

This course was developed as a part of the VLIR-UOS Cross-Cutting project s:

•Statistics: 2011-2016, 2017.

•Statistics: 2017.

Statistics for development: 2018-2020.



The >eR-Biostat initiative
Making R based education materials in
statistics accessible for all

An introduction to R: Short Version (2017)

Part 2: basic programming

Developed by

Dan Lin (Hasselt University) and Ziv Shkedy (Hasselt University)

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ER-BioStat





Overview

- 1. Basic programming in R: objects in R
- 2. Reading external datasets
- 3. Programming in R: a for loop
- 4. Programming in R: user functions
- 5. Application of a for loop: bootstrap.

Chapter 1 Basic programming Objects in R

Simple objects

Vectors

A function in R that creates a vector: c()

```
> x<-c("A","A","A","B","B","B","B")
> x
[1] "A" "A" "A" "B" "B" "B" "B"
```

Index vectors

All the elements in y for which x=A

```
> ya<-y[x=="A"]
> ya
[1] 10 11 9 15
```

```
> yb<-y[x=="B"]
> yb
[1] 3 5 7 2
```

Data frames

A data structure which contains more than 1 object.

Objects can be numeric objects and character objects

```
> z<-data.frame(x,y)</pre>
  x y
1 A 10
2 A 11
3 A 9
4 A 15
5 B 3
6 B 5
 B 7
  В
8
```

The \$

The object x in z

```
> z$x
[1] A A A A B B B B
Levels: A B
> z$y
[1] 10 11 9 15 3 5 7 2
```

Matrix

Rows and columns

```
X_{ij} = x[i,j]
```

The matrix reloaded

```
> matw+10
      [,1] [,2] [,3]
[1,] 11 12 210
[2,] 12 13 14
[3,] 50 19 6010
```

```
>
[1] 1 3 6000
```

The inverse matrix

```
> solve(matw)

[,1] [,2] [,3]

[1,] -0.687854189 0.39056517 0.0226680962

[2,] 0.453361924 0.07658141 -0.0151631184

[3,] 0.003905652 -0.00271864 0.0000382907
```

Example: data frame

Example: an R object of a data frame

Practical session

Create the folowig data frame:

Α	100
В	99
С	105
D	35
Ε	0
F	250

Chapter 2 Reading external datasets

Read an external file (text file)

> names(spwh3)<-c("id","y","x1","gender")

Read an external file (csv file)

```
> gsw.ts <- read.csv("C:/projects/NBA/GSW_TS.csv",header = FALSE,sep =";")
```

The data

>	spwł	า3		
	id	У	x1	gender
1	1	10.111368	1	0
2	2	9.948930	1	0
3	3	10.322560	1	0
4	4	10.241052	1	0
5	5	9.911427	1	0
6	6	9.357969	1	0
7	7	10.649141	1	0
8	8	10.150197	1	0
9	9	9.403218	1	0
10	10	8.027072	1	0
11	11	20.020056	1	1

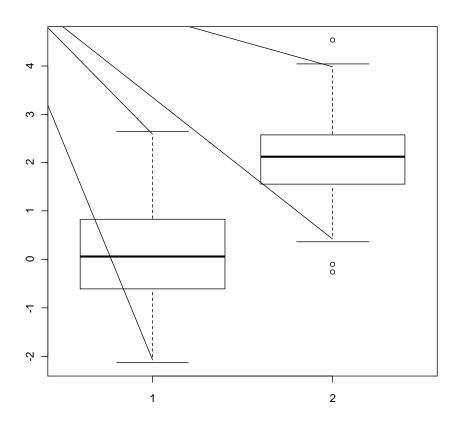
The sleep data in R

>	sleep		
	extra	group	ID
1	0.7	1	1
2	-1.6	1	2
3	-0.2	1	3
4	-1.2	1	4
5	-0.1	1	5
			•
14	0.1	2	4
15	-0.1	2	5
16	4.4	2	6
17	5.5	2	7
18	1.6	2	8
19	4.6	2	9
20	3.4	2	10

Two samples t-test

```
> y1<-spwh3$y[spwh3$gender==0]</pre>
> y2<-spwh3$y[spwh3$gender==1]</pre>
> t.test(y1,y2)
        Welch Two Sample t-test
data: y1 and y2
t = -9.1428, df = 58, p-value = 7.715e-13
alternative hypothesis: true difference in means is not
equal to 0
95 percent confidence interval:
 -12.229889 -7.836547
sample estimates:
mean of x mean of y
 14.99933 25.03254
```

Two samples t-test



- > y1<-rnorm(100,0,1)
- > y2<-rnorm(57,2,1)
- > boxplot(y1,y2)

Two samples t-test

```
> t.test(y1,y2)
        Welch Two Sample t-test
data: y1 and y2
t = -14.2203, df = 126.176, p-value < 2.2e-16
alternative hypothesis: true difference in means is not
equal to 0
95 percent confidence interval:
 -2.290641 -1.730980
sample estimates:
mean of x mean of y
-0.0063866 2.0044240
```

R object for the output

```
> t.t<-t.test(y1,y2)
> summary(t.t)
            Length Class
                           Mode
statistic
                           numeric
                    -none-
parameter
                    -none- numeric
p.value
                    -none- numeric
conf.int
                    -none- numeric
estimate
                    -none- numeric
null.value
                    -none- numeric
alternative
                    -none- character
method
                    -none- character
data.name
                    -none- character
```

R object for the output

> t.t

Welch Two Sample t-test data: y1 and y2 t = -14.2203, df = 126.176, p-value < 2.2e-16 alternative hypothesis: true difference in means is not equal to 0 95 percent confidence interval: -2.290641 -1.730980 sample estimates: mean of x mean of y -0.0063866 2.0044240 > t.t\$p.value [1] 5.570543e-28 > t.t\$statistic + -14.22034

Practical session

Create the following text file:

```
A 100
B 99
C 105
D 35
E 0
F 250
```

and read it to R as an external file

Chapter 3 Programming I: A for loop

A for loop

```
for(i in 1:B)
{
```

Here you ask from R to do the same thing B times.....

Generate 1000 samples from N(2,1)

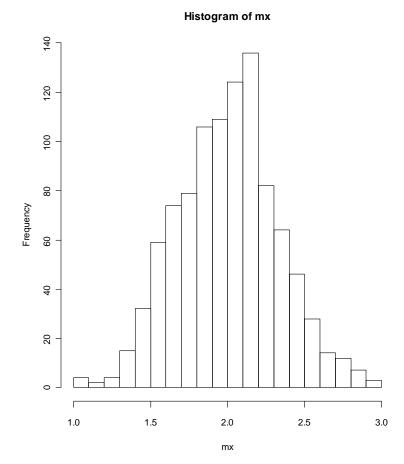
A random sample from N(2,1). Sample size=10. $X_i \sim N(\mu = 2, \sigma = 1)$

```
> x<-rnorm(10,2,1)
> X
 [1] 2.1531462 2.4426189 0.8080064 1.4051178 1.9392356 0.6466574
 [7] 0.7519918 -0.1097367 2.3338487 3.7598694
> x<-rnorm(10,2,1)
> X
 [1] 2.9694328 1.1065506 1.5612572 0.3904008 1.6890423 3.7319756 0.9026146
  [8] 1.7763012 2.4356002 0.9643299
> x<-rnorm(10,2,1)
> X
 [1] 2.1888795 2.6353313 2.7131707 1.2311123 2.8258664 0.8101126 2.1533630
[8] 2.9126222 0.4085356 1.5586004
> mean(x)
[1] 1.943759
```

Generate 1000 samples from N(2,1)

mx: A vector of 1000 numbers

```
> mx<-c(1:1000)
> for(i in 1:1000)
+ {
+ x<-rnorm(10,2,1)
+ mx[i]<-mean(x)
+ }
> hist(mx,nclass=25)
```



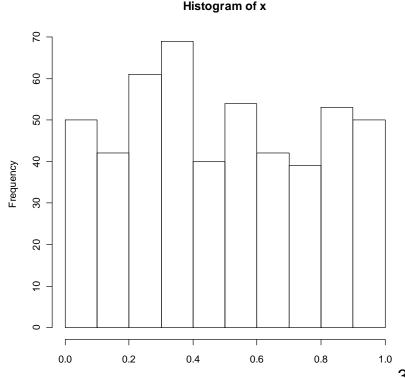
A random sample from N(2,1). Sample size=10.

Repeat this 1000 times

- Generate 1000 samples (n=50) from U(0,1).
- Calculate the minimum of each sample.
- Estimate the density of the minimum.

- Generate 1000 samples (n=50) from U(0,1).
- Calculate the minimum of each sample.

```
> x<-runif(500,0,1)
> hist(x)
> min(x)
[1] 0.004631357
```



Х

Estimate the density of the minimum.

```
for(i in 1:B)
{
Generate 1000 samples (n=50) from U(0,1).
Calculate the minimum of each sample.
}
```

Estimate the density of the minimum.

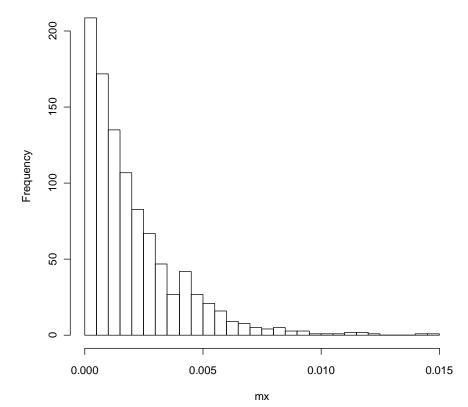
```
for(i in 1:B)
{
Generate 1000 samples (n=50) from U(0,1).
Calculate the minimum of each sample.
}

> mx<-c(1:1000)
> for(i in 1:1000)
+ {
+ x<-runif(500,0,1)
+ mx[i]<-min(x)
+ }</pre>
```

Estimate the density of the minimum.

```
> mx<-c(1:1000)
> for(i in 1:1000)
+ {
+ x<-runif(500,0,1)
+ mx[i]<-min(x)
+ }
>hist(mx)
```

Histogram of mx



Practical session

Make a for loop that print your name 500 times.

Chapter 4

Programming in R II: User functions

Generate s random sample pf size 1000 from N(0,3)

A user function: general form

```
function name<-function(x)
{</pre>
```

R commands (what do you what that the function will do for you.....)

}

A user function: general form

```
function name<-function(x)
{
</pre>
```

Input: a sample

Output:

- Descriptive statistics: mean, median, quantiles
- Graphical output: histogram

R functions for the output:

```
mean()
median()
quantile(x)
hist()
```

A user function: general form

A small program to produce the output:

```
mean.x<-mean(x)
med.x<-median(x)
quantile(x)
hist(x)</pre>
```

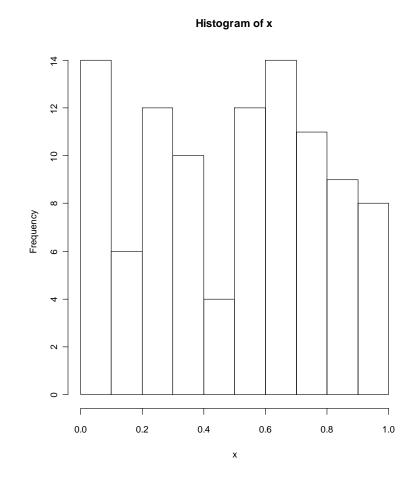
See slide 39.

A user function: example

```
fch20<-function(x)
                           The input
mean.x<-mean(x)
med.x < -median(x)
                       The output
q.x<-quantile(x)
hist(x)
return(mean.x,med.x,q.x)
```

A user function: output

```
> z<-runif(100,0,1)</pre>
> fch20(z)
$mean.x
[1] 0.4947539
$med.x
[1] 0.5291341
$q. x
        0%
                   25%
   50%
                          100%
               75%
0.01240262 0.24212404
   0.52913405 0.72482479
   0.98413912
Warning message:
In return(mean.x, med.x, q.x) :
   multi-àrgument returns aré
   deprecated
>
```



Practical session

 Write a function which receive a numerical vector as an input and calculate the mean of the vector.

Chapter 5: Application : the for loop

The bootstrap estimate of the standard error for the mean

The observed data

A sample of 10 observations:

```
> x <- c(11.201, 10.035, 11.118, 9.055, 9.434, 9.663, 10.403, 11.662, 9.285,8.84)
```

> mean(x)

[1] 10.0696

We wish to estimate the standard error of the sample mean

$$S.E(\bar{x}) = \frac{\sigma_F}{\sqrt{n}}$$

Parametric and nonparametric bootstrap

nonparametric bootstrap

$$F \rightarrow (x_1, x_2, ..., x_n)$$

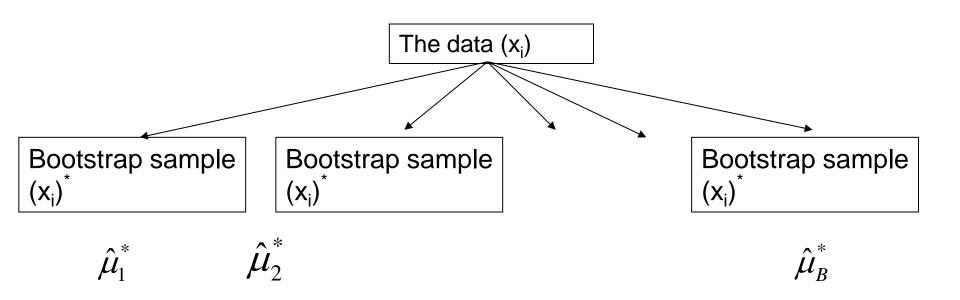
We resample from the empirical distribution parametric bootstrap

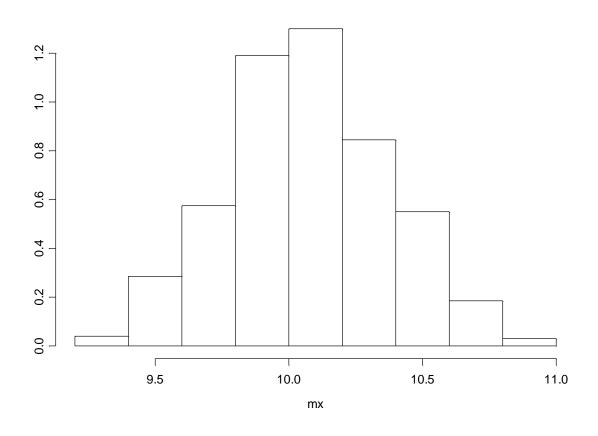
We assume a parametric model for F

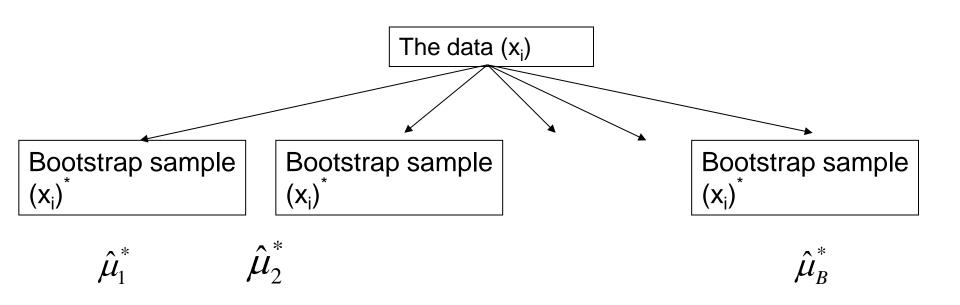
$$F(\theta)$$

We resample from

$$F(\hat{\theta})$$







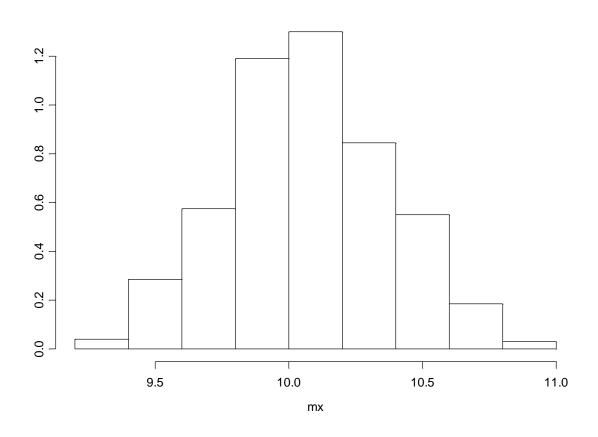
$$S.E.(\hat{\mu}) = \left\{ \frac{1}{B-1} \sum_{b=1}^{B} (\hat{\mu}_b^* - \hat{\mu}^*)^2 \right\}^{0.5}$$

R code

```
> var(mx)
[1] 0.09357364
```

The estimated standard error 0.093

```
n<-length(x)
B<-1000
mx<-c(1:B)
for(i in 1:B){
  cat(i)
boot.i<-sample(x,n,replace=T)
mx[i]<-mean(boot.i)
}</pre>
```



Parametric bootstrap

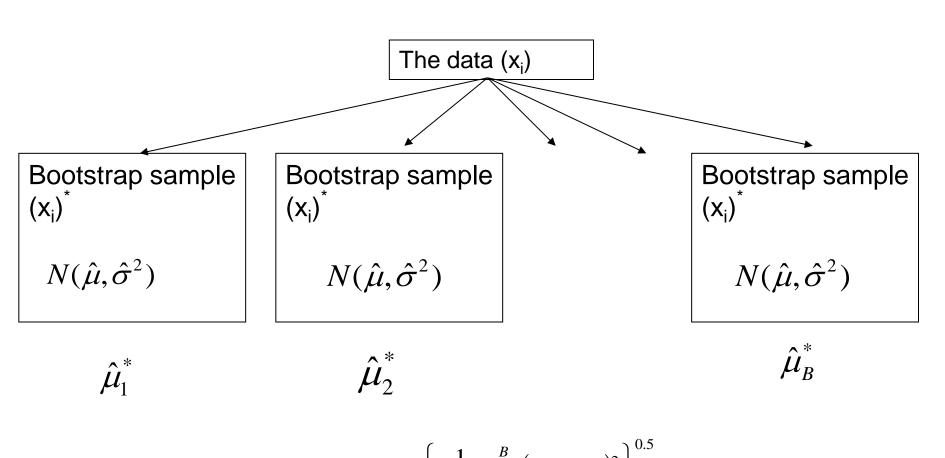
We assume a parametric model for F

We estimate F by

$$F = N(\mu, \sigma^2) \qquad \hat{F} = N(\hat{\mu}, \hat{\sigma}^2)$$

We replace the unknown parameters in F with their plug-in estimates

Parametric bootstrap



$$S.E.(\hat{\mu}) = \left\{ \frac{1}{B+1} \sum_{b=1}^{B} (\hat{\mu}_b^* - \hat{\mu}^*)^2 \right\}^{0.5}$$

R code

```
> var(mx)
[1] 0.1007613
```

Bootstrap estimate for the standard error for the mean

```
B<-1000
MLx<-mean(x)
Varx<-var(x)
mx<-c(1:B)
for(i in 1:B){
  cat(i)
boot.i<-rnorm(n,MLx,sqrt(Varx))
mx[i]<-mean(boot.i)
}</pre>
```

Parametric bootstrap

