

Lecture 7: Policy Gradient

David Silver

Outline

- 1 Introduction
- 2 Finite Difference Policy Gradient
- 3 Monte-Carlo Policy Gradient
- 4 Actor-Critic Policy Gradient

Policy-Based Reinforcement Learning

- In the last lecture we approximated the value or action-value function using parameters θ ,

$$V_{\theta}(s) \approx V^{\pi}(s)$$

$$Q_{\theta}(s, a) \approx Q^{\pi}(s, a)$$

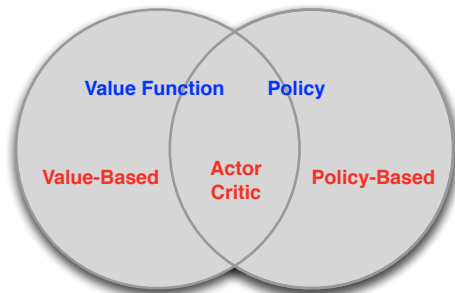
- A policy was generated directly from the value function
 - e.g. using ϵ -greedy
- In this lecture we will directly parametrise the **policy**

$$\pi_{\theta}(s, a) = \mathbb{P}[a \mid s, \theta]$$

- We will focus again on **model-free** reinforcement learning

Value-Based and Policy-Based RL

- Value Based
 - Learnt Value Function
 - Implicit policy (e.g. ϵ -greedy)
- Policy Based
 - No Value Function
 - Learnt Policy
- Actor-Critic
 - Learnt Value Function
 - Learnt Policy



Advantages of Policy-Based RL

Advantages:

- Better convergence properties
- Effective in high-dimensional or continuous action spaces
- Can learn stochastic policies

Disadvantages:

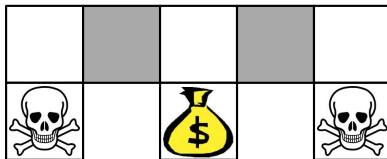
- Typically converge to a local rather than global optimum
- Evaluating a policy is typically inefficient and high variance

Example: Rock-Paper-Scissors



- Two-player game of rock-paper-scissors
 - Scissors beats paper
 - Rock beats scissors
 - Paper beats rock
- Consider policies for *iterated* rock-paper-scissors
 - A deterministic policy is easily exploited
 - A uniform random policy is optimal (i.e. Nash equilibrium)

Example: Aliased Gridworld (1)



- The agent cannot differentiate the grey states
- Consider features of the following form (for all N, E, S, W)

$$\phi(s, a) = \mathbf{1}(\text{wall to } N, a = \text{move } E)$$

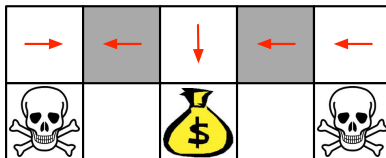
- Compare value-based RL, using an approximate value function

$$Q_{\theta}(s, a) = f(\phi(s, a), \theta)$$

- To policy-based RL, using a parametrised policy

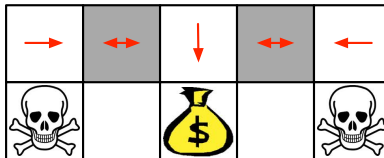
$$\pi_{\theta}(s, a) = g(\phi(s, a), \theta)$$

Example: Aliased Gridworld (2)



- Under aliasing, an optimal **deterministic** policy will either
 - move W in both grey states (shown by red arrows)
 - move E in both grey states
- Either way, it can get stuck and *never* reach the money
- Value-based RL learns a near-deterministic policy
 - e.g. greedy or ϵ -greedy
- So it will traverse the corridor for a long time

Example: Aliased Gridworld (3)



- An optimal **stochastic** policy will randomly move E or W in grey states

$$\pi_{\theta}(\text{wall to N and S, move E}) = 0.5$$

$$\pi_{\theta}(\text{wall to N and S, move W}) = 0.5$$

- It will reach the goal state in a few steps with high probability
- Policy-based RL can learn the optimal stochastic policy

Policy Objective Functions

목적 함수 J

θ 가 policy를 결정함.

- Goal: given policy $\pi_\theta(s, a)$ with parameters θ , find best θ
- But how do we measure the quality of a policy π_θ ?

- ① ■ In episodic environments we can use the start value

$$J_1(\theta) = V^{\pi_\theta}(s_1) = \mathbb{E}_{\pi_\theta}[v_1]$$

- ② ■ In continuing environments we can use the average value

$$J_{avV}(\theta) = \sum_s d^{\pi_\theta}(s) V^{\pi_\theta}(s)$$

stationary distribution - 각 state별로 얻은 복귀에 대한 평균값.

- ③ ■ Or the average reward per time-step

$$J_{avR}(\theta) = \sum_s d^{\pi_\theta}(s) \sum_a \pi_\theta(s, a) \mathcal{R}_s^a$$

- where $d^{\pi_\theta}(s)$ is stationary distribution of Markov chain for π_θ

Policy Optimisation

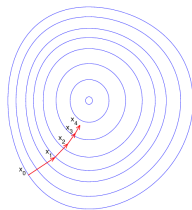
- Policy based reinforcement learning is an **optimisation** problem
- Find θ that maximises $J(\theta)$
- Some approaches do not use gradient
 - Hill climbing
 - Simplex / amoeba / Nelder Mead
 - Genetic algorithms
- Greater efficiency often possible using gradient
 - Gradient descent - silver 장외는 이걸 쓴다.
 - Conjugate gradient
 - Quasi-newton - newton method.
- We focus on gradient descent, many extensions possible
- And on methods that exploit sequential structure

Policy Gradient

↳ π 가 아냐, J 에 대한 gradient를 update할 때, loss - error를 minimize.

- Let $J(\theta)$ be any policy objective function
- Policy gradient algorithms search for a local maximum in $J(\theta)$ by ascending the gradient of the policy, w.r.t. parameters θ

maximize
|
gradient
ascent

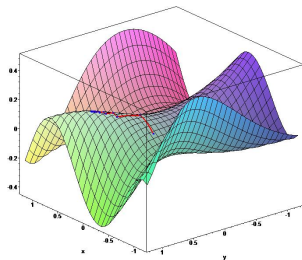


$$\Delta\theta = \alpha \nabla_{\theta} J(\theta)$$

- Where $\nabla_{\theta} J(\theta)$ is the policy gradient

$$\nabla_{\theta} J(\theta) = \begin{pmatrix} \frac{\partial J(\theta)}{\partial \theta_1} \\ \vdots \\ \frac{\partial J(\theta)}{\partial \theta_n} \end{pmatrix}$$

- and α is a step-size parameter



Computing Gradients By Finite Differences

- To evaluate policy gradient of $\pi_{\theta}(s, a)$
- For each dimension $k \in [1, n]$
 - Estimate k th partial derivative of objective function w.r.t. θ
 - By perturbing θ by small amount ϵ in k th dimension

$\theta_1, \dots, \theta_n$ dimensions

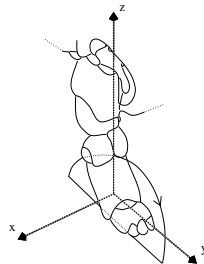
$$\left(\frac{\partial J(\theta)}{\partial \theta_1}, \dots, \frac{\partial J(\theta)}{\partial \theta_n} \right) = \nabla J(\theta)$$

$$\frac{\partial J(\theta)}{\partial \theta_k} \approx \frac{J(\theta + \epsilon u_k) - J(\theta)}{\epsilon}$$

where u_k is unit vector with 1 in k th component, 0 elsewhere

- Uses n evaluations to compute policy gradient in n dimensions
- Simple, noisy, inefficient but sometimes effective
- Works for arbitrary policies, even if policy is not differentiable

Training AIBO to Walk by Finite Difference Policy Gradient



- Goal: learn a fast AIBO walk (useful for Robocup)
- AIBO walk policy is controlled by 12 numbers (elliptical loci)
- Adapt these parameters by finite difference policy gradient
- Evaluate performance of policy by field traversal time

AIBO Walk Policies

- Before training
- During training
- After training

Score Function

- We now compute the policy gradient *analytically*
- Assume policy π_θ is differentiable whenever it is non-zero
- and we know the gradient $\nabla_\theta \pi_\theta(s, a)$
- **Likelihood ratios** exploit the following identity

$$\begin{aligned}\nabla_\theta \pi_\theta(s, a) &= \pi_\theta(s, a) \frac{\nabla_\theta \pi_\theta(s, a)}{\pi_\theta(s, a)} \\ &= \pi_\theta(s, a) \nabla_\theta \log \pi_\theta(s, a)\end{aligned}$$

$$\frac{dx}{x} = d(\log x)$$

$$\left[\begin{aligned} \frac{d}{dx} \log x &= \frac{1}{x} \\ d \log x &= \frac{dx}{x} \end{aligned} \right]$$

- The **score function** is $\nabla_\theta \log \pi_\theta(s, a)$

Likelihood ratio $\in \mathbb{R}$.

$\nabla \pi$ 를 $\pi \nabla \log \pi$ 로 바꾸기
편하기 하기 위해

Softmax Policy

- We will use a softmax policy as a running example
- Weight actions using linear combination of features $\phi(s, a)^\top \theta$
- Probability of action is proportional to exponentiated weight

$$\pi_\theta(s, a) \propto e^{\phi(s, a)^\top \theta}$$

- The score function is

$$\nabla_\theta \log \pi_\theta(s, a) = \phi(s, a) - \mathbb{E}_{\pi_\theta} [\phi(s, \cdot)]$$

Gaussian Policy

- In continuous action spaces, a Gaussian policy is natural
- Mean is a linear combination of state features $\mu(s) = \phi(s)^\top \theta$
- Variance may be fixed σ^2 , or can also be parametrised
- Policy is Gaussian, $a \sim \mathcal{N}(\mu(s), \sigma^2)$
- The score function is

$$\nabla_{\theta} \log \pi_{\theta}(s, a) = \frac{(a - \mu(s))\phi(s)}{\sigma^2}$$

One-Step MDPs

- Consider a simple class of **one-step** MDPs

- Starting in state $s \sim d(s)$
- Terminating after one time-step with reward $r = \mathcal{R}_{s,a}$

- Use likelihood ratios to compute the policy gradient

어떤 policy 분포 $d(s)$ 를 따라 state에서, policy에 의해 나타낸
한 step 이후의 reward π
를 나타냄.

목적 함수 ③번. - $J(\theta) = \mathbb{E}_{\pi_\theta} [r]$

$$= \sum_{s \in \mathcal{S}} d(s) \sum_{a \in \mathcal{A}} \pi_\theta(s, a) \mathcal{R}_{s,a}$$

$$\nabla_\theta J(\theta) = \sum_{s \in \mathcal{S}} d(s) \sum_{a \in \mathcal{A}} \pi_\theta(s, a) \nabla_\theta \log \pi_\theta(s, a) \mathcal{R}_{s,a}$$

$$= \mathbb{E}_{\pi_\theta} [\nabla_\theta \log \pi_\theta(s, a) r]$$

likelihood ratio trick 사용하며

$\pi_\theta(s, a)$ 를
도미노 법칙 $\rightarrow \mathbb{E}_{\pi_\theta}$ 기댓값으로
표현 가능

한 step 이후의 policy에 의해 나타낸 sample reward

Policy Gradient Theorem

- The policy gradient theorem generalises the likelihood ratio approach to multi-step MDPs
 - Replaces instantaneous reward r with long-term value $Q^\pi(s, a)$
 - Policy gradient theorem applies to start state objective, average reward and average value objective
- Handwritten notes:*
 - Under "generalises": r 은 Q 로 대체하면 된다. (증명됨)
 - Under "likelihood ratio approach to multi-step MDPs": 앞의 목적함수 3개 모두 해당.

Theorem

For any differentiable policy $\pi_\theta(s, a)$,
 for any of the policy objective functions $J = J_1, J_{avR}$, or $\frac{1}{1-\gamma} J_{avV}$,
 the policy gradient is

$$\nabla_\theta J(\theta) = \mathbb{E}_{\pi_\theta} [\nabla_\theta (\log \pi_\theta(s, a)) \cdot Q^{\pi_\theta}(s, a)]$$

Handwritten note: score function $\times Q$

or reinforce algorithm - 몬카로에서 쓰임

Monte-Carlo Policy Gradient (REINFORCE)

- Update parameters by stochastic gradient ascent
- Using policy gradient theorem
- Using return v_t as an unbiased sample of $Q^{\pi_\theta}(s_t, a_t)$

$$\Delta\theta_t = \alpha \nabla_\theta \log \pi_\theta(s_t, a_t) v_t$$

Q는 true value of all, 23477 return(Q의 unbiased sample of)을 쓴다.

function REINFORCE

Initialise θ arbitrarily

for each episode $\{s_1, a_1, r_2, \dots, s_{T-1}, a_{T-1}, r_T\} \sim \pi_\theta$ **do**

for $t = 1$ to $T - 1$ **do**

$\theta \leftarrow \theta + \alpha \nabla_\theta \log \pi_\theta(s_t, a_t) v_t$

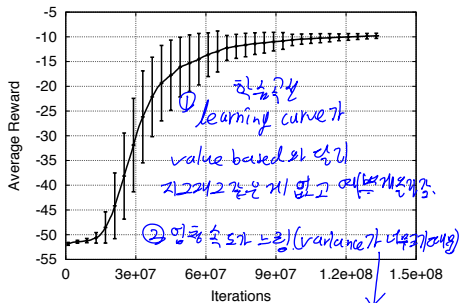
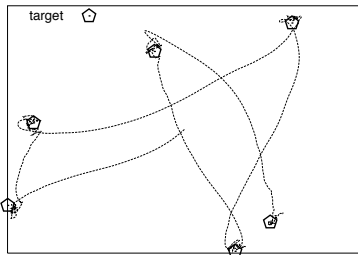
end for

end for

return θ

end function

Puck World Example



variance를 어떻게

줄이려? actor-critic 방법론 등

- Continuous actions exert small force on puck
- Puck is rewarded for getting close to target
- Target location is reset every 30 seconds
- Policy is trained using variant of Monte-Carlo policy gradient

Reducing Variance Using a Critic

- Monte-Carlo policy gradient still has high variance
- We use a **critic** to estimate the action-value function,

$$\underbrace{Q_w(s, a)}_{\text{approximated } Q} \approx \underbrace{Q^{\pi_\theta}(s, a)}_{\text{true } Q \text{ value}}$$

- Actor-critic algorithms maintain two sets of parameters

Critic Updates action-value function parameters (w)

Actor Updates policy parameters (θ), in direction suggested by critic

- Actor-critic algorithms follow an *approximate* policy gradient

$$\nabla_{\theta} J(\theta) \approx \mathbb{E}_{\pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(s, a) Q_w(s, a)]$$

$$\Delta \theta = \alpha \nabla_{\theta} \log \pi_{\theta}(s, a) Q_w(s, a)$$

Estimating the Action-Value Function

- The critic is solving a familiar problem: policy evaluation
- How good is policy π_θ for current parameters θ ?
- This problem was explored in previous two lectures, e.g.
 - Monte-Carlo policy evaluation
 - Temporal-Difference learning
 - TD(λ)
- Could also use e.g. least-squares policy evaluation

Action-Value Actor-Critic

- Simple actor-critic algorithm based on action-value critic
- Using linear value fn approx. $Q_w(s, a) = \phi(s, a)^\top w$
 - Critic** Updates w by linear TD(0)
 - Actor** Updates θ by policy gradient

function QAC *Q-actor-critic*

 Initialise s, θ

 Sample $a \sim \pi_\theta$

for each step **do**

 Sample reward $r = \mathcal{R}_s^a$; sample transition $s' \sim \mathcal{P}_{s'}^a$.

 Sample action $a' \sim \pi_\theta(s', a')$

TD error $\delta = r + \gamma Q_w(s', a') - Q_w(s, a)$

$\theta = \theta + \alpha \nabla_\theta \log \pi_\theta(s, a) Q_w(s, a)$

$w \leftarrow w + \beta \delta \phi(s, a)$

$a \leftarrow a', s \leftarrow s'$

end for

end function

Bias in Actor-Critic Algorithms

- Approximating the policy gradient introduces bias
- A biased policy gradient may not find the right solution
 - e.g. if $Q_w(s, a)$ uses aliased features, can we solve gridworld example?
- Luckily, if we choose value function approximation carefully
- Then we can avoid introducing any bias
- i.e. We can still follow the *exact* policy gradient

Compatible Function Approximation

Theorem (Compatible Function Approximation Theorem)

If the following two conditions are satisfied:

- 1 Value function approximator is *compatible* to the policy

$$\nabla_w Q_w(s, a) = \nabla_\theta \log \pi_\theta(s, a)$$

- 2 Value function parameters w minimise the mean-squared error

$$\varepsilon = \mathbb{E}_{\pi_\theta} [(Q^{\pi_\theta}(s, a) - Q_w(s, a))^2]$$

Then the policy gradient is exact,

$$\nabla_\theta J(\theta) = \mathbb{E}_{\pi_\theta} [\nabla_\theta \log \pi_\theta(s, a) Q_w(s, a)]$$

Proof of Compatible Function Approximation Theorem

If w is chosen to minimise mean-squared error, gradient of ε w.r.t. w must be zero,

$$\nabla_w \varepsilon = 0$$

$$\mathbb{E}_{\pi_\theta} [(Q^\theta(s, a) - Q_w(s, a)) \nabla_w Q_w(s, a)] = 0$$

$$\mathbb{E}_{\pi_\theta} [(Q^\theta(s, a) - Q_w(s, a)) \nabla_\theta \log \pi_\theta(s, a)] = 0$$

$$\mathbb{E}_{\pi_\theta} [Q^\theta(s, a) \nabla_\theta \log \pi_\theta(s, a)] = \mathbb{E}_{\pi_\theta} [Q_w(s, a) \nabla_\theta \log \pi_\theta(s, a)]$$

So $Q_w(s, a)$ can be substituted directly into the policy gradient,

$$\nabla_\theta J(\theta) = \mathbb{E}_{\pi_\theta} [\nabla_\theta \log \pi_\theta(s, a) Q_w(s, a)]$$

Reducing Variance Using a Baseline

- We subtract a baseline function $B(s)$ from the policy gradient
- This can reduce variance, without changing expectation

state s 에 대한 일정한 함수로 강조. (일정한 함수)

$$\begin{aligned} \mathbb{E}_{\pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(s, a) B(s)] &= \sum_{s \in \mathcal{S}} d^{\pi_{\theta}}(s) \sum_a \nabla_{\theta} \pi_{\theta}(s, a) B(s) \\ &\stackrel{\text{likelihood ratio trick을 역산함} \rightarrow}{=} \sum_{s \in \mathcal{S}} d^{\pi_{\theta}} B(s) \nabla_{\theta} \sum_{a \in \mathcal{A}} \pi_{\theta}(s, a) \\ &= 0 \end{aligned}$$

확률의 합이 1이라 1. $\nabla_{\theta} 1 = 0$

- A good baseline is the state value function $B(s) = V^{\pi_{\theta}}(s)$ *이렇게 대입*
- So we can rewrite the policy gradient using the **advantage function** $A^{\pi_{\theta}}(s, a)$ *(variance를 줄일 수 있음.)*

advantage function

$$A^{\pi_{\theta}}(s, a) = Q^{\pi_{\theta}}(s, a) - V^{\pi_{\theta}}(s)$$

$$\nabla_{\theta} J(\theta) = \mathbb{E}_{\pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(s, a) A^{\pi_{\theta}}(s, a)]$$

Estimating the Advantage Function (1)

→ $Q - V$. 이제 V 도 없으니 parameter 2개 세게 필요...

- The advantage function can significantly reduce variance of policy gradient
- So the critic should really estimate the advantage function
- For example, by estimating *both* $V^{\pi_{\theta}}(s)$ and $Q^{\pi_{\theta}}(s, a)$
- Using two function approximators and two parameter vectors,

$$\begin{aligned} V_v(s) &\approx V^{\pi_{\theta}}(s) \\ Q_w(s, a) &\approx Q^{\pi_{\theta}}(s, a) \\ A(s, a) &= Q_w(s, a) - V_v(s) \end{aligned}$$

→ parameter를 2개짜!

→ Q 없이 V 에 대한

parameter만으로

advantage를 계산할 수

있게 함

(다음 페이지)

- And updating *both* value functions by e.g. TD learning

Estimating the Advantage Function (2)

- For the true value function $V^{\pi_{\theta}}(s)$, the TD error $\delta^{\pi_{\theta}}$ *advantage of sample*

$$\delta^{\pi_{\theta}} = r + \gamma V^{\pi_{\theta}}(s') - V^{\pi_{\theta}}(s)$$
state

- is an unbiased estimate of the advantage function

$$\begin{aligned} \mathbb{E}_{\pi_{\theta}} [\delta^{\pi_{\theta}} | s, a] &= \mathbb{E}_{\pi_{\theta}} [r + \gamma V^{\pi_{\theta}}(s') | s, a] - V^{\pi_{\theta}}(s) \\ &= Q^{\pi_{\theta}}(s, a) - V^{\pi_{\theta}}(s) \\ &= A^{\pi_{\theta}}(s, a) \end{aligned}$$

- So we can use the TD error to compute the policy gradient

$$\nabla_{\theta} J(\theta) = \mathbb{E}_{\pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(s, a) \delta^{\pi_{\theta}}]$$

- In practice we can use an approximate TD error

$$\delta_v = r + \gamma V_v(s') - V_v(s)$$

- This approach only requires one set of critic parameters v

Critics at Different Time-Scales

- Critic can estimate value function $V_\theta(s)$ from many targets at different time-scales From last lecture...

- For MC, the target is the return v_t

$$\Delta\theta = \alpha(v_t - V_\theta(s))\phi(s)$$

- For TD(0), the target is the TD target $r + \gamma V(s')$

$$\Delta\theta = \alpha(r + \gamma V(s') - V_\theta(s))\phi(s)$$

- For forward-view TD(λ), the target is the λ -return v_t^λ

$$\Delta\theta = \alpha(v_t^\lambda - V_\theta(s))\phi(s)$$

- For backward-view TD(λ), we use eligibility traces

$$\delta_t = r_{t+1} + \gamma V(s_{t+1}) - V(s_t)$$

$$e_t = \gamma\lambda e_{t-1} + \phi(s_t)$$

$$\Delta\theta = \alpha\delta_t e_t$$

Actors at Different Time-Scales

- The policy gradient can also be estimated at many time-scales

$$\nabla_{\theta} J(\theta) = \mathbb{E}_{\pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(s, a) A^{\pi_{\theta}}(s, a)]$$

- Monte-Carlo policy gradient uses error from complete return

$$\Delta\theta = \alpha(v_t - V_v(s_t)) \nabla_{\theta} \log \pi_{\theta}(s_t, a_t)$$

- Actor-critic policy gradient uses the one-step TD error

$$\Delta\theta = \alpha(r + \gamma V_v(s_{t+1}) - V_v(s_t)) \nabla_{\theta} \log \pi_{\theta}(s_t, a_t)$$

Policy Gradient with Eligibility Traces

- Just like forward-view $TD(\lambda)$, we can mix over time-scales

$$\Delta\theta = \alpha(v_t^\lambda - V_v(s_t))\nabla_\theta \log \pi_\theta(s_t, a_t)$$

- where $v_t^\lambda - V_v(s_t)$ is a biased estimate of advantage fn
- Like backward-view $TD(\lambda)$, we can also use eligibility traces
 - By equivalence with $TD(\lambda)$, substituting $\phi(s) = \nabla_\theta \log \pi_\theta(s, a)$

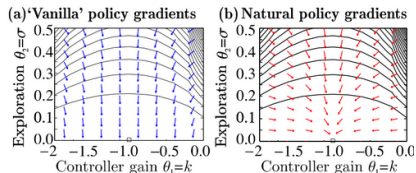
$$\begin{aligned}\delta &= r_{t+1} + \gamma V_v(s_{t+1}) - V_v(s_t) \\ e_{t+1} &= \lambda e_t + \nabla_\theta \log \pi_\theta(s, a) \\ \Delta\theta &= \alpha \delta e_t\end{aligned}$$

- This update can be applied online, to incomplete sequences

Alternative Policy Gradient Directions

- Gradient ascent algorithms can follow *any* ascent direction
- A good ascent direction can significantly speed convergence
- Also, a policy can often be reparametrised without changing action probabilities
- For example, increasing score of all actions in a softmax policy
- The vanilla gradient is sensitive to these reparametrisations

Natural Policy Gradient



- The **natural policy gradient** is parametrisation independent
- It finds ascent direction that is closest to vanilla gradient, when changing policy by a small, fixed amount

$$\nabla_{\theta}^{nat} \pi_{\theta}(s, a) = G_{\theta}^{-1} \nabla_{\theta} \pi_{\theta}(s, a)$$

- where G_{θ} is the Fisher information matrix

$$G_{\theta} = \mathbb{E}_{\pi_{\theta}} \left[\nabla_{\theta} \log \pi_{\theta}(s, a) \nabla_{\theta} \log \pi_{\theta}(s, a)^T \right]$$

Natural Actor-Critic

- Using compatible function approximation,

$$\nabla_w A_w(s, a) = \nabla_\theta \log \pi_\theta(s, a)$$

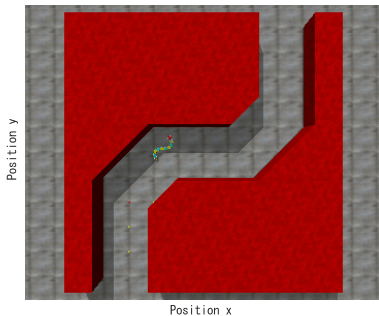
- So the natural policy gradient simplifies,

$$\begin{aligned}\nabla_\theta J(\theta) &= \mathbb{E}_{\pi_\theta} [\nabla_\theta \log \pi_\theta(s, a) A^{\pi_\theta}(s, a)] \\ &= \mathbb{E}_{\pi_\theta} \left[\nabla_\theta \log \pi_\theta(s, a) \nabla_\theta \log \pi_\theta(s, a)^T w \right] \\ &= G_\theta w\end{aligned}$$

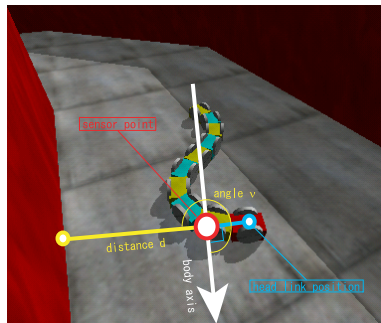
$$\nabla_\theta^{\text{nat}} J(\theta) = w$$

- i.e. update actor parameters in direction of critic parameters

Natural Actor Critic in Snake Domain

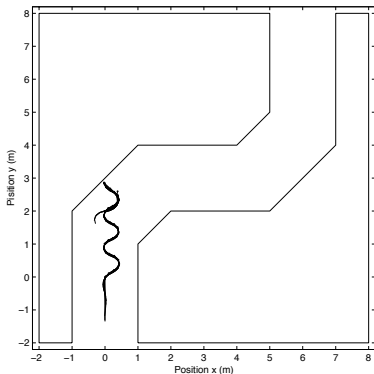


(a) Crank course

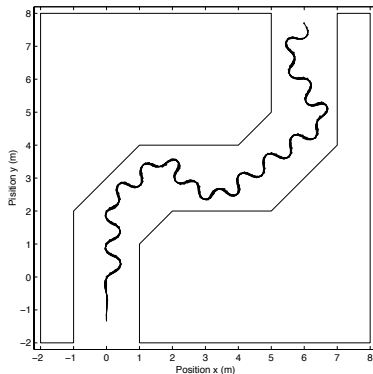


(b) Sensor setting

Natural Actor Critic in Snake Domain (2)

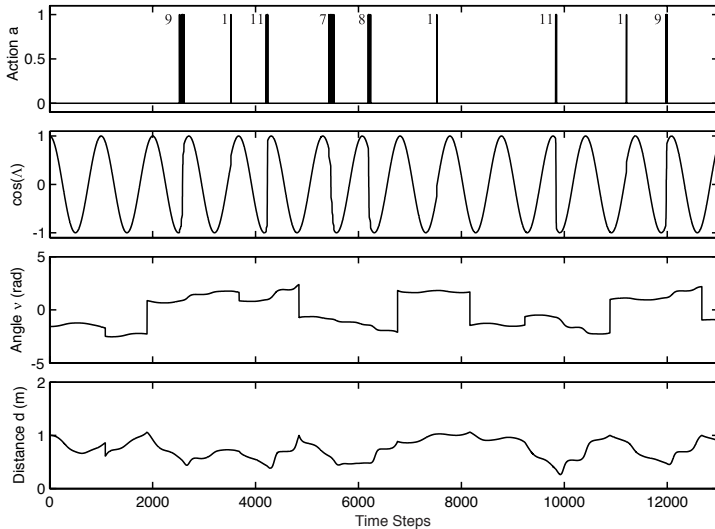


(a) Before learning



(b) After learning

Natural Actor Critic in Snake Domain (3)



Summary of Policy Gradient Algorithms

- The **policy gradient** has many equivalent forms

$\nabla_{\theta} J(\theta) = \mathbb{E}_{\pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(s, a) \underbrace{v_t}_{\text{return.}}]$	<i>(only actor)</i> <u>REINFORCE</u>
$= \mathbb{E}_{\pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(s, a) Q^w(s, a)]$	Q Actor-Critic
$= \mathbb{E}_{\pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(s, a) A^w(s, a)]$	Advantage Actor-Critic
$= \mathbb{E}_{\pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(s, a) \delta]$	TD Actor-Critic
$= \mathbb{E}_{\pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(s, a) \delta e]$	TD(λ) Actor-Critic
$G_{\theta}^{-1} \nabla_{\theta} J(\theta) = w$	Natural Actor-Critic

- Each leads a stochastic gradient ascent algorithm
- Critic uses **policy evaluation** (e.g. MC or TD learning) to estimate $Q^{\pi}(s, a)$, $A^{\pi}(s, a)$ or $V^{\pi}(s)$