j$ .  
It is thus  $P_i$ 's knowledge of the local time at  $P_j$ .

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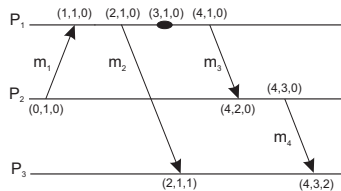
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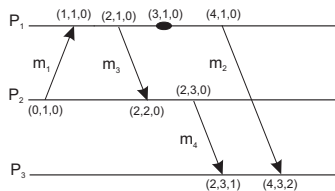
$$VC_j[k] \leftarrow \max\{VC_j[k], ts(m)[k]\}, \forall k$$

after which it executes the first step and delivers the message to the application.

# Vector Clocks (4)



(a)

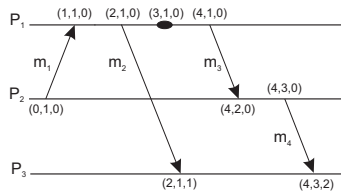


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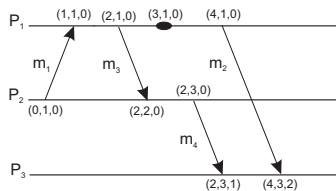
Capturing potential causality when exchanging messages



# Vector Clocks (4)



(a)



(b)

Capturing potential causality when exchanging messages

Situation	$ts(m_2)$	$ts(m_4)$	$ts(m_2) < ts(m_4)$	$ts(m_2) > ts(m_4)$	Conclusion
(a)	(2, 1, 0)	(4, 3, 0)	Yes	No	$m_2$ may causally precede $m_4$
(b)	(4, 1, 0)	(2, 3, 0)	No	No	$m_2$ and $m_4$ may conflict

We say that  $ts(a) < ts(b)$ , if and only if,  $ts(a)[k] \leq ts(b)[k], \forall k$  and there is at least one  $k'$  such that  $ts(a)[k'] < ts(b)[k']$

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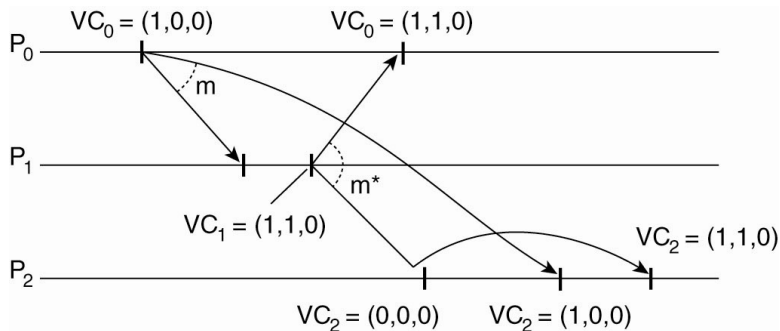
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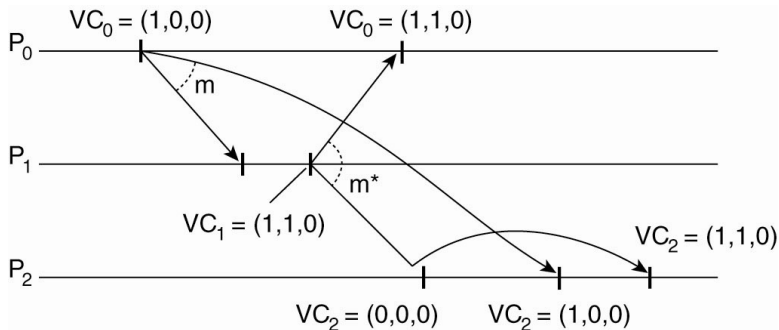
( $P_j$  has seen all the messages that have been seen by  $P_i$  when it sent message  $m$ )

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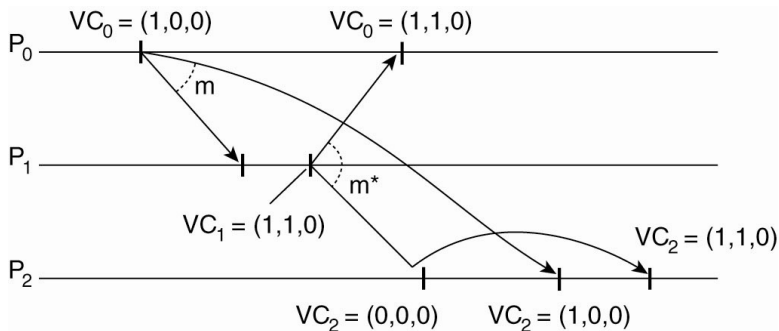
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- ▶ On  $P_2$ : The message  $m^*$  arrives sooner than  $m$ . The delivery of  $m^*$  is delayed by  $P_2$  until  $m$  has been received and delivered to  $P_2$ 's application layer.

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- ▶ Middleware deals with message ordering:
  - ▶ The middleware cannot tell what the message contains so only potential causality is captured.
  - ▶ Two messages sent by the same process are always marked as causally related.
- ▶ Middleware cannot be aware of external communication.  
Ordering issues can only be adequately solved by looking at the application for which the communication is taking place.  
This is known as the **end-to-end argument**.

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- ▶ *Goal:* When an election starts, it ends with all processes agreeing on who the coordinator is.

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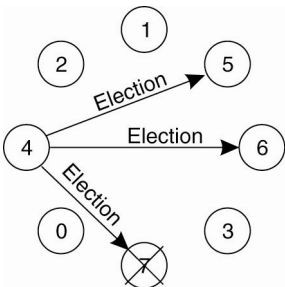
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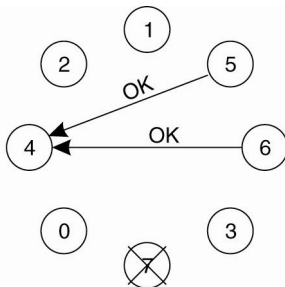
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- ▶ The new coordinator sends a message to all processes announcing that it is the new coordinator.
- ▶ Several elections can be running simultaneously. If a process that was down previously comes back up, it immediately runs an election. The “biggest” process in town always wins, hence the name “**bully algorithm**.”



## Bully Algorithm (2)

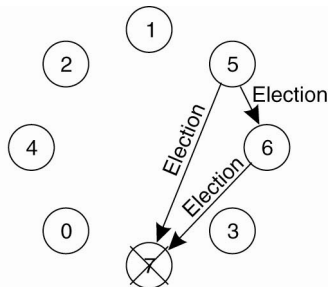


(a)



Previous coordinator  
has crashed

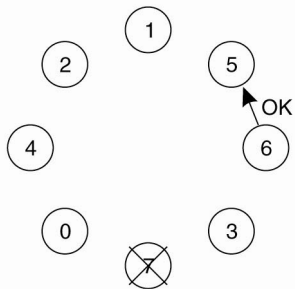
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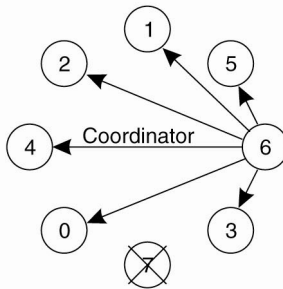
(c)

- (a) Process 4 holds an election.
- (b) Processes 5 and 6 respond, telling 4 to stop.
- (c) Now 5 and 6 each hold an election.

# Bully Algorithm (3)



(d)



(e)

(d) Process 6 tells 5 to stop.

(e) Process 6 wins and tells everyone.

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- ▶ If Process 7 comes back up, it just sends a new election message and bullies them into submission.
- ▶ We can use **Are You Alive** messages periodically to speed up detection of absconding coordinators

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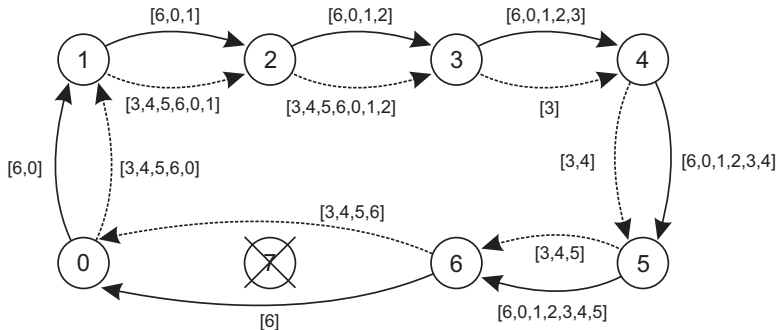
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- ▶ Then the message type is changed to **COORDINATOR** and the message circulates once again so everyone knows the new coordinator and the new ring configuration.

## Ring Algorithm (2)



Election algorithm using a ring. Elections were initiated by  $P_6$  and  $P_3$ .

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  - ▶ Solutions use either DHT (**Distributed Hash Tables**) or randomly unstructured layouts.

# References

- ▶ Time, clocks, and the ordering of events in a distributed system. Leslie Lamport. *Communications of the ACM* 21 (7): 558–565, 1978.
- ▶ Time is an illusion. Lunchtime doubly so. George V. Neville-Neil. *Communications of the ACM*, January 2016, Vol. 59. No. 1, pages 50–55. [Note: this article is only accessible on campus]