## Spark Examples

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- Wordcount
- Case-Analysis
- ▶ Top N Patents
- Pagerank

## Correlation

- Correlation is any statistical association. Most commonly refers to the degree to which a pair of variables are *linearly related*.
- ▶ A causal relationship implies correlation but the presence a correlation is not sufficient to infer the presence of a causal relationship.
- Pearson correlation coefficientis commonly used. It reflects a linear relationship (which may be present even when one variable is a nonlinear function of the other).
- ▶ The Pearson correlation coefficient between two random variables X and Y with expected values  $\mu_X$  and  $\mu_Y$  and standard deviations  $\sigma_X$  and  $\sigma_Y$  is defined as:

$$\rho X, Y = corr(X, Y) = \frac{cov(X, Y)}{\sigma_X \sigma_Y}$$
 (1)

$$= \frac{E[(X-\mu_X)(Y-\mu_Y)]}{\sigma_X \sigma_Y}$$
 (2)

▶ The value is in the range (-1,+1). +1 is perfect increasing/direct linear relationship, -1 is perfect decreasing/inverse linear relationship. As it approaches zero there is less of a relationship (closer to uncorrelated).

## P-value

- ► To quantify the idea of *statistical significance*.
- ▶ The p-value is defined as the probability, under the null hypothesis H, about the unknonw distribution F of the random variable X, for the variate to be observed as a value equal to or more extreme than the value observed.
- ▶ For example, this could be  $Pr(X \ge x|H)$  (right-tail event) or be  $Pr(X \le x|H)$  (left-tail event) or  $min\{Pr(X \le x|H), Pr(X \ge x|H)\}$  (double-tail event)
- The null hypothesis H is rejected if any of these probabilities is less than or equal to a small, fixed but arbitrarily pre-defined threshold value α, which is referred to as the level of significance.
- ▶ The setting of  $\alpha$  is arbitrary. By convention,  $\alpha$  is commonly set to 0.05, 0.01, 0.005, or 0.001.