

Overview

Recall that the logistic regression algorithm builds upon the intuition from linear regression. In logistic regression, you start by taking the input data, x, and multiplying it by a vector of weights for each of the individual features, which produces an output, y. Afterward, you'll work on using an iterative approach via gradient descent to tune these weights.

Linear regression setup

Write a simple function $predict_y()$ that takes in a matrix x of observations and a vector of feature weights w and outputs a vector of predictions for the various observations.

Recall that this is the sum of the product of each of the feature observations and their corresponding feature weights:

 $\alpha_i = X_{i1} \cdot x_{i2} \cdot x_{i3} \cdot x_{i3} \cdot x_{in} \cdot x_{i$

Hint: Think about which mathematical operation you've seen previously that will take a matrix (x) and multiply it by a vector of weights (w). Use NumPy!

```
import numpy as np

def predict_y(X, w):
    return np.dot(X,w)
```

The sigmoid function

Recall that the sigmoid function is used to map the linear regression model output to a range of 0 to 1, satisfying basic premises of probability. As a reminder, the sigmoid function is defined by:

$$S(x) = \frac{1}{1 + e^{\left(-x\right)}}$$

Write this as a Python function where x is the input and the function outputs the result of the sigmoid function.

Hint: Use NumPy!

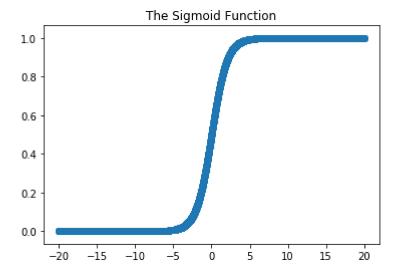
```
# Your code here
def sigmoid(x):
    x = np.array(x)
    return 1/(1 + np.e**(-1*x))
```

Plot the sigmoid

For good measure, let's do a brief investigation of your new function. Plot the output of your sigmoid() function using 10,000 values evenly spaced from -20 to 20.

```
import matplotlib.pyplot as plt
%matplotlib inline

# Plot sigmoid
x = np.linspace(start=-20, stop=20, num=10**4)
y = [sigmoid(xi) for xi in x]
plt.scatter(x, y)
plt.title('The Sigmoid Function')
plt.show()
```



Gradient descent with the sigmoid function

Recall that gradient descent is a numerical method for finding a minimum to a cost function. In the case of logistic regression, you are looking to minimize the error between the model's predictions and the actual data labels. To do this, you first calculate an error vector based on the current model's feature weights. You then multiply the transpose of the training matrix itself by this error vector in order to obtain the gradient. Finally, you take the gradient, multiply it by the step size and add this to our current weight vector to update it. Below, write such a function. It will take 5 inputs:

- X
- v
- max_iterations
- alpha (the step size)
- initial_weights

By default, have your function set the initial_weights parameter to a vector where all feature weights are set to 1.

```
# Your code here
def grad desc(X, y, max iterations, alpha, initial weights=None):
    """Be sure to set default behavior for the initial weights parameter."""
    if initial weights == None:
        initial weights = np.ones((X.shape[1],1)).flatten()
   weights col= pd.DataFrame(initial weights)
    weights = initial weights
    # Create a for loop of iterations
    for iteration in range(max iterations):
        # Generate predictions using the current feature weights
        predictions = sigmoid(np.dot(X,weights))
        # Calculate an error vector based on these initial predictions and the corre
        error vector = y - predictions
        # Calculate the gradient
        # As we saw in the previous lab, calculating the gradient is often the most
        # Here, your are provided with the closed form solution for the gradient of
        # For more details on the derivation, see the additional resources section b
        gradient = np.dot(X.transpose(),error vector)
        # Update the weight vector take a step of alpha in direction of gradient
        weights += alpha * gradient
        weights_col = pd.concat([weights_col, pd.DataFrame(weights)], axis=1)
    # Return finalized weights
    return weights, weights_col
```

Running your algorithm

Now that you've coded everything from the ground up, you can further investigate the convergence behavior of the gradient descent algorithm. Remember that gradient descent does not guarantee a global minimum, only a local minimum, and that small deviations in the starting point or step size can lead to different outputs.

First, run the following cell to import the data and create the predictor and target variables:

```
import pandas as pd
 df = pd.read csv('heart.csv')
 # Create the predictor and target variables
 y = df['target']
 X = df.drop(columns=['target'], axis=1)
 print(y.value_counts())
 X.head()
 1.0
         165
 0.0
         138
 Name: target, dtype: int64
<style scoped> .dataframe tbody tr th:only-of-type { vertical-align: middle; }
  .dataframe tbody tr th {
      vertical-align: top;
 }
  .dataframe thead th {
      text-align: right;
```

</style>

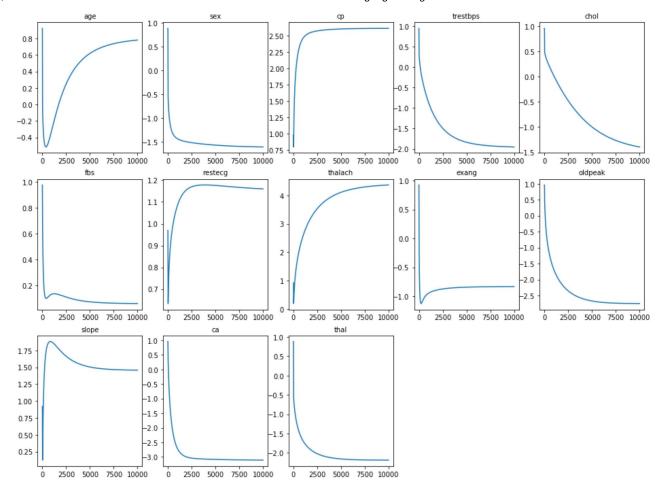
79										
	age	sex	ср	trestbps	chol	fbs	restecg	thalac		
0	0.708333	1.0	1.000000	0.481132	0.244292	1.0	0.0	0.6030		
1	0.166667	1.0	0.666667	0.339623	0.283105	0.0	0.5	0.8854		
2	0.250000	0.0	0.333333	0.339623	0.178082	0.0	0.0	0.7709		
3	0.562500	1.0	0.333333	0.245283	0.251142	0.0	0.5	0.8167		

	age	sex	ср	trestbps	chol	fbs	restecg	thalac
4	0.583333	0.0	0.000000	0.245283	0.520548	0.0	0.5	0.7022

Run your algorithm and plot the successive weights of the features through iterations. Below is a dataset, with x and y predefined for you. Use your logistic regression function to train a model. As the model trains, record the iteration cycle of the gradient descent algorithm and the weights of the various features. Then, plot this data on subplots for each of the individual features. Each graph should have the iteration number on the x-axis and the value of that feature weight for that iteration cycle on the y-axis. This will visually display how the algorithm is adjusting the weights over successive iterations, and hopefully show convergence to stable weights.

```
weights, weight_col = grad_desc(X, y, 10000, 0.001)
weight_col.columns = np.arange(len(weight_col.columns))
plt.figure(figsize=(16, 12))

for (i, j) in enumerate(weights):
    plt.subplot(3, 5, i + 1)
    plt.title(list(X)[i], size='medium')
    plt.plot(weight_col.iloc[i].T)
    plt.axis('tight')
```



Scikit-learn

For comparison, import scikit-learn's standard LogisticRegression() function. Initialize it with **no intercept** and **C=1e16** or another very high number. The reason is as follows: our implementation has not used an intercept, and you have not performed any regularization such as Lasso or Ridge (scikit-learn uses I2 by default). The high value of c will essentially negate this. Also, set the <code>random_state</code> to 2 and use the 'liblinear' solver.

After initializing a regression object, fit it to x and y.

```
# Your code here
from sklearn.linear_model import LogisticRegression
logreg = LogisticRegression(fit_intercept=False, C=1e16, random_state=2, solver='lib
logreg.fit(X, y)
```

```
random_state=2, solver='liblinear', tol=0.0001, verbose=0,
warm start=False)
```

Compare the models

Compare the coefficient weights of your model to that generated by scikit-learn.

Level up (Optional)

Update the gradient descent algorithm to also return the cost after each iteration. Then rerun the algorithm and create a graph displaying the cost versus the iteration number.

```
# Your code here
import matplotlib.pyplot as plt
%matplotlib inline

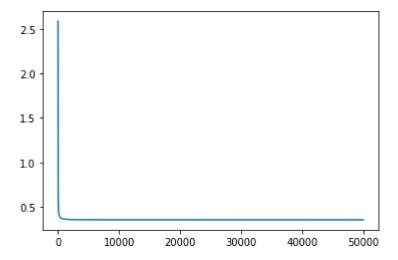
def grad_desc(X, y, max_iterations, alpha, initial_weights=None):
    """Be sure to set default behavior for the initial_weights parameter."""
    if initial_weights == None:
        initial_weights = np.ones((X.shape[1],1)).flatten()
    weights = initial_weights
    costs = []
    # Create a for loop of iterations
    for iteration in range(max_iterations):
        # Generate predictions using the current feature weights
        predictions = sigmoid(np.dot(X,weights))
        # Calculate an error vector based on these initial predictions and the corre
        error_vector = y - predictions
```

```
# Calculate the gradient (transpose of X times error is the gradient)
    gradient = np.dot(X.transpose(),error_vector)
    # Update the weight vector take a step of alpha in direction of gradient
    weights += alpha * gradient
    # Calculate the cost
    cost = ((-y * np.log(predictions))-((1-y)* np.log(1-predictions))).mean()
    costs.append(cost)
    # Return finalized Weights
    return weights, costs

max_iterations = 50000
weights, costs = grad_desc(X, y, max_iterations, 0.001)
print('Coefficient weights:\n', weights)
plt.plot(range(max_iterations), costs)
plt.show()
```

```
Coefficient weights:

[ 0.8122867 -1.61296293 2.61777735 -1.96890616 -1.50963664 0.05698231 1.15221375 4.42107696 -0.83034101 -2.74655062 1.45579366 -3.11550418 -2.19128237]
```



Additional Resources

If you want to see more of the mathematics behind the gradient derivation above, check out section 4.4.1 from the Elements of Statistical Learning which can be found here: https://web.stanford.edu/~hastie/ElemStatLearn//.

Summary

Congratulations! You just coded logistic regression from the ground up using NumPy! With this, you should have a fairly deep understanding of logistic regression and how the algorithm works! In the upcoming labs, you'll continue to explore this from a few more angles, plotting your data along with the decision boundary for our predictions.

Releases

No releases published

Packages

No packages published

Contributors 6











Languages

Jupyter Notebook 100.0%