

1. Find a minimal cover for the following FD set

FDs = { $FGH \rightarrow I$, $FI \rightarrow H$, $DI \rightarrow G$, $DH \rightarrow EG$, $I \rightarrow F$, $H \rightarrow F$ }

1) Decomposition

$FGH \rightarrow I$
 $FI \rightarrow H$
 $DI \rightarrow G$
 $DH \rightarrow E$
 $DH \rightarrow G$
 $I \rightarrow F$
 $H \rightarrow F$

2) Redundant LHS

$FGH \rightarrow FG$ (removed H) $\rightarrow FG+ = FG$
 $FGH \rightarrow FH$ (removed G) $\rightarrow FH+ = FH$
 $FGH \rightarrow GH$ (removed F) $\rightarrow GH+ = GHFI$ [redundant]
 $FI \rightarrow F$ (removed I) $\rightarrow F+ = F$
 $FI \rightarrow I$ (removed F) $\rightarrow I+ = IFH$ [redundant]
 $DI \rightarrow D$ (removed I) $\rightarrow D+ = D$
 $DI \rightarrow I$ (removed F) $\rightarrow I+ = IFH$
 $DH \rightarrow D$ (removed H) $\rightarrow D+ = D$
 $DH \rightarrow H$ (removed D) $\rightarrow H+ = HF$

FGH replaced by GH
 FI replaced by I

3) Remove redundant dependencies

$GH \rightarrow I \Rightarrow GH+ = GHF$
 $I \rightarrow H \Rightarrow I+ = IF$
 $DI \rightarrow G \Rightarrow DI+ = DIHEGF$ [redundant]
 $DH \rightarrow E \Rightarrow DH+ = DHGIF$
 $DH \rightarrow G \Rightarrow DH+ = DHE$
 $I \rightarrow F \Rightarrow I+ = IHF$ [redundant]
 $H \rightarrow F \Rightarrow H+ = H$

4) Combine common LHS

$GH \rightarrow I$
 $I \rightarrow H$
 $DH \rightarrow EG$
 $H \rightarrow F$

Without combining

$GH \rightarrow I$
 $I \rightarrow H$
 $DH \rightarrow E$
 $DH \rightarrow G$
 $H \rightarrow F$

2. Use the universal table and the **Minimal Cover** FD shown below to answer parts a, b and c.

Universal Table BCDFGH

Minimal cover FD set { $BG \rightarrow C$, $G \rightarrow F$, $C \rightarrow H$, $C \rightarrow G$, $F \rightarrow D$ }

a. Find a key for the universal table.

A potential key is: B, C

$C+ = CHGFD$

b. Is the decomposition of BCDFGH into GFD and BGCH lossless? Justify your answer.

Given that we can intersect GFD and BGCH on G which means we can do a natural join on both of them, we preserve lossless decomposition

c. Use 3NF synthesis to create a set of 3NF tables.

Combine LHS

$C \rightarrow HG$
 $BG \rightarrow C$
 $G \rightarrow F$
 $F \rightarrow D$

$R1 = \{C, H, G\}$
 $R2 = \{B, G, C\}$
 $R3 = \{G, F\}$
 $R4 = \{F, D\}$

$R2 = \{B, G, C\} \rightarrow BGC+ = BGCHFD$