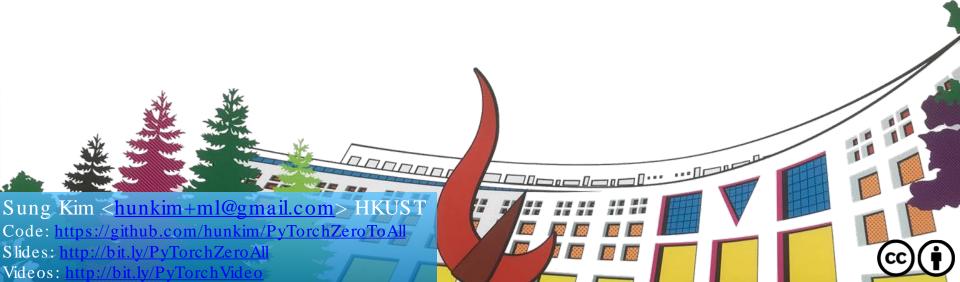
### ML/DL for Everyone with PYTERCH

Lecture 4: Back-propagation



#### Call for Comments

Please feel free to add comments directly on these slides.

Other slides: <a href="http://bit.ly/PyTorchZeroAll">http://bit.ly/PyTorchZeroAll</a>



#### ML/DL for Everyone with PYTORCH

Lecture 4: Back-propagation & Autograd



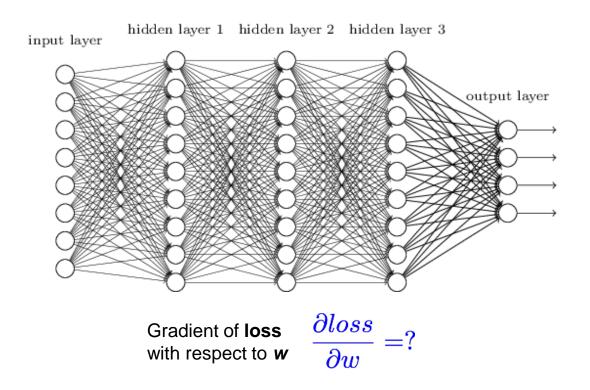
#### Computing gradient in simple network



```
Gradient of loss with respect to \frac{\partial loss}{\partial w} = ?
```

```
# compute gradient
def gradient(x, y): # d_loss/d_w
   return 2 * x * (x * w - y)
```

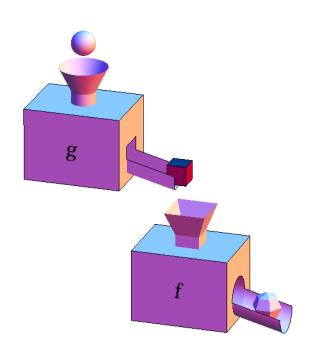
#### Complicated network?



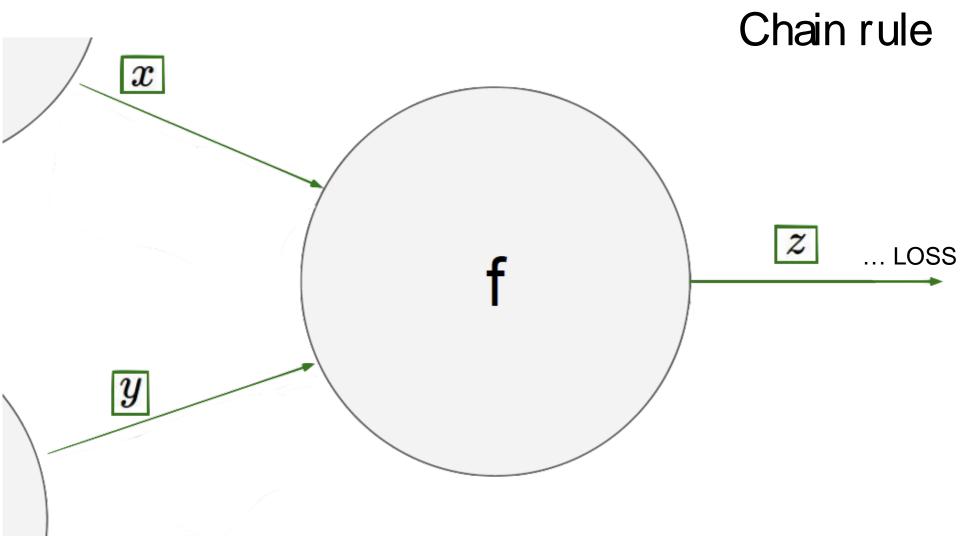
#### Better way? Computational graph + chain rule

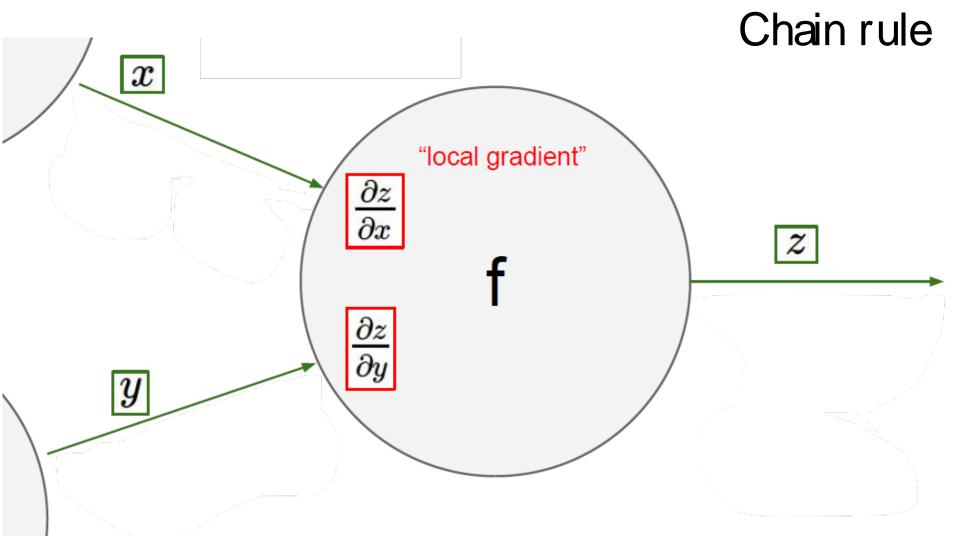


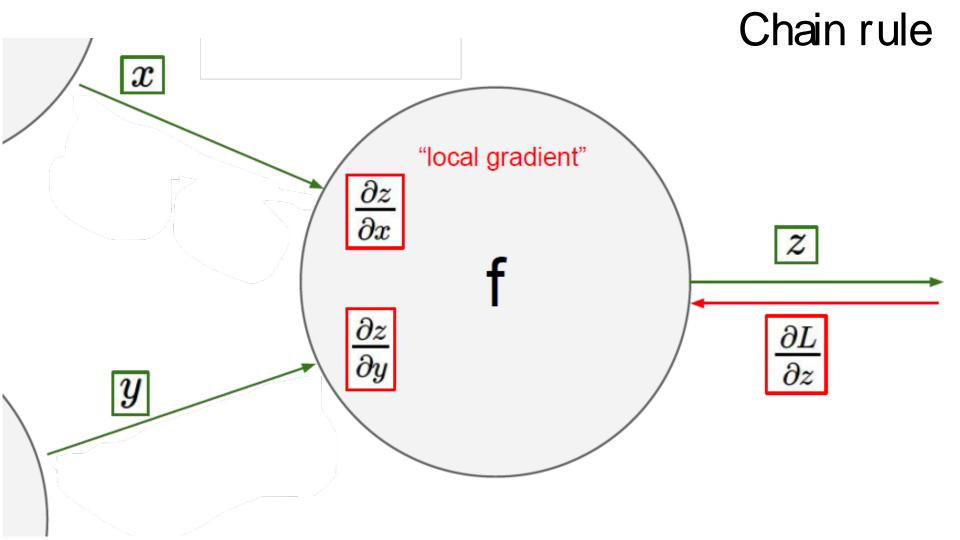
#### Chain Rule

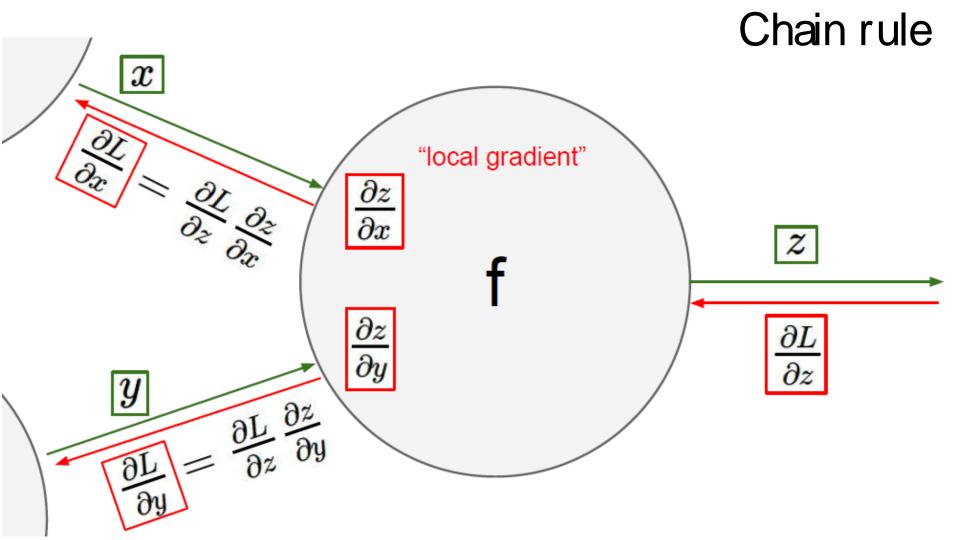


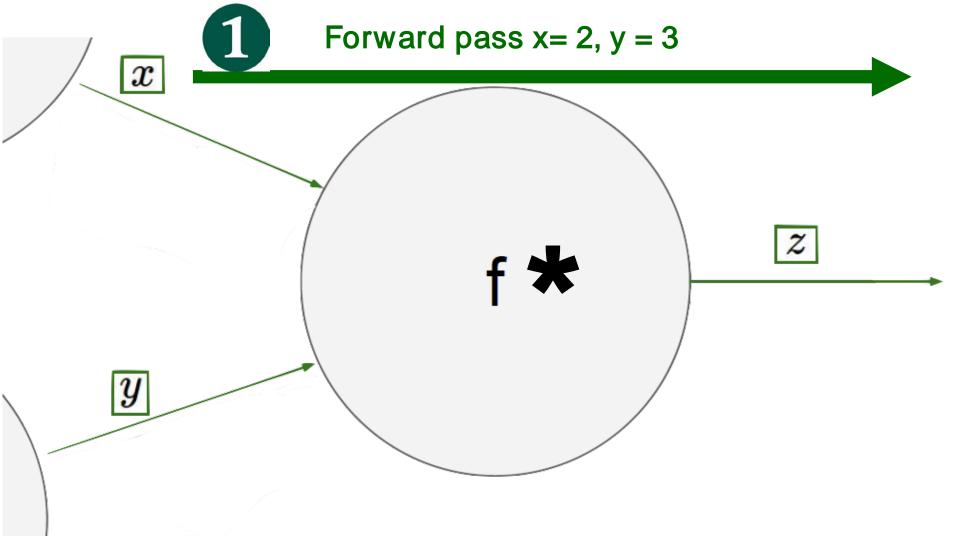
$$y = f(g); g = g(x)$$
  
$$\frac{df}{dx} = \frac{df}{dg} \frac{dg}{dx}$$

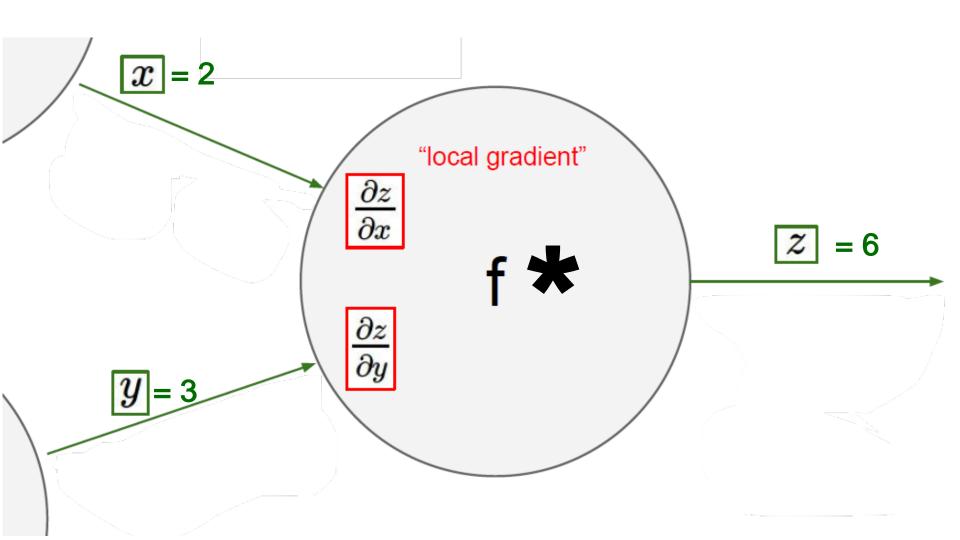


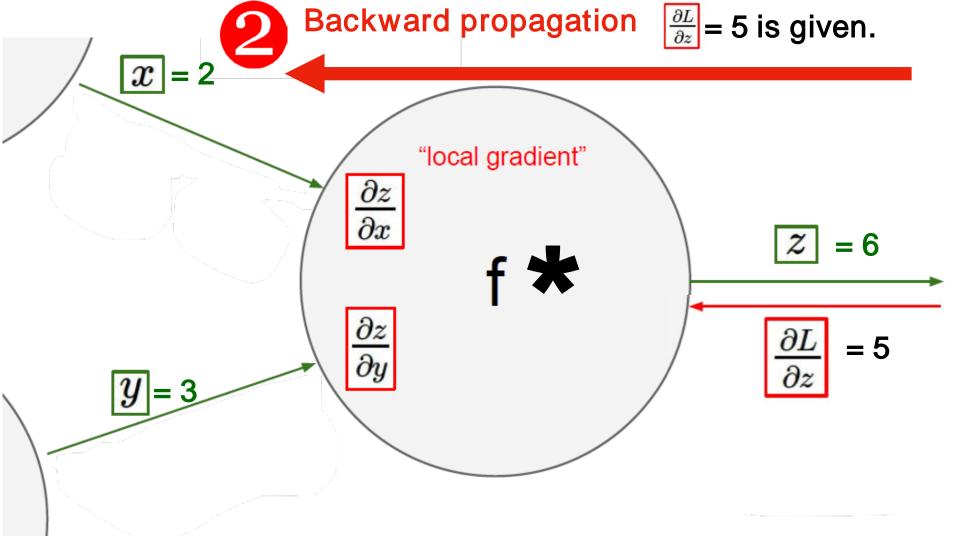


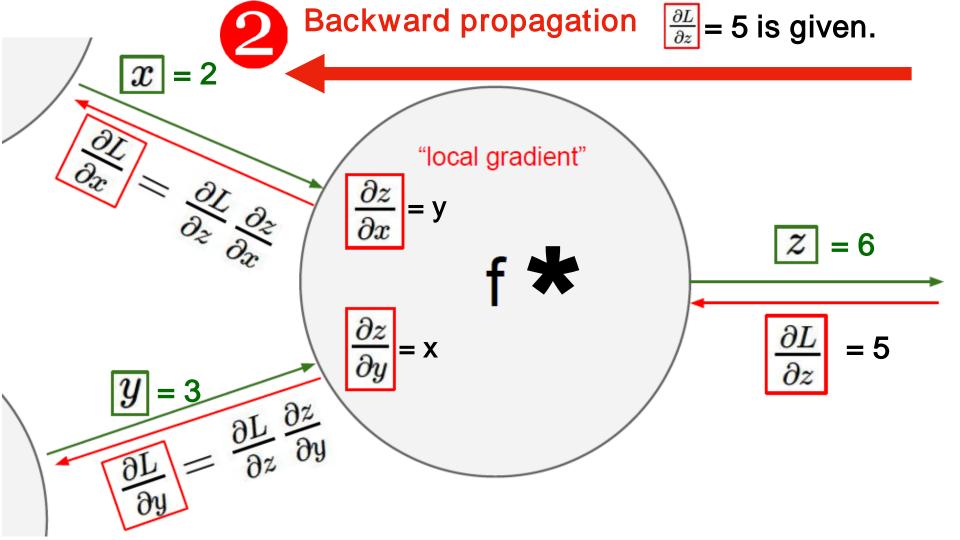


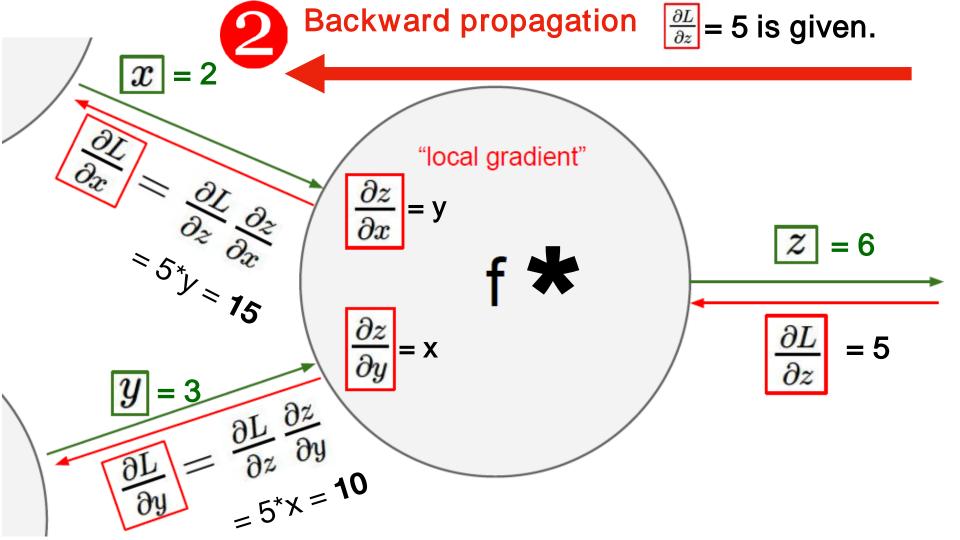






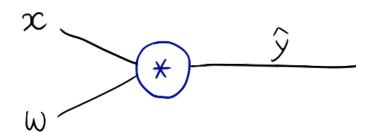






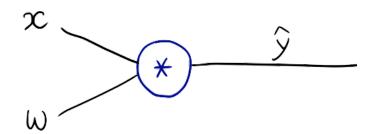
$$\hat{y} = x * w$$

$$\hat{y} = x * w$$



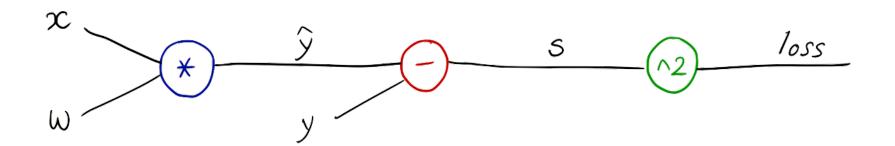
$$\hat{y} = x * w$$

$$loss = (\hat{y} - y)^2 = (x * w - y)^2$$

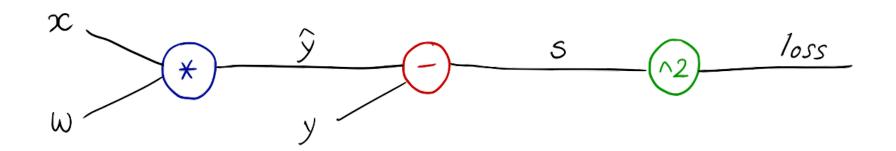


$$\hat{y} = x * w$$

$$loss = (\hat{y} - y)^2 = (x * w - y)^2$$

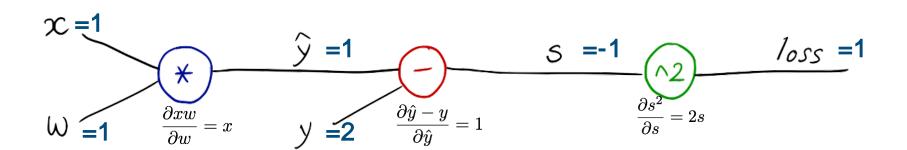


### 1 Forward pass x=1, y=2 where w=1



## 24

#### **Backward propagation**



$$\frac{\partial loss}{\partial w} =$$

### 2\_

#### **Backward propagation**

$$\frac{\partial loss}{\partial w} = \frac{\partial loss}{\partial \hat{y}} \frac{\partial \hat{y}}{\partial w} = -2 * x = -2 * 1 = -2$$
$$\frac{\partial loss}{\partial \hat{y}} = \frac{\partial loss}{\partial s} \frac{\partial s}{\partial \hat{y}} = -2 * 1 = -2$$
$$\frac{\partial loss}{\partial s} = 2s = -2$$

$$\mathcal{X} = 1$$

$$\mathcal{Y} = 1$$

$$\mathcal{Y} = 1$$

$$\mathcal{Y} = 1$$

$$\mathcal{Y} = 2$$

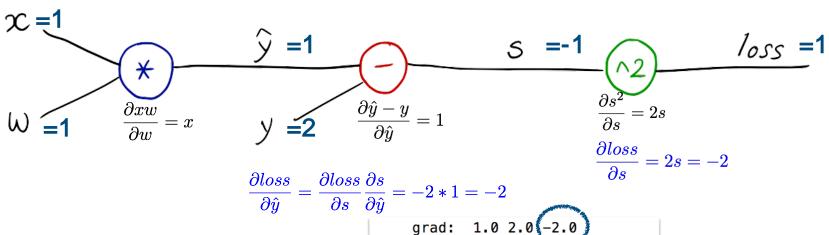
$$\mathcal{Y} = 3$$

$$\mathcal{Y} = 2$$

$$\mathcal{Y} = 3$$

## 24

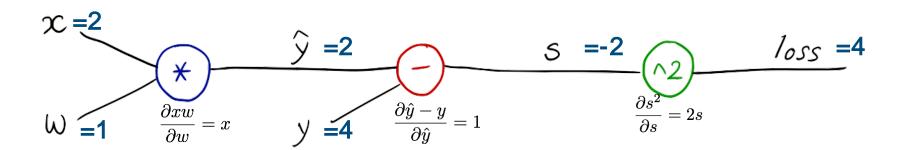
#### **Backward propagation**



 $\frac{\partial loss}{\partial w} = \frac{\partial loss}{\partial \hat{y}} \frac{\partial \hat{y}}{\partial w} = -2 * x = -2 * 1 = -2$ 

grad: 2.0 4.0 -7.84 grad: 3.0 6.0 -16.2288 ogress: 0 4.919240100095999

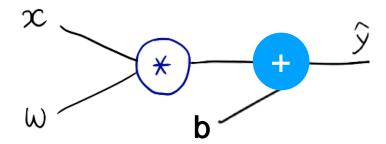
#### Exercise 4-1: x = 2, y=4, w=1



$$\frac{\partial loss}{\partial w} =$$

#### Exercise 4-2: x = 1, y=2, w=1, b=2

$$\hat{\mathbf{y}} = \mathbf{x} * \mathbf{w} + \mathbf{b} \qquad loss = (\hat{y} - y)^2$$



#### Data and Variable



```
import torch
import numpy as np
import matplotlib.pyplot as plt

x_data = [1.0, 2.0, 3.0]
y_data = [2.0, 4.0, 6.0]

w = torch.tensor([1.0], requires_grad=True)
```

#### Model and Loss



```
# our model forward pass
def forward(x):
  return x * w
# loss function
def loss(x, y):
 y_pred = forward(x)
  return (y_pred - y) ** 2
```

#### Training: forward, backward, and update weight

```
# before training
print("predict (before training)", 4, forward(4).item())
for epoch in range(10):
    for x_val, y_val in zip(x_data, y_data):
        y_pred = forward(x_val) # 1) Forward pass
        I = loss(y_pred, y_val) # 2) Compute loss
        I.backward() # 3) Back propagation to update weights
        print("\tgrad: ", x_val, y_val, w.grad.item())
        w.data = w.data - 0.01 * w.grad.item()
        # Manually zero the gradients after updating weights
        w.grad.data.zero_()
   print(f"Epoch: {epoch} | Loss: {l.item()}")
# After training
print("Prediction (after training)", 4, forward(4).item())
```

#### Output

```
for epoch in range(10):
    for x_val, y_val in zip(x_data, y_data):
       y_pred = forward(x_val) # 1) Forward pass
        I = loss(v pred. v val) # 2) Compute loss
        I.backward() # 3) Back propagation to update weights
       print("\tgrad: ", x_val, y_val, w.grad.item())
       w.data = w.data - 0.01 * w.grad.item()
       # Manually zero the gradients after updating weights
       w.grad.data.zero_()
   print(f"Epoch: {epoch} | Loss: {l.item()}")
```

```
grad: 3.0 6.0 -11.998146057128906
progress: 1 3.9987640380859375
    grad: 1.0 2.0 -1.0931644439697266
    grad: 2.0 4.0 -4.285204887390137
    grad: 3.0 6.0 -8.870372772216797
progress: 2 2.1856532096862793
    grad: 1.0 2.0 -0.8081896305084229
    grad: 2.0 4.0 -3.1681032180786133
    grad: 3.0 6.0 -6.557973861694336
progress: 3 1.1946394443511963
    grad: 1.0 2.0 -0.5975041389465332
    grad: 2.0 4.0 -2.3422164916992188
    grad: 3.0 6.0 -4.848389625549316
progress: 4 0.6529689431190491
    grad: 1.0 2.0 -0.4417421817779541
    grad: 2.0 4.0 -1.7316293716430664
    grad: 3.0 6.0 -3.58447265625
progress: 5 0.35690122842788696
    grad: 1.0 2.0 -0.3265852928161621
    grad: 2.0 4.0 -1.2802143096923828
    grad: 3.0 6.0 -2.650045394897461
progress: 6 0.195076122879982
    grad: 1.0 2.0 -0.24144840240478516
    grad: 2.0 4.0 -0.9464778900146484
    grad: 3.0 6.0 -1.9592113494873047
progress: 7 0.10662525147199631
    grad: 1.0 2.0 -0.17850565910339355
    grad: 2.0 4.0 -0.699742317199707
    grad: 3.0 6.0 -1.4484672546386719
```

predict (before training) 4 4.0 grad: 1.0 2.0 -2.0

progress: 0 7.315943717956543

grad: 2.0 4.0 -7.840000152587891 grad: 3.0 6.0 -16.228801727294922

grad: 1.0 2.0 -1.478623867034912 grad: 2.0 4.0 -5.796205520629883

```
predict (before training) 4 4.0
    grad: 1.0 2.0 -2.0
    grad: 2.0 4.0 -7.84
    grad: 3.0 6.0 -16.2288
progress: 0 4.919240100095999
    grad: 1.0 2.0 -1.478624
    grad: 2.0 4.0 -5.796206079999999
    grad: 3.0 6.0 -11.998146585599997
progress: 1 2.688769240265834
    grad: 1.0 2.0 -1.093164466688
    grad: 2.0 4.0 -4.285204709416961
    grad: 3.0 6.0 -8.87037374849311
progress: 2 1.4696334962911515
    grad: 1.0 2.0 -0.8081896081960389
    grad: 2.0 4.0 -3.1681032641284723
    grad: 3.0 6.0 -6.557973756745939
progress: 3 0.8032755585999681
    grad: 1.0 2.0 -0.59750427561463
    grad: 2.0 4.0 -2.3422167604093502
    grad: 3.0 6.0 -4.848388694047353
progress: 4 0.43905614881022015
    grad: 1.0 2.0 -0.44174208101320334
    grad: 2.0 4.0 -1.7316289575717576
    grad: 3.0 6.0 -3.584471942173538
progress: 5 0.2399802903801062
    grad: 1.0 2.0 -0.3265852213980338
    grad: 2.0 4.0 -1.2802140678802925
    grad: 3.0 6.0 -2.650043120512205
progress: 6 0.1311689630744999
    grad: 1.0 2.0 -0.241448373202223
    grad: 2.0 4.0 -0.946477622952715
    grad: 3.0 6.0 -1.9592086795121197
progress: 7 0.07169462478267678
    grad: 1.0 2.0 -0.17850567968888198
    grad: 2.0 4.0 -0.6997422643804168
    grad: 3.0 6.0 -1.4484664872674653
progress: 8 0.03918700813247573
    grad: 1.0 2.0 -0.13197139106214673
    grad: 2.0 4.0 -0.5173278529636143
    grad: 3.0 6.0 -1.0708686556346834
progress: 9 0.021418922423117836
predict (after training) 4 7.804863933862125
```

#### Output

(from numeric gradient computation)

```
# Before training
print("predict (before training)", 4, forward(4))
# Training loop
for epoch in range(10):
    for x, y in zip(x_data, y_data):
        qrad = qradient(x, y)
        w = w - 0.01 * grad
        print("\tgrad: ", x, y, grad)
        l = loss(x, y)
    print ("progress:", epoch, l)
# After training
print("predict (after training)", 4, forward(4))
```

#### Output

(from numeric gradient computation)

#### predict (before training) 4 4.0 grad: 1.0 2.0 -2.0 grad: 2.0 4.0 -7.84 grad: 3.0 6.0 -16.2288 progress: 0 4.919240100095999 grad: 1.0 2.0 -1.478624 grad: 2.0 4.0 -5.796206079999999 grad: 3.0 6.0 -11.998146585599997 progress: 1 2.688769240265834 grad: 1.0 2.0 -1.093164466688 grad: 2.0 4.0 -4.285204709416961 grad: 3.0 6.0 -8.87037374849311 progress: 2 1.4696334962911515 grad: 1.0 2.0 -0.8081896081960389 grad: 2.0 4.0 -3.1681032641284723 grad: 3.0 6.0 -6.557973756745939 progress: 3 0.8032755585999681 grad: 1.0 2.0 -0.59750427561463 grad: 2.0 4.0 -2.3422167604093502 grad: 3.0 6.0 -4.848388694047353 progress: 4 0.43905614881022015 grad: 1.0 2.0 -0.44174208101320334 grad: 2.0 4.0 -1.7316289575717576 grad: 3.0 6.0 -3.584471942173538 progress: 5 0.2399802903801062 grad: 1.0 2.0 -0.3265852213980338 grad: 2.0 4.0 -1.2802140678802925 grad: 3.0 6.0 -2.650043120512205 progress: 6 0.1311689630744999 grad: 1.0 2.0 -0.241448373202223 grad: 2.0 4.0 -0.946477622952715 grad: 3.0 6.0 -1.9592086795121197 progress: 7 0.07169462478267678 grad: 1.0 2.0 -0.17850567968888198

grad: 2.0 4.0 -0.6997422643804168

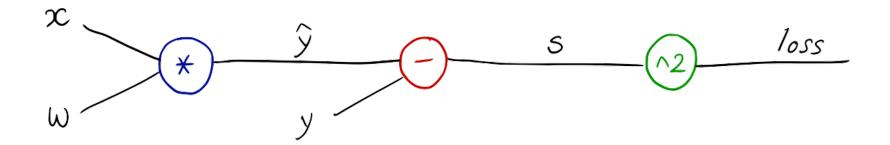
#### Output

(computational graph)

```
predict (before training) 4 4.0
    grad: 1.0 2.0 -2.0
   grad: 2.0 4.0 -7.84
    grad: 3.0 6.0 -16.2288
progress: 0 4.919240100095999
    grad: 1.0 2.0 -1.478624
    grad: 2.0 4.0 -5.796206079999999
    grad: 3.0 6.0 -11.998146585599997
progress: 1 2.688769240265834
    grad: 1.0 2.0 -1.093164466688
    grad: 2.0 4.0 -4.285204709416961
    grad: 3.0 6.0 -8.87037374849311
progress: 2 1.4696334962911515
    grad: 1.0 2.0 -0.8081896081960389
    grad: 2.0 4.0 -3.1681032641284723
    grad: 3.0 6.0 -6.557973756745939
progress: 3 0.8032755585999681
    grad: 1.0 2.0 -0.59750427561463
    grad: 2.0 4.0 -2.3422167604093502
    grad: 3.0 6.0 -4.848388694047353
progress: 4 0.43905614881022015
    grad: 1.0 2.0 -0.44174208101320334
    grad: 2.0 4.0 -1.7316289575717576
    grad: 3.0 6.0 -3.584471942173538
progress: 5 0.2399802903801062
    grad: 1.0 2.0 -0.3265852213980338
   grad: 2.0 4.0 -1.2802140678802925
    grad: 3.0 6.0 -2.650043120512205
progress: 6 0.1311689630744999
    grad: 1.0 2.0 -0.241448373202223
    grad: 2.0 4.0 -0.946477622952715
    grad: 3.0 6.0 -1.9592086795121197
progress: 7 0.07169462478267678
    grad: 1.0 2.0 -0.17850567968888198
    grad: 2.0 4.0 -0.6997422643804168
```



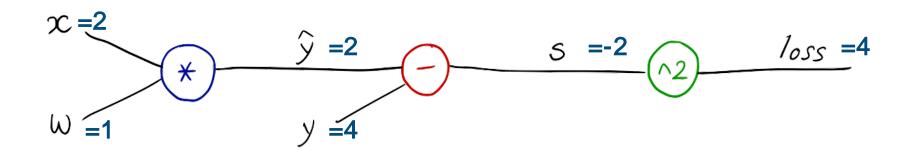
#### PyTorch forward/backward



#### Forward pass

```
# Any random value
w = torch.tensor([1.0], requires_grad=True)
l = loss(x=1, y=2)
                        \hat{y} = 1
                                                                   loss = 1
 \partial loss
```

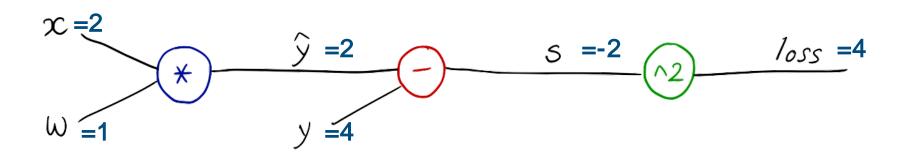
#### Back propagation: I.backward()



$$\frac{\partial loss}{\partial w} = \text{W.grad}$$

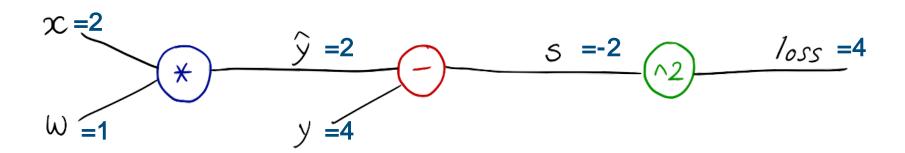
#### Weight update (step)

w.data = w.data - 0.01 \* w.grad.data



$$\frac{\partial loss}{\partial w} = \text{W.grad}$$

# Exercise 4-3: implement computational graph and backprop using NumPy



$$\frac{\partial loss}{\partial w} =$$

# Exercise 4-4: Compute gradients using computational graph (manually)

$$\hat{y} = x^2 w_2 + x w_1 + b$$
$$loss = (\hat{y} - y)^2$$

$$\frac{\partial loss}{\partial w_1} = ?$$

$$\frac{\partial loss}{\partial w_2} = ?$$

## Exercise 4-5: compute gradients using PyTorch

$$\hat{y} = x^2 w_2 + x w_1 + b$$
$$loss = (\hat{y} - y)^2$$

$$\frac{\partial loss}{\partial w_1} = ?$$

$$\frac{\partial loss}{\partial w_2} = ?$$



Lecture 5: Linear regression in the PyTorch way