

Calculate Minkowski distance between two points

Getting Started

You'll start by writing a generalized function to calculate any of the three distance metrics you've learned about. Let's review what you know so far:

The *Manhattan distance* and *Euclidean distance* are both special cases of *Minkowski distance*.

Take a look at the formula for Minkowski distance below:

$$d(x,y) = \left(\sum_{i=1}^n |x_i-y_i|^c
ight)^{rac{1}{c}}$$

Manhattan distance is a special case where c=1 in the equation above (which means that you can remove the root operation and just keep the summation).

Euclidean distance is a special case where c=2 in the equation above.

Knowing this, you can create a generalized distance() function that calculates Minkowski distance, and takes in c as a parameter. That way, you can use the same function for every problem, and still calculate Manhattan and Euclidean distance metrics by just passing in the appropriate values for the c parameter!

In the cell below:

- Complete the distance() function which should implement the Minkowski distance equation above to return the distance, a single number
- This function should take in 4 arguments:
 - o a : a tuple or array that describes a vector in n-dimensional space
 - o b: a tuple or array that describes a vector in n-dimensional space (this must be the same length as a!)
 - o c: which tells us the norm to calculate the vector space (if set to 1, the result will be Manhattan, while 2 will calculate Euclidean distance)
 - verbose: set to True by default. If true, the function should print out if the distance metric returned is a measurement of Manhattan, Euclidean, or Minkowski distance
- Since euclidean distance is the most common distance metric used, this function should default to using c=2 if no value is set for c

HINT:

- 1. You can avoid using a for loop like we did in the previous lesson by simply converting the tuples to NumPy arrays
- 2. Use np.power() as an easy way to implement both squares and square roots.

 np.power(a, 3) will return the cube of a, while np.power(a, 1/3) will return the cube root of 3. For more information on this function, refer the NumPy documentation!

```
import numpy as np
def distance(a, b, c=2, verbose=True):
    if len(a) != len(b):
        raise ValueError("Both vectors must be of equal length!")
    if verbose:
        if c == 1:
            print("Calculating Manhattan distance:")
        elif c == 2:
            print("Calculating Euclidean distance:")
        else:
            print(f"Calcuating Minkowski distance (c={c}):")
    return np.power(np.sum(np.power(np.abs(np.array(a) - np.array(b)), c)), 1/c)
test_point_1 = (1, 2)
test point 2 = (4, 6)
print(distance(test point 1, test point 2)) # Expected Output: 5.0
print(distance(test_point_1, test_point_2, c=1)) # Expected Output: 7.0
print(distance(test point 1, test point 2, c=3)) # Expected Output: 4.49794144527541
Calculating Euclidean distance:
5.0
Calculating Manhattan distance:
7.0
Calcuating Minkowski distance (c=3):
4.497941445275415
```

Great job!

Now, use your function to calculate distances between points:

Problem 1

Calculate the *Euclidean distance* between the following points in 5-dimensional space:

```
Point 1: (-2, -3.4, 4, 15, 7)
```

Point 2: (3, -1.2, -2, -1, 7)

```
print(distance((-2, -3.4, 4, 15, 7), (3, -1.2, -2, -1, 7))) # Expected Output: 17.93
```

Calculating Euclidean distance: 17.939899665271266

Problem 2

Calculate the *Manhattan distance* between the following points in 10-dimensional space:

```
Point 1: [0, 0, 0, 7, 16, 2, 0, 1, 2, 1]
```

Point 2: [1, -1, 5, 7, 14, 3, -2, 3, 3, 6]

```
print(distance( [0, 0, 0, 7, 16, 2, 0, 1, 2, 1], [1, -1, 5, 7, 14, 3, -2, 3, 3, 6],
```

Calculating Manhattan distance: 20.0

Problem 3

Calculate the *Minkowski distance* with a norm of 3.5 between the following points:

```
Point 1: (-2, 7, 3.4)
```

Point 2: (3, 4, 1.5)

```
print(distance((-2, 7, 3.4), (3, 4, 1.5), c=3.5)) # Expected Output: 5.2687896591883
```

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Calcuating Minkowski distance (c=3.5): 5.268789659188307

Summary

Great job! Now that you know about the various distance metrics, you can use them to writing a K-Nearest Neighbors classifier from scratch!

Releases

No releases published

Packages

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