#### Import the libraries

```
In [1]: #importing the libraries
import tensorflow as tf
from tensorflow import keras
import numpy as np
import pandas as pd
```

WARNING:tensorflow:From C:\Users\Teo Boon Kean\AppData\Local\Programs\Python\Python311\Lib\site-packages\keras\s rc\losses.py:2976: The name tf.losses.sparse\_softmax\_cross\_entropy is deprecated. Please use tf.compat.v1.losses .sparse\_softmax\_cross\_entropy instead.

#### Load the data and data pre-processing

```
In [2]: #load the datasets
        baseline df = pd.read excel('extracted features baseline.xlsx')
        toolwear df = pd.read excel('extracted features toolwear.xlsx')
In [3]: #labelling the datasets. O for baseline, 1 for toolwear. This will be the variable the model tries to predict
        baseline_df["state"] = 0
        toolwear_df["state"] = 1
In [4]: #concantanate the datasets
        combined df = pd.concat([baseline df, toolwear_df], axis=0)
        print(combined_df.shape)
       (840, 67)
In [5]: #getting the y label
        state = combined_df["state"].values
        print(state.shape)
       (840,)
In [6]: #getting the features to train the model
        features = combined_df.drop('state', axis=1).values
        print(features.shape)
       (840, 66)
In [7]: #train test split
        from sklearn.model selection import train test split
        X train, X test, Y train, Y test = train test split(features, state, test size=0.2, random state=50)
In [8]: #data scalling
        from sklearn.preprocessing import StandardScaler
        sc = StandardScaler()
        X_train = sc.fit_transform(X train)
        X_test = sc.transform(X_test)
```

# Specify the architecture of the stacked autoencoder

```
In [9]: #specify the number of condensed features for the 3 autoencoders. This will be the number of neurons in the hide
condensed_e1 = 50
condensed_e2 = 30
condensed_e3 = 10
```

# Construction and training of the first-Level autoencoder

```
In [10]: #constructing the first Autoencoder

#input layer
in_ael = keras.Input(features.shape[1])
#hidden encoded layer
h_ael = keras.layers.Dense(condensed_el)(in_ael)
#output layer
out_ael = keras.layers.Dense(features.shape[1])(h_ael)

ael = keras.Model(in_ael, out_ael)
encoderl = keras.Model(in_ael, h_ael)
ael.summary()
```

WARNING:tensorflow:From C:\Users\Teo Boon Kean\AppData\Local\Programs\Python\Python311\Lib\site-packages\keras\s rc\backend.py:1398: The name tf.executing\_eagerly\_outside\_functions is deprecated. Please use tf.compat.v1.executing\_eagerly\_outside\_functions instead.

#### Model: "model"

Layer (type)	Output Shape	Param #
input_1 (InputLayer)	[(None, 66)]	0
dense (Dense)	(None, 50)	3350
dense_1 (Dense)	(None, 66)	3366

\_\_\_\_\_

Total params: 6716 (26.23 KB)
Trainable params: 6716 (26.23 KB)
Non-trainable params: 0 (0.00 Byte)

```
In [11]: #compilling and training the first autoencoder
    ael.compile(optimizer='adam', loss='mse')
    ael.fit(X_train, X_train, epochs = 50, batch_size = 8, validation_split = 0.1)
```

WARNING:tensorflow:From C:\Users\Teo Boon Kean\AppData\Local\Programs\Python\Python311\Lib\site-packages\keras\s rc\optimizers\\_\_init\_\_.py:309: The name tf.train.Optimizer is deprecated. Please use tf.compat.v1.train.Optimize r instead.

#### Epoch 1/50

WARNING:tensorflow:From C:\Users\Teo Boon Kean\AppData\Local\Programs\Python\Python311\Lib\site-packages\keras\s rc\utils\tf\_utils.py:492: The name tf.ragged.RaggedTensorValue is deprecated. Please use tf.compat.v1.ragged.RaggedTensorValue instead.

```
Epoch 2/50
76/76 [=====
         Epoch 3/50
76/76 [====
          Epoch 4/50
76/76 [=====
          Epoch 5/50
76/76 [====
               =======] - Os 2ms/step - loss: 0.0950 - val loss: 0.0772
Epoch 6/50
           76/76 [====
Epoch 7/50
76/76 [====
                =======] - 0s 2ms/step - loss: 0.0597 - val_loss: 0.0511
Epoch 8/50
76/76 [====
                  ======] - 0s 2ms/step - loss: 0.0502 - val loss: 0.0430
Epoch 9/50
76/76 [=====
          Fnoch 10/50
76/76 [========== ] - 0s 2ms/step - loss: 0.0374 - val loss: 0.0330
Epoch 11/50
Epoch 12/50
76/76 [====
                =======] - 0s 2ms/step - loss: 0.0291 - val_loss: 0.0265
Epoch 13/50
76/76 [====
                 =======] - Os 3ms/step - loss: 0.0262 - val_loss: 0.0238
Epoch 14/50
76/76 [====
               =======] - Os 2ms/step - loss: 0.0237 - val loss: 0.0222
Epoch 15/50
76/76 [=====
            =========] - 0s 2ms/step - loss: 0.0215 - val loss: 0.0202
Epoch 16/50
76/76 [=====
           =========] - 0s 2ms/step - loss: 0.0198 - val_loss: 0.0193
Epoch 17/50
76/76 [=====
          Epoch 18/50
76/76 [=====
          Epoch 19/50
76/76 [=============] - 0s 2ms/step - loss: 0.0158 - val loss: 0.0152
Epoch 20/50
76/76 [=====
              ========] - Os 2ms/step - loss: 0.0147 - val loss: 0.0141
Epoch 21/50
76/76 [=====
              ========] - Os 2ms/step - loss: 0.0138 - val_loss: 0.0131
Epoch 22/50
                 =======] - Os 2ms/step - loss: 0.0128 - val_loss: 0.0129
76/76 [====
Epoch 23/50
                =======] - Os 2ms/step - loss: 0.0122 - val_loss: 0.0120
76/76 [====
Epoch 24/50
            76/76 [=====
Epoch 25/50
Epoch 26/50
76/76 [============] - 0s 2ms/step - loss: 0.0102 - val_loss: 0.0100
```

```
Epoch 27/50
    76/76 [============ ] - 0s 2ms/step - loss: 0.0096 - val loss: 0.0092
    Epoch 28/50
    Epoch 29/50
    76/76 [=====
                  ========] - Os 2ms/step - loss: 0.0086 - val loss: 0.0084
    Epoch 30/50
    76/76 [======
              Epoch 31/50
                76/76 [=====
    Epoch 32/50
    76/76 [=====
                   =======] - 0s 2ms/step - loss: 0.0073 - val_loss: 0.0073
    Epoch 33/50
    Epoch 34/50
    Epoch 35/50
    Epoch 36/50
               =========] - 0s 2ms/step - loss: 0.0060 - val_loss: 0.0063
    76/76 [=====
    Epoch 37/50
                  =======] - Os 3ms/step - loss: 0.0058 - val_loss: 0.0057
    76/76 [=====
    Epoch 38/50
                  ========] - Os 3ms/step - loss: 0.0055 - val_loss: 0.0056
    76/76 [=====
    Epoch 39/50
    76/76 [===========] - 0s 2ms/step - loss: 0.0052 - val loss: 0.0054
    Epoch 40/50
    76/76 [=============] - 0s 2ms/step - loss: 0.0050 - val_loss: 0.0051
    Epoch 41/50
    Epoch 42/50
    Epoch 43/50
    76/76 [========== ] - 0s 2ms/step - loss: 0.0044 - val loss: 0.0043
    Epoch 44/50
    76/76 [===========] - 0s 2ms/step - loss: 0.0042 - val loss: 0.0044
    Epoch 45/50
    76/76 [============] - 0s 2ms/step - loss: 0.0040 - val_loss: 0.0041
    Epoch 46/50
    76/76 [======
             Epoch 47/50
    76/76 [=====
                  ========] - 0s 2ms/step - loss: 0.0037 - val loss: 0.0037
    Epoch 48/50
    Epoch 49/50
    76/76 [===========] - 0s 2ms/step - loss: 0.0035 - val loss: 0.0033
    76/76 [============] - 0s 2ms/step - loss: 0.0033 - val loss: 0.0034
Out[11]: <keras.src.callbacks.History at 0x11d3d978250>
```

### Encoding the original features with the first-level encoder

#### Construction and training of the second-level autoencoder

```
In [13]: #constructing the second Autoencoder

#input layer
in_ae2 = keras.Input(condensed_e1)
#hidden encoded layer
h_ae2 = keras.layers.Dense(condensed_e2)(in_ae2)
#output layer
out_ae2 = keras.layers.Dense(condensed_e1)(h_ae2)
ae2 = keras.Model(in_ae2, out_ae2)
encoder2 = keras.Model(in_ae2, h_ae2)
ae2.summary()
```

Layer (type)	Output Shape	Param #
input_2 (InputLayer)	[(None, 50)]	0
dense_2 (Dense)	(None, 30)	1530
dense_3 (Dense)	(None, 50)	1550

\_\_\_\_\_

Total params: 3080 (12.03 KB) Trainable params: 3080 (12.03 KB) Non-trainable params: 0 (0.00 Byte)

```
In [14]: #compilling and training the second autoencoder using the encoded features from the first encoder
      ae2.compile(optimizer='adam', loss='mse')
      ae2.fit(encoded1, encoded1, epochs = 50, batch_size = 8, validation_split = 0.1)
     Epoch 1/50
     76/76 [=========== ] - 1s 3ms/step - loss: 1.5454 - val loss: 0.7970
     Epoch 2/50
     76/76 [===========] - 0s 2ms/step - loss: 0.6806 - val loss: 0.4427
     Epoch 3/50
     76/76 [====
                     ========] - Os 2ms/step - loss: 0.3951 - val loss: 0.2988
     Epoch 4/50
     76/76 [====
                      =======] - Os 2ms/step - loss: 0.2691 - val loss: 0.2177
     Epoch 5/50
                        =======] - 0s 2ms/step - loss: 0.2003 - val loss: 0.1681
     76/76 [===
     Epoch 6/50
     76/76 [====
                         =======] - Os 2ms/step - loss: 0.1570 - val loss: 0.1333
     Epoch 7/50
     76/76 [=====
                Epoch 8/50
     76/76 [====
                Epoch 9/50
     76/76 [====
                   Epoch 10/50
     76/76 [=====
                   Epoch 11/50
     76/76 [====
                      =======] - 0s 2ms/step - loss: 0.0683 - val loss: 0.0619
     Epoch 12/50
                    ========] - 0s 2ms/step - loss: 0.0612 - val_loss: 0.0555
     76/76 [=====
     Epoch 13/50
     76/76 [====
                        =======] - 0s 2ms/step - loss: 0.0554 - val_loss: 0.0514
     Epoch 14/50
     76/76 [====
                           =====] - Os 2ms/step - loss: 0.0511 - val loss: 0.0472
     Epoch 15/50
     76/76 [=====
                   =========] - 0s 2ms/step - loss: 0.0469 - val loss: 0.0433
     Fnoch 16/50
     76/76 [======
                Epoch 17/50
     Epoch 18/50
     76/76 [====
                         ======] - 0s 2ms/step - loss: 0.0381 - val_loss: 0.0357
     Epoch 19/50
     76/76 [===
                         ======] - Os 2ms/step - loss: 0.0355 - val loss: 0.0338
     Epoch 20/50
     76/76 [====
                       ========] - Os 2ms/step - loss: 0.0334 - val loss: 0.0324
     Epoch 21/50
     76/76 [=====
                    =========] - 0s 2ms/step - loss: 0.0315 - val loss: 0.0303
     Epoch 22/50
     76/76 [=====
                  Epoch 23/50
     76/76 [=====
                Epoch 24/50
                   76/76 [=====
     Epoch 25/50
     Epoch 26/50
     76/76 [=====
                      ========] - Os 2ms/step - loss: 0.0242 - val loss: 0.0237
     Epoch 27/50
     76/76 [====
                      =======] - Os 2ms/step - loss: 0.0230 - val_loss: 0.0226
     Epoch 28/50
                        =======] - 0s 2ms/step - loss: 0.0221 - val_loss: 0.0215
     76/76 [====
     Epoch 29/50
                       =======] - Os 2ms/step - loss: 0.0212 - val_loss: 0.0203
     76/76 [====
     Epoch 30/50
                  76/76 [=====
     Epoch 31/50
     Epoch 32/50
```

```
Epoch 33/50
     76/76 [============= ] - 0s 2ms/step - loss: 0.0182 - val loss: 0.0177
     Epoch 34/50
     76/76 [======
               Epoch 35/50
     76/76 [====
                      ========] - Os 2ms/step - loss: 0.0167 - val loss: 0.0161
     Epoch 36/50
     76/76 [=====
                    ========] - Os 2ms/step - loss: 0.0163 - val loss: 0.0160
     Epoch 37/50
     76/76 [=====
                     ========] - Os 2ms/step - loss: 0.0158 - val_loss: 0.0151
     Epoch 38/50
     76/76 [====
                        ======] - 0s 2ms/step - loss: 0.0153 - val_loss: 0.0150
     Epoch 39/50
                76/76 [======
     Epoch 40/50
     Epoch 41/50
     Epoch 42/50
                     ========] - Os 2ms/step - loss: 0.0134 - val_loss: 0.0130
     76/76 [=====
     Epoch 43/50
                      =======] - Os 2ms/step - loss: 0.0131 - val_loss: 0.0126
     76/76 [====
     Epoch 44/50
     76/76 [=====
                      =======] - Os 2ms/step - loss: 0.0130 - val_loss: 0.0125
     Epoch 45/50
                  ========] - Os 2ms/step - loss: 0.0124 - val_loss: 0.0124
     76/76 [=====
     Epoch 46/50
     76/76 [=============] - 0s 2ms/step - loss: 0.0122 - val_loss: 0.0117
     Epoch 47/50
     76/76 [=============] - 0s 2ms/step - loss: 0.0118 - val_loss: 0.0118
     Epoch 48/50
     Epoch 49/50
     Epoch 50/50
     76/76 [============] - 0s 2ms/step - loss: 0.0110 - val_loss: 0.0109
Out[14]: <keras.src.callbacks.History at 0x11d40233e10>
```

#### Encoding the first-level features with the second-level encoder

# Construction and training of the third-level autoencoder

```
In [16]: #constructing the third Autoencoder

#input layer
in_ae3 = keras.Input(condensed_e2)
#hidden encoded layer
h_ae3 = keras.layers.Dense(condensed_e3)(in_ae3)
#output layer
out_ae3 = keras.layers.Dense(condensed_e2)(h_ae3)

ae3 = keras.Model(in_ae3, out_ae3)
encoder3 = keras.Model(in_ae3, h_ae3)

ae3.summary()
```

Model: "model\_4"

Layer (type)	Output Shape	Param #
input_3 (InputLayer)	[(None, 30)]	0
dense_4 (Dense)	(None, 10)	310
dense_5 (Dense)	(None, 30)	330
Total params: 640 (2.50 k	:=====================================	

Total params: 640 (2.50 KB) Trainable params: 640 (2.50 KB) Non-trainable params: 0 (0.00 Byte)

```
In [17]: #compilling and training the third autoencoder using the encoded features from the second encoder
    ae3.compile(optimizer='adam', loss='mse')
    ae3.fit(encoded2, encoded2, epochs = 50, batch_size = 8, validation_split = 0.1)
```

```
Epoch 1/50
76/76 [============ ] - 1s 3ms/step - loss: 2.9634 - val loss: 2.0508
Epoch 2/50
76/76 [============= ] - 0s 2ms/step - loss: 1.9371 - val loss: 1.4378
Epoch 3/50
76/76 [====
            ========] - 0s 2ms/step - loss: 1.3860 - val loss: 1.0655
Epoch 4/50
76/76 [====
       Epoch 5/50
76/76 [====
        Epoch 6/50
76/76 [====
             ========] - Os 2ms/step - loss: 0.7824 - val_loss: 0.6811
Epoch 7/50
76/76 [============ ] - 0s 2ms/step - loss: 0.6939 - val loss: 0.6094
Epoch 8/50
Epoch 9/50
Epoch 10/50
         76/76 [=====
Epoch 11/50
76/76 [=====
             ========] - 0s 2ms/step - loss: 0.4758 - val_loss: 0.4301
Epoch 12/50
76/76 [====
            ========] - Os 2ms/step - loss: 0.4462 - val_loss: 0.4060
Epoch 13/50
76/76 [=========== ] - 0s 2ms/step - loss: 0.4238 - val loss: 0.3905
Epoch 14/50
76/76 [============] - 0s 2ms/step - loss: 0.4056 - val_loss: 0.3760
Epoch 15/50
Epoch 16/50
76/76 [============ ] - 0s 2ms/step - loss: 0.3816 - val loss: 0.3568
Epoch 17/50
Epoch 18/50
76/76 [============ ] - 0s 2ms/step - loss: 0.3649 - val loss: 0.3424
Epoch 19/50
Epoch 20/50
Epoch 21/50
76/76 [====
                   ==] - 0s 2ms/step - loss: 0.3476 - val_loss: 0.3291
Epoch 22/50
Epoch 23/50
76/76 [========== ] - 0s 2ms/step - loss: 0.3390 - val loss: 0.3197
Epoch 24/50
76/76 [============] - 0s 2ms/step - loss: 0.3349 - val loss: 0.3178
Epoch 25/50
76/76 [=====
           =========] - Os 2ms/step - loss: 0.3318 - val_loss: 0.3130
Epoch 26/50
76/76 [====
              =======] - Os 2ms/step - loss: 0.3291 - val_loss: 0.3114
Epoch 27/50
76/76 [====
                ======] - Os 2ms/step - loss: 0.3265 - val loss: 0.3085
Epoch 28/50
76/76 [=====
         Epoch 29/50
76/76 [===========] - 0s 2ms/step - loss: 0.3220 - val loss: 0.3049
Epoch 30/50
Epoch 31/50
Epoch 32/50
76/76 [========== ] - 0s 2ms/step - loss: 0.3159 - val loss: 0.2998
Epoch 33/50
76/76 [======
        Epoch 34/50
76/76 [======
         Epoch 35/50
76/76 [=====
             ========] - Os 2ms/step - loss: 0.3110 - val loss: 0.2969
Epoch 36/50
76/76 [====
           =========] - Os 2ms/step - loss: 0.3097 - val loss: 0.2955
Epoch 37/50
76/76 [========== ] - 0s 2ms/step - loss: 0.3086 - val loss: 0.2932
Epoch 38/50
Epoch 39/50
Epoch 40/50
Epoch 41/50
76/76 [====
          Epoch 42/50
```

```
Epoch 43/50
    76/76 [========== ] - 0s 2ms/step - loss: 0.3019 - val loss: 0.2898
    Epoch 44/50
    76/76 [==
                   =======] - Os 2ms/step - loss: 0.3007 - val loss: 0.2898
    Epoch 45/50
    76/76 [=====
                   =======] - Os 2ms/step - loss: 0.3000 - val loss: 0.2897
    Epoch 46/50
               76/76 [=====
    Epoch 47/50
                 76/76 [=====
    Epoch 48/50
    Epoch 49/50
    76/76 [===========] - 0s 2ms/step - loss: 0.2970 - val loss: 0.2870
    Epoch 50/50
    76/76 [==========] - 0s 2ms/step - loss: 0.2968 - val loss: 0.2853
Out[17]: <keras.src.callbacks.History at 0x11d400ca790>
```

#### Constructing the final stacked autoencoder

```
In [18]: #constructing the stacked autoencoder. Initialising all the layers
         #input layer which number of neurons equals the number of original features
         l in = keras.Input(features.shape[1])
         #hidden layer of encoder 1
         l_e1 = keras.layers.Dense(condensed_e1)(l_in)
         #hidden layer of encoder 2
         l e2 = keras.layers.Dense(condensed e2)(l e1)
         #hidden layer of encoder 3
         l e3 = keras.layers.Dense(condensed e3)(l e2)
         #hidden layer of decoder 2
         l d2 = keras.layers.Dense(condensed e2)(l e3)
         #hidden layer of decoder 1
         l_d1 = keras.layers.Dense(condensed_e1)(l_d2)
         #output layer which is the same as the input
         l out = keras.layers.Dense(features.shape[1])(l d1)
         #defining the autoencode
         stacked_ae = keras.Model(l_in, l_out)
         stacked ae.summary()
```

Model: "model 6"

Layer (type)	Output Shape	Param #
input_4 (InputLayer)	[(None, 66)]	0
dense_6 (Dense)	(None, 50)	3350
dense_7 (Dense)	(None, 30)	1530
dense_8 (Dense)	(None, 10)	310
dense_9 (Dense)	(None, 30)	330
dense_10 (Dense)	(None, 50)	1550
dense_11 (Dense)	(None, 66)	3366
=======================================		

Total params: 10436 (40.77 KB)
Trainable params: 10436 (40.77 KB)
Non-trainable params: 0 (0.00 Byte)

# Transferring the trained weights of the 3 autoencoders to the stacked autoencoder

```
In [19]: #setting the weights of the stacked autoencoder to those in the trained autoencoders

#first encoder layer
stacked_ae.layers[1].set_weights(ae1.layers[1].get_weights())
```

```
#second encoder layer
stacked_ae.layers[2].set_weights(ae2.layers[1].get_weights())
#third encoder layer
stacked_ae.layers[3].set_weights(ae3.layers[1].get_weights())
#first decoder layer
stacked_ae.layers[4].set_weights(ae3.layers[2].get_weights())
#second decoder layer
stacked_ae.layers[5].set_weights(ae2.layers[2].get_weights())
#second decoder layer
stacked_ae.layers[6].set_weights(ae1.layers[2].get_weights())
```

### Evaluating the performance of stacked autoencoder

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