No magnetic monopole has ever been observed in nature. Classical electrodynamics, however, does not provide the reason their nonexistance. Since Maxwell equations merely formalize the experimental observations on electric and magnetic phenomena, no a priori rejection of the monopole is made. Despite the lack of concrete experimental results, the interest in a consistent theory of magnetic monopoles has not vanished throughout the past century, since Dirac first published his original paper in 1931.

Our first step in introducing a theory of the magnetic monopole will be a naive construction of an elementary classical model, aimed to write the equations of motion of an electron in a Coulomb-like magnetic field. This is only meant to stress the main problems of the subject. We begin assuming the existence of a magnetic charge, analogous to the electric charge, and consequently modify Maxwell equations, including the non-zero divergence of the magnetic field $\bf B$, that has to be equal to the local magnetic charge density, namely ρ_q .

Here arises the first contraddiction. If we define the electromagnetic potential **A**, **B** being the curl of **A**, it is impossible to have both $\mathbf{B} = \nabla \times \mathbf{A}$ and $\nabla \cdot \mathbf{B} = 4\pi \rho_g$ at the same time. The reason is that **A** is not defined everywhere in space, but will always have a string of singularities.

A non contraddictory monopole theory is incompatible with a global vector potential. We are forced to dercribe our model using only local potentials, that are required to agree on their overlap region via an appropriate transformation.

The frame that fits the most to this picture is that of gauge theories.

Since classical electrodynamics is a U(1) gauge theory, we define local potentials on two open sets, requiring that a U(1) gauge trasformation connects them in the overlapping region. This way it is possibile to define the correct monopole field and to remove the previous contraddiction. Also we give a topological meaning to the magnetic charge, via the characteristic Chern classes of the manifold of the theory. A relationship between magnetic and electric charge is obtained requiring the trasformation of the fields to be single valued.

One of the main problems of this Abelian model is to be found when we try to extend our theory to a quantum field theory.

The next step is to generalize our theory to a non-Abelian gauge group, having U(1) as a subgroup, and that will restrict to our previous abelian theory under normal conditions. This spontaneous symmetry breaking process preserves all the earlier predictions, gives a solution to the problems of the previous model.

Theories of this kind are named Yang-Mills theories.

The first and simplest case is considering SU(2) as the gauge group. We will analyze two models of this type.

The first model, proposed by Wu and Yang in 1969, is capable of solving all of the abelian model problems, but gives badly-defined configuration energies, leading to divergencies.

The second one is a special case of the more general model proposed by Georgi and Glashow in 1974. The gauge potential is coupled with another complex field, the Higgs field. This immediatly breaks the symmetry of SU(2) down to U(1), and solves the infinite energies problem. The last achievement is a definition of the magnetic charge that is directly derived from the conservation of the field strength tensor, so from Maxwell equations themselves.

Unfortunately, the model has no analytic solution in general: numerical solutions to the problem are to be found. We conclude our dissertation briefly mentioning an ansatz proposed by 't Hooft and Polyakov, a starting point for numerical solutions of the Georgi-Glashow model.