VLSI DPS HW#4

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1. Calculate the Frobenius Distance

```
Matrix A:

-104   -4   -119   -85

-57   76   89   52

12   -92   111   -120

117   -21   45   -58

119   106   65   -117

-88   74   62   -104

120   117   -28   82

117   39   39   49
```

• Generate a random matrix A

-0.3726	-0.2042	0.0430	0.4192	0.4264	-0.3153	0.4300	0.4192
0.0918	0.4283	-0.4575	-0.2266	0.3851	0.4517	0.4372	0.0634
-0.4671	0.4719	0.5443	0.1017	0.1681	0.3738	-0.2847	0.0594
-0.5104	0.3772	-0.2673	-0.2421	-0.5552	-0.3311	0.1386	0.1732
0.6116	0.4864	0.2875	0.1650	-0.1330	-0.2509	0.0945	0.4358
0	0.4163	-0.2190	0.3501	0.2810	-0.4499	-0.1521	-0.5930
0	0	0.5390	-0.3943	0.0328	-0.1821	0.5809	-0.427
0	0	0	-0.6314	0.4854	-0.3856	-0.3927	0.250
atrix Q_fix	κ :						
-0.3750	-0.2031	0.0361	0.4150	0.4258	-0.3213	0.4258	0.4189
-0.0918	0.4287	-0.4551	-0.2295	0.3867	0.4561	0.4365	0.061
-0.4697	-0.4756	0.5391	0.0977	0.1680	0.3701	-0.2900	0.0508
-0.5117	-0.3867	-0.0898	-0.2422	-0.5537	-0.3271	0.1426	0.1729
0.6084	-0.4941	0.4355	0.1631	-0.1367	-0.2598	0.0908	0.428
0	-0.4121	-0.0605	0.3584	0.2900	-0.4424	-0.1523	-0.5879
0	0	-0.5449	-0.3916	0.0332	-0.1836	0.5840	-0.4258
0	0	0	-0.6318	0.4863	-0.3857	-0.3916	0.244

Matrix R_fl	oat :		
279.0914	61.7289	62.2807	30.2840
0.0000	206.9023	9.4802	29.4226
-0.0000	-0.0000	206.9619	-85.9580
-0.0000	0.0000	-0.0000	228.3668
0.0000	-0.0000	0.0000	-0.0000
0.0000	-0.0000	0.0000	-0.0000
-0.0000	-0.0000	0.0000	-0.0000
0.0000	-0.0000	-0.0000	-0.0000
Matrix R_fi	x :		
	x : 61.0000	61.0000	30.0000
	3.5. S.	61.0000 9.0000	30.0000 28.5000
280.5000	61.0000		
280.5000	61.0000 208.2500	9.0000	28.5000 -86.7500
280.5000 0 0	61.0000 208.2500 0	9.0000 207.7500	28.5000 -86.7500
280.5000 0 0 0	61.0000 208.2500 0	9.0000 207.7500 0	28.5000 -86.7500 230.2500
0 0 0	61.0000 208.2500 0 0	9.0000 207.7500 0 0	28.5000 -86.7500 230.2500

- Q_float and R_float are generated from Q*[A|I] =[R|Q]
- Q_fix and R_fix are generated from Cordic given's rotation
- The Frobenius Distance (Euclidean Norm) is sqrt(trace((float-fix)*(float-fix)'))

```
Q Fix Point Loss:
2.1017

R Fix Point Loss:
3.4539
```

Fix-point precision

р с с р . с с с	• •			
Data	Sign bit	Integer part	Fraction part	Length
A (input)	1	7	0	8
Q (output)	1	1	10	12
R (output)	1	9	2	12
K (parameter)	1	0	9	10

2. Timing diagram

1 CYCLE 2 RD ADDR	01 0	2 3	4	5						12 63																					37 3 13 1		9 40	41	42	43 4	4 4:	146	4/	40 -	19 3	0 32	32	22 2	-	-	-	,0 5.	100	01	02 0	12 0	4 6:	0 00
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N : No Operation(idle)

• K : Multiplied by K

• 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |: The matrix index of data write back to tb

3. Clock cycles needed to complete one QR factorization

67 cycles

4. The initiation interval of two successive QR factorizations



When GG1 performs all vectoring over, the next input is valid. The initiation interval is 41 cycles.

Matlab result

```
fatrix A:
  -95 -125
               -53 -108
  113 -117
                      109
                62
  116
         -85
               -80
                       70
   19
          38
                47
                       -4
          59
               -82
                      -17
 -113
          37
  -68
               -34
                      -14
  -38
         -13
                32
                      - 50
   82
                        2
         12
                71
```

- Random matrix A
- Hardware loss

```
Hardware implementation loss

Fix Point Loss:

1.3477

Fix Point Loss:

2.3847
```

```
Actual values
                                                                        Shift to integer to simulate hardware performance
                                                                      ----- INT scale
----- Original scale
                                                                      Matrix Q_float :
Matrix O float :
                                                                      -393.3211 467.8451 480.2657 78.6642 -467.8451 -281.5351 -157.3284 339.4982
  -0.3841 0.4569
                  0.4690 0.0768 -0.4569 -0.2749 -0.1536
                                                                       -807.8038 -439.6231 -266.2414 230.0868 133.8913 88.4553 -128.0858 191.7783
  -0.7889 -0.4293 -0.2600
                           0.2247
                                   0.1308
                                            0.0864 -0.1251
                                                            0.1873
                                                    0.3423
                                                                        78.3759 307.1939 -753.7280 221.6229 -359.5194 -110.1942 350.5433 258.0019
   0.0765
          0.3000 -0.7361
                           0.2164
                                   -0.3511
                                            -0.1076
                                                             0.2520
                                                                       -349.4265 695.8533 -204.9684 -131.0403 355.1718 212.6709 -134.5897 -439.9903
           0.6795
                   -0.2002
                           -0.1280
                                    0.3468
  -0.3412
                                            0.2077
                                                    -0.1314
                                                             -0.4297
                                                                       336.2825 142.6095 -115.1396 456.8971 227.2753 129.8618 -713.2458 340.4449
   0.3284
          0.1393
                  -0.1124
                           0.4462
                                    0.2219
                                            0.1268
                                                    -0.6965
                                                             0.3325
                                                                             0 193.6781 252.2366 115.1114 560.8470 195.9207 542.0406 536.1423
       0
         0.1891 0.2463
                            0.1124
                                    0.5477
                                            0.1913
                                                    0.5293
                                                             0.5236
                                                                             0
                                                                                 0 245.0265 764.1410 -216.8794 346.2087 241.7700 -423.4107
       0
             0 0.2393
                            0.7462
                                   -0.2118
                                            0.3381
                                                   0.2361
                                                             -0.4135
                                            -0.8338
                                                    0.0720
                                                                             0
                                                                                              0 342.4072 378.3236 -853.8199 73.7731 -231.8482
       0
               0
                    0
                            0.3344
                                    0.3695
                                                             -0 2264
                                                                      Matrix Q fix :
Matrix Q_fix :
                                                                       -392 467 479
                                                                                       77 -470 -285 -163
                                                                                                           340
                            0.0752
                                   -0.4590 -0.2783 -0.1592
  -0.3828 0.4561
                  0.4678
                                                             0.3320
                                                                       -807 -437 -264
                                                                                                 97 -129
                                                                                       231
                                                                                            136
  -0.7881 -0.4268 -0.2578
                            0.2256
                                                                                                           196
                                   0.1328
                                            0.0947 -0.1260
                                                             0.1914
                                                                        78
                                                                             309 -752
                                                                                       222
                                                                                            -363
                                                                                                 -112
                                                                                                      354
   0.0762 0.3018 -0.7344
                           0.2168
                                   -0.3545
                                            -0.1094
                                                    0.3457
                                                             0.2441
                                                                        -356
                                                                             -94
                                                                                  100 -139
                                                                                            342
                                                                                                 196
                                                                                                      -99
  -0.3477
          -0.0918
                   0.0977
                           -0.1357
                                    0.3340
                                            0.1914
                                                    -0.0967
                                                             -0.4404
                                                                        330 -691
                                                                                  196
                                                                                       448
                                                                                            223
                                                                                                 136 -701
   0.3223
          -0.6748
                   0.1914
                            0.4375
                                    0.2178
                                            0.1328
                                                    -0.6846
                                                             0.3213
                                                                        0 -189 -238
                                                                                        80
                                                                                            533
                                                                                                 206
                                                                                                      514
       0 -0.1846 -0.2324
                                            0.2012
                                                    0.5020
                                                             0.5146
                            0.0781
                                    0.5205
                                                                          0
                                                                             0 256
                                                                                       778 -197
                                                                                                 323
                                                                                                      261 -416
       0
             0 0.2500
                            0.7598
                                    -0.1924
                                            0.3154
                                                     0.2549
                                                             -0.4063
                                                                               0
                                                                                    0
                                                                                       327
                                                                                            402 -857
       0
               0
                       0
                            0.3193
                                    0.3926
                                           -0.8369
                                                    0.0762
                                                            -0.1963
                                                                              DataTypeMode: Fixed-point: binary point scaling
Matrix R float :
                                                                                Signedness: Signed
 247.3297 -73.5415 80.2087 143.7676
                                                                                WordLength: 12
  -0.0000 194.2618
                  42.1888 22.5000
                                                                            FractionLength: 0
   0.0000 0.0000 144.8919 -37.0943
   0.0000 -0.0000 -0.0000 94.3326
                                                                      Matrix R float :
   0.0000 0.0000 -0.0000
                           0.0000
                                                                        989.3190 -294.1660 320.8349 575.0704
   0.0000
           0.0000
                   0.0000
                           0.0000
                                                                         -0.0000 777.0472 168.7551 89.9999
  -0.0000
           0.0000
                   0.0000
                           0.0000
                                                                          0.0000 0.0000 579.5677 -148.3771
  -0.0000 0.0000
                  0.0000
                           -0.0000
                                                                          0.0000 -0.0000 -0.0000 377.3306
                                                                          0.0000
                                                                                  0.0000
                                                                                         -0.0000
                                                                                                  0.0000
Matrix R_fix :
                                                                          0.0000
                                                                                  0.0000
                                                                                          0.0000
                                                                                                  0.0000
 248.0000 -74.2500 79.7500 143.0000
                                                                         -0.0000
                                                                                 0.0000
                                                                                          0.0000
                                                                                                  0.0000
       0 195.2500
                  42.0000 22.7500
                                                                         -0.0000 0.0000
                                                                                          0.0000
               0 146.5000 -37.5000
       0
                       0 94,0000
                                                                      Matrix R_fix :
       0
               0
                       0
                               0
                                                                         992 -297 319
                                                                                        572
       0
               0
                       0
                                0
                                                                              781
                                                                                  168
                                                                          0
       0
               0
                       0
                                0
                                                                               0
                                                                                   586 -150
       0
               0
                       0
                                0
                                                                               0
                                                                                    0
                                                                                       376
                                                                          0
                                                                          0
                                                                               0
                                                                                    0
                                                                                         0
                                                                          0
                                                                               0
                                                                                    0
                                                                                         0
                                                                          0
                                                                               0
                                                                                    0
                                                                                    0
                                                                                         0
                                                                               DataTypeMode: Fixed-point: binary point scaling
```

Signedness: Signed WordLength: 12 FractionLength: 0

Matlab result

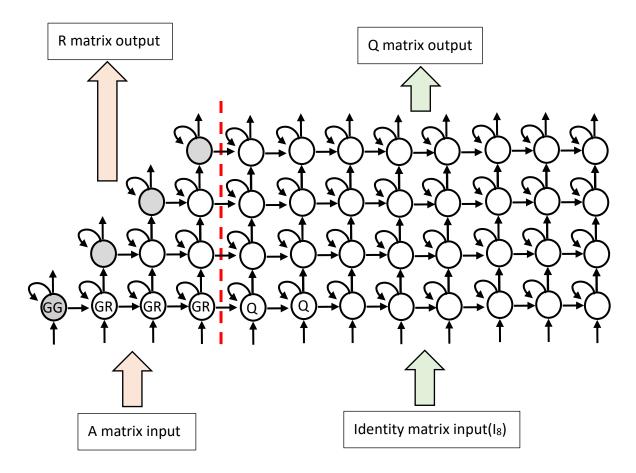
Record the values during iteration, which can be used for debugging in hardware implementation.

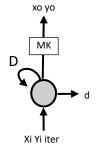
```
k = 1 \text{ row} 78:
d = 1 \ 1 \ -1 \ 1
GG1 Iteration 4 times: X = 594; Y = -5594
GR11 Iteration 4 times: X = 108; Y = 43
GR12 Iteration 4 times: X = 331; Y = -390
GR13 Iteration 4 times: X = 153; Y = 291
                                     0; Y =
Q11 Iteration 4 times: input: X =
                                                0 \text{ output: } X =
                                                                  0; Y =
Q12 Iteration 4 times: input: X =
                                     0: Y =
                                                0 \text{ output: } X =
                                                                  0: Y =
Q13 Iteration 4 times: input: X =
                                    0; Y =
                                                0 output: X =
                                                                  0: Y =
                                    0; Y =
Q14 Iteration 4 times: input: X =
                                               0 \text{ output: } X =
                                                                  0: Y =
Q15 Iteration 4 times: input: X =
                                     0; Y =
                                                0 output: X =
                                                                  0: Y =
                                    0; Y =
Q16 Iteration 4 times: input: X =
                                                0 \text{ output: } X =
                                                                  0: Y =
Q17 Iteration 4 times: input: X = -1024; Y =
                                                0 output: X = -720; Y = -1520
Q18 Iteration 4 times: input: X = 0; Y = -1024 output: X = 1520; Y = -720
 d = 1 - 1 - 1 - 1
 GG1 Iteration 8 times: X = 596; Y = 1596
 GR11 Iteration 8 times: X = 107; Y = 45
 GR12 Iteration 8 times: X = 334; Y = -388
 GR13 Iteration 8 times: X = 150; Y = 293
                                                 0 \text{ output: } X =
                                                                   0; Y =
 Q11 Iteration 8 times: input: X =
                                     0; Y =
 012 Iteration 8 times: input: X =
                                      0: Y =
                                                 0 output: X =
                                                                   0: Y =
                                                                              0
 Q13 Iteration 8 times: input: X =
                                     0; Y =
                                                 0 \text{ output: } X =
                                                                   0; Y =
                                      0; Y =
 014 Iteration 8 times: input: X =
                                                 0 output: X =
                                                                   0: Y =
                                                                              0
 Q15 Iteration 8 times: input: X =
                                      0; Y =
                                                  0 \text{ output: } X =
                                                                   0; Y =
                                                                              0
                                     0; Y =
                                                                   0; Y =
 Q16 Iteration 8 times: input: X =
                                                 0 \text{ output: } X =
 Q17 Iteration 8 times: input: X = -720; Y = -1520 output: X = -711; Y = -1528
 Q18 Iteration 8 times: input: X = 1520; Y = -720 output: X = 1528; Y = -708
 d = -1 \ 1 \ 0 \ 0
 GG1 Iteration 12 times: X = 597; Y = 0597
 GR11 Iteration 12 times: X = 107; Y = 45
 GR12 Iteration 12 times: X = 333; Y = -389
 GR13 Iteration 12 times: X = 151; Y = 293
 Q11 Iteration 12 times: input: X =
                                                                     0; Y =
                                                                                0
                                        0: Y =
                                                   0 output: X =
 Q12 Iteration 12 times: input: X =
                                        0; Y =
                                                    0 \text{ output: } X =
                                                                     0: Y =
                                                                                0
 Q13 Iteration 12 times: input: X =
                                      0; Y =
                                                   0 output: X =
                                                                     0; Y =
 Q14 Iteration 12 times: input: X =
                                        0; Y =
                                                   0 output: X =
                                                                     0: Y =
                                                                                0
 Q15 Iteration 12 times: input: X =
                                        0; Y =
                                                                     0; Y =
                                                   0 output: X =
                                                                                0
 Q16 Iteration 12 times: input: X =
                                        0; Y =
                                                   0 output: X =
                                                                     0; Y =
                                                                                0
 Q17 Iteration 12 times: input: X = -711; Y = -1528 output: X = -714; Y = -1527
 Q18 Iteration 12 times: input: X = 1528; Y = -708 output: X = 1527; Y = -711
  GG1 Multiplied by K: X = 362; Y = 0
  GR11 Multiplied by K:
                         X = -500; Y = -468
  GR12 Multiplied by K: X = -212; Y = 248
  GR13 Multiplied by K: X = -432; Y = 436
  Q11 Multiplied by K: X = 0; Y = 0
  Q12 Multiplied by K:
                        X = 0; Y = 0
  Q13 Multiplied by K: X = 0; Y = 0
  Q14 Multiplied by K: X = 0; Y = 0
  Q15 Multiplied by K: X = 0; Y = 0
  Q16 Multiplied by K: X = 0; Y = 0
  Q17 Multiplied by K:
                        X = -434; Y = -928
  Q18 Multiplied by K: X = 927; Y = -432
  k = 1 \text{ row}67:
```

```
k = 4 \text{ row}45
 d = -1 \ 1 \ -1 \ -1
 GG4 Iteration 4 times: X = 608; Y = 40608
 Q41 Iteration 4 times: input: X = -488; Y =
                                                 0 output: X = -618; Y = 511
 Q42 Iteration 4 times: input: X = 399; Y = -567 output: X = -89; Y = -1134
 Q43 Iteration 4 times: input: X = -62; Y = 213 output: X = 144; Y = 335
 Q44 Iteration 4 times: input: X = -411; Y = 233 output: X = -277; Y =
 Q45 Iteration 4 times: input: X = 96; Y = 397 output: X = 536; Y = 403
 Q46 Iteration 4 times: input: X = 49; Y = 233 output: X = 305; Y = 245
 Q47 Iteration 4 times: input: X = 402; Y = -577 output: X = -96; Y = -1151
 Q48 Iteration 4 times: input: X = -557; Y = -66 output: X = -775; Y = 499
 GG4 Iteration 8 times: X = 612; Y = -4612
 Q41 Iteration 8 times: input: X = -618; Y = 511 output: X = -582; Y = 555
 Q42 Iteration 8 times: input: X = -89; Y = -1134 output: X = -169; Y = -1129
 Q43 Iteration 8 times: input: X = 144; Y = 335 output: X = 167; Y = 324
 Q44 Iteration 8 times: input: X = -277; Y = 726 output: X = -225; Y =
 Q45 Iteration 8 times: input: X = 536; Y = 403 output: X = 565; Y =
 Q46 Iteration 8 times: input: X = 305; Y = 245 output: X = 323; Y = 223
Q47 Iteration 8 times: input: X = -96; Y = -1151 output: X = -177; Y = -1145
 Q48 Iteration 8 times: input: X = -775; Y = 499 output: X = -739; Y = 554
GG4 Iteration 12 times: X = 616; Y = -1616
Q41 Iteration 12 times: input: X = -582; Y = 555 output: X = -585; Y = 548
Q42 Iteration 12 times: input: X = -169; Y = -1129 output: X = -158; Y = -1133
Q43 Iteration 12 times: input: X = 167; Y = 324 output: X = 166; Y = 324
Q44 Iteration 12 times: input: X = -225; Y = 746 output: X = -228; Y =
Q45 Iteration 12 times: input: X = 565; Y = 365 output: X = 564; Y =
Q46 Iteration 12 times: input: X = 323; Y = 223 output: X = 323; Y = 224
Q47 Iteration 12 times: input: X = -177; Y = -1145 output: X = -166; Y = -1149
Q48 Iteration 12 times: input: X = -739; Y = 554 output: X = -742; Y = 547
GG4 Multiplied by K: X = 376; Y = -1
Q41 Multiplied by K: X = -356; Y = 330
Q42 Multiplied by K: X = -94; Y = -691
Q43 Multiplied by K: X = 100; Y = 196
Q44 Multiplied by K: X = -139; Y = 448
Q45 Multiplied by K: X = 342; Y = 223
Q46 Multiplied by K: X = 196; Y = 136
Q47 Multiplied by K: X = -99; Y = -701
Q48 Multiplied by K: X = -451; Y = 329
```

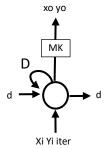
Hardware implementation result

1. Hardware architecture





GG(vectoring mode): One GG contains 4 micro-rotation modules, when iteration over, it outputs to above and multiplied by K(MK module), the rest of data will be transmitted to the right GR and Q modules.



GR(rotation mode): GR is almost the same module as GG, the only difference is rotation direction d, d will input from the left module(GG or GR).

2. Verilog code (only core part):

a. GG module

```
1 module GG_one_iter #(
 2
     parameter R LEN = 12,
 3
     parameter R FRAC = 2
 4)(
    input signed [R_LEN-1:0]
input signed [R_LEN-1:0]
 5
 6
                                      уi,
 7
     input
                        [3:0]
                                     iter,
 8
                         [1:0]
    output
                                     d,
9
     output reg signed [R LEN-1:0]
                                      xo,
     output reg signed [R_LEN-1:0]
10
11);
12
13 assign d = (yi == 0) ? 2 : xi[R_LEN-1] ^ yi[R_LEN-1];
14
15 always @(*) begin
    if(d == 2) begin
16
        xo = xi;
17
18
       yo = yi;
19
     end
20
    else if(d == 1) begin
21
       xo = xi - (yi >>> iter);
        yo = yi + (xi >>> iter);
22
23
     end
     else begin
24
25
       xo = xi + (yi >>> iter);
        yo = yi - (xi >>> iter);
26
27
     end
28 end
29
30 endmodule
```

b. GR module

```
1 module GR_one_iter #(
 2
     parameter R LEN = 12,
 3
     parameter R FRAC = 2
 4)
 5 (
    input signed [R_LEN-1:0] xi,
     input signed [R_LEN-1:0] yi,
 6
 7
    input
                       [3:0]
                                   iter,
 8
    input
                       [1:0]
                                  d,
 9
    output reg signed [R_LEN-1:0]
                                    XO,
     output reg signed [R_LEN-1:0]
10
11);
12
13 always @(*) begin
    if(d == 2) begin
14
15
       xo = xi;
16
       yo = yi;
17
    end
18
    else if(d == 1) begin
19
       xo = xi - (yi >>> iter);
20
       yo = yi + (xi >>> iter);
21
    end
22
     else begin
23
       xo = xi + (yi >>> iter);
24
       yo = yi - (xi >>> iter);
25
26 end
27
28 endmodule
```

c. Q module is the same as GR

d. MK (multiplied by K)

```
1 module MK #(
 2
     parameter R_LEN = 12,
 3
    parameter R_FRAC = 2,
 4
    parameter K LEN = 10,
 5
     parameter K_FRAC = 9
 6)(
 7
     input signed [R LEN-1:0]
                                       хi,
 8
    input
               signed [R_LEN-1:0]
                                        yi,
    output signed [R_LEN-1:0]
 9
                                        XO,
10
                signed [R_LEN-1:0]
     output
                                         уо
11);
12
13 localparam signed K = 10'b0 100110111; // K = 0.607421875
14
15 wire
               signed [R_LEN+K_LEN-1:0] xo_0;
16 wire
                signed [R LEN+K LEN-1:0] yo 0;
17
18
19 assign xo 0 = xi * K;
20 assign yo_0 = yi * K;
21
22 //truncate to R_LEN bits
23 assign x0 = \{x0 \ 0 \ [R \ LEN+K \ LEN-1], x0 \ 0 \ [R \ LEN+K \ FRAC-2:K \ FRAC]\};
24 assign yo = {yo 0[R LEN+K LEN-1], yo 0[R LEN+K FRAC-2:K FRAC]};
25
26 endmodule
27
```

```
1 always @ (posedge clk or posedge rst) begin
 2
      if (rst) begin
 3
         iter gg1 <= 'd0;
 4
      end
 5
      else if(ROT wire) begin
 6
        if(nop gg1) begin
 7
             iter gg1 <= 'd0;
 8
         end
 9
         else if(iter_last_gg1) begin
10
            iter gg1 <= iter gg1 + 'd1;
11
         end
12
         else begin
13
            iter_gg1 <= iter_gg1 + ITER_ONE_CYCLE;</pre>
14
         end
15
      end
16
     else begin
17
        iter gg1 <= 'd0;
18
      end
19 end
20
21 // GG1 input data xi, yi
22 always @(posedge clk or posedge rst) begin
23
      if (rst) begin
24
        xi gg1 <= 'd0;
25
        yi gg1 <= 'd0;
26
      end
27
      else if(OP wire) begin
28
        case(iter gg1)
29
             0: begin
30
                if(start gg1) begin
31
                   xi gg1 <= 'd0;
32
                   yi gg1 <= rd A data ext;
33
34
                else if(nop gg1 && !finish gg1) begin
35
                   xi_gg1 <= rd_A_data_ext;</pre>
                   yi_gg1 <= yo_gg1;</pre>
36
37
                end
38
                else begin
39
                   xi_gg1 \le xo_gg1;
40
                   yi gg1 <= yo gg1;
41
                end
42
             end
43
             ITER K: begin
44
                if(finish gg1) begin
45
                    xi_gg1 <= xo_gg1;</pre>
```

```
46
                   yi_gg1 <= yo_gg1;</pre>
47
                end
48
                else begin
49
                  xi_gg1 <= rd_A_data_ext;</pre>
50
                   yi_gg1 \le xo_mk1;
51
                end
52
            end
53
             default: begin
54
               xi gg1 <= xo gg1;
55
               yi_gg1 <= yo_gg1;</pre>
56
             end
57
        endcase
58
     end
59
      else begin
60
        xi_gg1 <= 'd0;
61
        yi_gg1 <= 'd0;
62
      end
63 end
64
65 // GG1 mk_count
66 always @(posedge clk or posedge rst) begin
67
     if (rst) begin
68
        mk count gg1 <= 'd0;
69
      end
70
      else if(multk_gg1) begin
71
        mk count gg1 <= mk count gg1 + 'd1;
72
      end
73 end
```

f. GR iteration control

```
1// GR11 current iteration number
 2 always @ (posedge clk or posedge rst) begin
 3
     if (rst) begin
 4
        iter gr11 <= 'd0;
 5
       nop_gr11 <= 'd0;
 6
        d1 gr11 <= 'd0;
 7
        d2 gr11
                  <= 'd0;
 8
        d3 gr11 <= 'd0;
 9
        d4_gr11
                  <= 'd0;
10
        neg_gr11 <= 'd0;
11
        mk count gr11 <= 'd0;
12
     end
13
     else begin
        iter gr11 <= iter gg1;</pre>
14
15
        nop_gr11 <= nop_gg1;</pre>
16
        d1 gr11 <= d1 gg1;
17
        d2 gr11 <= d2 gg1;
18
        d3_gr11
                  <= d3_gg1;
19
        d4 gr11
                  <= d4 gg1;
        neg_gr11 <= neg_gg1;</pre>
20
21
        mk count gr11 <= mk count gg1;
22
     end
23 end
24
25 // GR11 input data xi, yi
26 always @ (posedge clk or posedge rst) begin
27
     if (rst) begin
28
        xi gr11 <= 'd0;
        yi_gr11 <= 'd0;
29
30
     end
31
     else if(OP wire) begin
32
        case(iter gr11)
33
            0: begin
               if(start gr11_reg) begin
34
                  xi_gr11 <= 'd0;
35
                  yi gr11 <= rd A data ext;
36
37
               end
38
               else if(nop gr11 && !finish gr11) begin
39
                  xi gr11 <= rd A data ext;
                  yi gr11 <= yo gr11;
40
41
               end
42
               else begin
43
                  xi gr11 <= xo gr11;
44
                  yi gr11 <= yo gr11;
45
               end
```

```
46
             end
47
             ITER_K: begin
48
                if(finish gr11) begin
49
                   xi_gr11 \le xo_mk1;
50
                    yi_gr11 <= yo_mk1;</pre>
51
                end
52
                else begin
53
                   xi_gr11 <= rd_A_data_ext;</pre>
54
                   yi gr11 <= xo mk1;
55
                end
56
             end
57
             default: begin
58
                xi_gr11 <= xo_gr11;
59
                yi_gr11 <= yo_gr11;</pre>
60
             end
61
         endcase
62
      end
63
      else begin
64
        xi_gr11 <= 'd0;
65
        xi_gr11 <= 'd0;
66
67 end
```

3. Simulation result

- a. simulation waveform
- Data propagate form left to right PE(GG, GR, Q)

€ 1+	Msgs																
<pre>/qr_cordic_tb/clk</pre>	0	سسا	ww	ww	mm	MM	ww	ww	ww	l	ww	ww	ww	nnn	mm	MM	MM
<pre>/qr_cordic_tb/rst</pre>	0	L															
<pre></pre>	0	-(0	X_X	(82		(135)		() (71	(<u>)</u>		(1070)	(1080					
	0	-(0)	() (12) X X (•		911) (11	13 () (() -4:	20		
	0	-(0						X	(0)			7) (() 1151	(-187	
	0	0) (0	\Box	742	(881			X = X
+- / /qr_cordic_tb/qr_cordic_inst/xi_gr11	0	0			(454	(625							(-420				
+- /qr_cordic_tb/qr_cordic_inst/xi_gr12	0	0	X_X	$x \times x \times x$	(510	() (89		169 X X		X X X			25				
	0	0	X		X X X-3	50 () (768					<u> </u>		42			
- /qr_cordic_tb/qr_cordic_inst/xi_gr21	0	0				1110		679	26) (-29			510 ()		-187		
+- / /qr_cordic_tb/qr_cordic_inst/xi_gr22	0	0			<u> </u>	1 10		X-417 X					[-1]		.495		
+- /qr_cordic_tb/qr_cordic_inst/xi_gr31	0	0							0 X			229) (∬ ∏-125		186	
- /qr_cordic_tb/qr_cordic_inst/xi_mk1	0	0					XXX	بتييا					шш	0			
- /qr_cordic_tb/qr_cordic_inst/xi_mk1_q	0	<u> </u>						1 10 1		للحليل	بحجيب		шш		ĭ		
	0	0						تتتا	ببي	XO X		11 10	بببي		(0		
- /qr_cordic_tb/qr_cordic_inst/xi_mk2_q	0	0								_	110		0 11	1 10 1		_	
- /qr_cordic_tb/qr_cordic_inst/xi_mk3	0	0									1 10	1 1 10			10 1	χ χο	
- /qr_cordic_tb/qr_cordic_inst/xi_mk3_q	0	0						X	1 1 10	للحلا	تحجب		шц	بتت		χo	
+ /qr_cordic_tb/qr_cordic_inst/xi_mk4	0	0										<u> </u>)	10	1 10	1 10
□ 🖚 dar cordic th/ar cordic inst/xi mk4 a	0	-(n										ľľn	YY	ľn ľ	l Y Y Y Y	YYY	ľn

Process matrix R

→ /qr_cordic_tb/qr_cordic_inst/xi_q11	0	{0
<pre></pre>	0	{0
/qr_cordic_tb/qr_cordic_inst/xi_q13	0	(0 X X X-1., X X X X X X X X X X X-227 X X X-173 X X X 173 X 0
+ /qr_cordic_tb/qr_cordic_inst/xi_q14	0	-{O
- /qr_cordic_tb/qr_cordic_inst/xi_q15	0	(0
- /qr_cordic_tb/qr_cordic_inst/xi_q16	0	(O
- /qr_cordic_tb/qr_cordic_inst/xi_q17	0	(0
- /qr_cordic_tb/qr_cordic_inst/xi_q 18	0	(O X X X X X X V V
- /qr_cordic_tb/qr_cordic_inst/xi_q21	0	(0
- /qr_cordic_tb/qr_cordic_inst/xi_q22	0	{0
- /qr_cordic_tb/qr_cordic_inst/xi_q23	0	(O
-/ /qr_cordic_tb/qr_cordic_inst/xi_q24	0	(O
- /qr_cordic_tb/qr_cordic_inst/xi_q25	0	(0
- /qr_cordic_tb/qr_cordic_inst/xi_q26	0	(0
- /qr_cordic_tb/qr_cordic_inst/xi_q27	0	(0)
- /qr_cordic_tb/qr_cordic_inst/xi_q28	0	(0
- /qr_cordic_tb/qr_cordic_inst/xi_q31	0	(O
-/- /qr_cordic_tb/qr_cordic_inst/xi_q32	0	(0
-/- /qr_cordic_tb/qr_cordic_inst/xi_q33	0	(0
. — 4 /ar cordic th/ar cordic inst/xi a34	0	\{\text{r} \\ \text{1} \\ \text{1} \\ \text{1} \\ \text{1} \\ \text{2} \\ \text{1} \\ \text{2} \\ \text{2} \\ \text{3} \\ \text{2} \\ \text{3} \\ \text{2} \\ \text{4} \\ \text{4} \\ \text{2} \\ \text{3} \\ \text{4} \\ \tex
A STA	725 00	

Process matrix Q

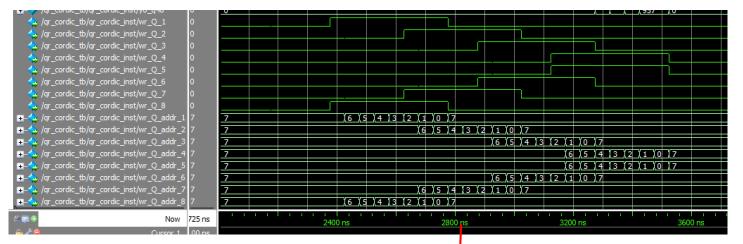
- Trocess matrix &		
<u>P</u> +	Msgs	
	0	-{0
+-// /qr_cordic_tb/qr_cordic_inst/yo_q12	0	-{0
/ /qr_cordic_tb/qr_cordic_inst/yo_q13	0	
	0	-{o
+	0	<u> </u>
+	0	<u> </u>
+	0	<u> </u>
-/-/ /qr_cordic_tb/qr_cordic_inst/yo_q18	0	
-/ /qr_cordic_tb/qr_cordic_inst/yo_q21	0	(0)(495)()(-1)()()()()()()()()()()()()()()()()()(
/ /qr_cordic_tb/qr_cordic_inst/yo_q22	0	-(0
/qr_cordic_tb/qr_cordic_inst/yo_q23	0	1
+	0	(0
+- / /qr_cordic_tb/qr_cordic_inst/yo_q26	0	7777 7777 70
+-1/ /qr_cordic_tb/qr_cordic_inst/yo_q27	0	
+-\(\frac{1}{2} \) /qr_cordic_tb/qr_cordic_inst/yo_q28	o	
+- / /qr_cordic_tb/qr_cordic_inst/yo_q31	o	- X-849 XXXX XXX XXXX XXX XXX XX
	0	(0) (-384) (1) (1) (-69) (1) (1) (1) (1)
	0	(0) (425 (1) (1) (1) (1) (1) (1) (1) (1) (1) (1)
/> /qr_cordic_tb/qr_cordic_inst/yo_q34	0	<u>-(0)()()())()(851)()()(0)(</u>
+	0	-{o
/-// /qr_cordic_tb/qr_cordic_inst/yo_q36	0	
	0	-{o
<u> </u>	^	

Data flow & data scheduling

timing diagram

GG1		N	N	N	N	78	3 78	3 7	8 7	8 N	1 6	7 6	7 6	7 6	7	N S	56	56	56	56	N	45	45	45	45	N :	34 3	34 3	34 3	34	N i	23	23 2	23	23	N	12	12	12	12	N								\top	T		
GR11			N	N	N	N	78	3 7	8 7	8 7	8 N	1 6	7 6	7 6	7 6	7	N :	56	56	56	56	N	45	45	45	45	N 3	34 3	34	34	34	N	23 2	23	23	23	N i	12	12	12	12	N										
GR12				N	N	N	N	7	8 7	8 7	8 7	8 N	1 6	7 6	7 6	7 6	57	N	56	56	56	56	N	45	45	45	45	N 3	34	34	34	34	N Z	23	23	23	23	N I	12	12	12	12	N									
GR13	Т				N	N	N	I N	V 7	8 7	8 7	8 7	8 1	V 6	7 6	7 6	57 (67	N	56	56	56	56	N	45	45	45	15]	N i	34	34	34	34	N i	23	23	23 2	23	N										Т			
MK1										k	K	F	ζ 1	ζ]	K [K	K	K		K	K	K	K		K	K	K 1	K		K	K	K	K		K	K :	K :	K		K	K	K	K								
Q11						N	N	I	I N						N e	7 6	57 (67	67	N	56	56	56	56	N	45	45	15 4	15	N :	34	34	34	34	N	23	23 2	23 2	23	N												
Q12	Т						N	I	I N	1 1	1 7	8 7	8 7	8 7	8	N (57 (67	67	67	N	56	56	56	56	N	45	15 4	15	45	N :	34	34	34	34	N Z	23 2	23 2	23	23	N	12	12	12	12	N						
Q13								N	I N	1 1	I	1 7	8 7	8 7	8 7	8	N (67	67	67	67	N	56	56	56	56	N 4	15 4	15	45	45	N	34 3	34	34	34	N 2	23 2	23	23	23	N	12	12	12	12	N					
Q14							Т	Т	N	1 1	1 1	1 1	V 7	8 7	8 7	8	78	N	67	67	67	67	N	56	56	56	56	N 4	15	45	45	45	N S	34	34	34	34	N 2	23	23	23	23	Ν	12	12	12	12	N				
Q15	П						Т	Т		N	1 1	I	1 1	V 7	8 7	8	78	78	N	67	67	67	67	N :	56	56	56	56	N 4	45	45	45	45	N :	34	34	34 3	34	N i	23	23	23	23	N	12	12	12	12	N			
Q16	Т						Т	Т	Т	Т	N	I	1 1	1	N 7	8	78	78	78	N	67	67	67	67	N	56	56	56 5	6	N .	45	45	45 4	15	N	34	34 3	34 3	34	N I	23	23	23	23	N	12	12	12	12	N		
Q17												1	1 1	N]	N]	N 7	78	78	78	78	N	67	67	67	67	N :	56	56 5	66	56	N 4	45	45 4	45	45	N :	34 3	34 3	34	34	N	23	23	23	23	N	12	12	12	12	N	
Q18													1	N]	N I	N I	N	78	78	78	78	N	67	67	67	67	N :	56 5	66	56	56	N	45 4	45	45	45	N 3	34 3	34	34	34	N	23	23	23	23	N	12	12	12	12	N
MK1_Q												I	I						K	K	K	K		K	K	K	K]	K	K	K	K		K	K	K	K		K	K	K	K		K	K	K	K		K	K	K	K

Write Q matrix data back



Each row has an independent write enable signal, since multiple data outputs from Q occur simultaneously in the systolic array.

Timing diagram

11	12	13	14	15	16	17	18														
				21	22	23	24	25	26	27	28										
									31	32	33	34	35	36	37	38					
														41	42	43	44	45	46	47	48
														51	52	53	54	55	56	57	58
									61	62	63	64	65	66	67	68					
				71	72	73	74	75	76	77	78										
81	82	83	84	85	86	87	88														
																					F

b. RTL simulation

Pattern 1:

START!!! S	imulation s	Start						
Toput A ma	triv.							
Input A ma	96	43	71					
- 105	4	49	44					
-60	113	-111	-127					
-89 -57	35 117	-63 -71	26 -29					
-16	-67	42	106					
6	45	88	-128					
-11	-54	-40	-10					
Output R m	atrix gold	en patter	n:					
656	-420	256	-42 -495					
Θ	756 0	-187 699	-495 186					
Ö	ő	0	758					
Θ								
Θ Θ	0	0 0	0 0					
Θ	9	0	0					
R matrix c	alculated	result:						
656	-420 756	256 -187	-42 -495					
0 0	/56 0	-187 699	-495 186					
Θ			758					
Θ	0	0	0					
0 0	0 0	Θ Θ	0 0					
9	0	0	0					
Output 0 m	atrix gold	n natter	n·					
-126	-658	-377	-565	-362	- 106	34	-70	
-452	-342	403	-124	440	-424	261	-332	
-418 567	440 123	-409 345	-194 81	-165 160	175 263	571 -667	-307 -197	
581	72	-234	29	-465	-79	-667 43	654	
Θ	532	77	-587	-51	-491	-418	-11	
0	0	631	-272 -508	-333 586	563 456	- 109 109	-372	
0 matrix c	0 alculated	0 result:	-508	586	456	109	487	
-126	-658	-377	-565	-362	- 106	34	-70	
-452 -418	-342 440	403 -409	- 124 - 194	440 - 165	-424 175	261 571	-332 -307	
-418 567	123	345	81	160	263	-667	-307 -197	
581	72	-234	29	-465	-79	43	654	
0	532	77	-587	-51	-491	-418	-11	
Θ	0 0	631 0	-272 -508	-333 586	563 456	- 109 109	-372 487	
, i				333		200		
******	******	 ********	S U M M		*******	*******	*******	***
								**
** Cong	ratulations ratulations	s!! Q mat	rix data	have been	n generate	d success	fully!	**
	********** simulation				******	*****	******	**
	finish at			ass				**
*****	*****	******	*****	******	******	******	******	***
	Congret	lations		<u></u> / 0.0	, ,			
	Congratu	car cons !		/ 0.0	´			
		on PASS!!		/^ ^ ^ \				
				^ ^ ^ ^	W			
				\mm_	-1-1			
	11			. 1				
\$finish ca	lled from : simulation	rile "qr_ n time	cordic_tb	o.v", line 3725000				
	VCS S	imul	ation					
Time: 3725								

Pattern 2:

```
Input A matrix:
-101 69
-100 110
-112 121
-25 -79
-14 -93
-35 50
67 -104
32 6
  Output R matrix golden

806 -739 -
0 648
0 0 0
0 0
0 0
0 0
0 0
0 0
0 0
R matrix calculated res
                                                                      pattern:
-247
-21
455
0
0
0
                                                                                                   366
181
268
593
0
0
 -247
-21
-21
455
0
0
0
                                                                                                   366
181
268
593
0
0
Output Q matrix golden pattern:
-514 -510 -571 -
-148 117 124 -
225 -575 -346 -
156 -175 170 -
-833 103 -401 -
0 -646 234
0 0 0 -595 -
0 Q matrix calculated result:
-514 -510 -571 -
-148 117 124 -
225 -575 -346 -
156 -175 170 -
-833 103 -401 -
0 0 -646 234
0 0 -595 -
0 0 0 -595 -
0 0 0 -595 -
                                                                                                                           -75
-673
322
555
29
-365
70
-199
-75
-673
322
555
29
-365
70
-199
                                                                                                                                                                                    349
-267
230
-344
167
244
777
42
                                                                                                -130
-650
-346
-372
-366
369
-248
-186
                                                                                                                                                                                                               164
216
-262
276
117
268
137
-851
                                                                                                                                                                                     349
-267
230
-344
167
244
777
42
  SUMMARY
           Congratulations!! R matrix data have been generated successfully!
Congratulations!! Q matrix data have been generated successfully!

The simulation results are all Pass!!
Get finish at cycle: 67
                         -- Congratulations !! -- / 0.0
-- Simulation PASS!! -- /^^^\
\m__m_
  $finish called from file "gr_cordic_tb.v", line 233.
$finish at simulation time 3725000
    V C S S i m u l a t i o n R e p o r t
Time: 3725000 ps
CPU Time: 2.290 seconds; Data structure size: 10.2Mb
```

Pattern 3: Pattern4:

```
START!!! Simulation Start .....
        -6
77
-70
-1
102
19
88
61
                                     123
68
20
109
20
-124
-98
92
295
-429
111
476
0
0
0
Output Q matrix golden

-33 436 -

-135 -465 -

-558 144

28 -45 -

-855 -6 -6 -6 -787 -
                                                   -5
-618
263
-507
-92
-376
262
-357
                                                                                 207
-463
-813
240
197
-136
81
                                 739
0
result:
                                                                  571
50
99
-57
-52
-298
385
677
                                                    -5
-618
263
-507
-92
-376
262
-357
                       436
-465
144
                                                                                                493
218
-347
222
213
-90
400
-615
                                                                                                             341
487
529
-222
-418
15
-323
-277
 ------ S U M M A R Y
         $finish called from file "qr_cordic_tb.v", line 233.
$finish at simulation time 3725000
V C S S i m u l a t i o n R e p o r t
Time: 3725000 ps
CPU Time: 2.460 seconds; Data structure si
                                                       Data structure size: 10.2Mb
```

```
START!!! Simulation Start .....
                                                     -84
-75
103
44
-9
105
-102
62
 R matrix calculated result:

875 0 -65

0 847 -774

0 0 462
                                                      462
0
0
0
0
Output Q matrix golden pattern:
-459 584 47
-327 391 -499 -
-270 -66 77 -
-260 214 281
-772 130 -365
0 693 74
0 0 759
0 0 0
Q matrix calculated result:
-459 584 47
-327 391 -499 -
-270 -66 77 -
-260 214 281
-772 130 -365
0 693 74
0 0 759
0 0 0
                                                                        239
-406
-254
549
39
103
-85
667
                                                                                                                                        -110
26
-879
-103
-349
263
219
-186
                                                                           239
-406
-254
549
39
103
-85
667
                                                                                                                                        -110
26
-879
-103
-349
263
219
-186
                                                                                               319
-482
-238
-409
 ** Congratulations!! R matrix data have been generated successfully! **

** Congratulations!! Omatrix data have been generated successfully! **

** The simulation results are all Pass!! **

** Get finish at cycle: 67
                   -- Congratulations !! --
  Data structure size: 10.2Mb
```

c. synthesis report (clock rate = 50ns)

i. timing report

```
perating Conditions: slow Library: slow
ire Load Model Mode: top
Qr_cordic tsmc13_w110

Point

clock clk (rise edge)
clock network delay (ideal)
yi_gg3_reg[0]/(K (DFFRX1)
yi_gg3_reg[0]/(K (DFFRX1)
yi_gg3_reg[0]/(X (DFFRX1)
yi_gg3_reg[0]/(X (DFFRX1)
yi_gg3_reg[0]/(X (DFFRX1)
yi_gg3_reg[0]/(X (DFFRX1)
yi_gg3_reg[0]/(X (DRFRX1)
yi_gg3_reg[0]/(X (DRFX1)
yi_gg3_re
```

ii. Area report

d. Gate-level simulation Pattern 1:

START!!! Simulation Start -20 -105 -60 -89 -57 96 4 113 35 117 -67 45 -54 43 49 -111 -63 -71 42 88 -40 71 44 -127 26 -29 106 -128 -10 Output R matrix golden 656 -420 0 756 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 R matrix calculated res pattern: 256 -187 186 758 0 0 0 matrix calculated result: -42 -495 186 758 0 0 0 699 Output Q matrix golden pattern: -126 -658 -377 -452 -342 403 -418 440 -409 -567 123 345 -581 72 -234 0 532 77 0 0 631 0 0 0 Q matrix calculated result: -126 -658 -377 -106 -424 175 263 -79 -491 563 456 -362 440 -165 160 -465 -51 -333 586 34 261 571 -667 43 -418 -109 109 -70 -332 -307 -197 654 -11 -372 487 -565 -124 -194 81 29 -587 -362 440 -165 160 -465 -51 34 261 571 -667 43 -418 -126 -452 -418 -70 -332 -307 -197 654 -11 -372 487 377 403 -658 -342 440 123 72 532 0 -409 345 -234 77 631 ** Congratulations!! Q matrix data have been generated successfully! ** ** Congratulations!! Q matrix data have been generated successfully! ** The simulation results are all Pass!! Get finish at cycle: 67 -- Congratulations !!

Pattern 2:

```
69
110
121
-79
-93
50
 pattern:
                                                                             366
181
268
593
0
0
 R matrix calculated result:

806 -739 -247
0 648 -21
0 0 455
0 0 50
0 0 0
0 0 0
0 0 0
Output Q matrix golden pattern:
-514 -510 -571 -
-148 117 124 -
225 -575 -346 -
156 -175 170 -
-833 103 -401 -
0 -646 234
0 0 0 -595 -
0 Q matrix calculated result:
-514 -510 -571 -
-148 117 124 -
225 -575 -346 -
156 -175 170 -
-833 103 -401 -
0 -646 234
0 0 -595 -
0 0 0 -
                                                                           -130
-650
-346
-372
-366
369
-248
-186
                                                                                                 -75
-673
322
555
29
-365
70
-199
                                                                                                                     -180
114
455
-592
-81
-421
-108
-499
                                                                                                                                             349
-267
230
-344
167
244
777
42
                                                                                                                     -180
114
455
-592
-81
-421
-108
                                                                           -130
-650
-346
-372
-366
369
-248
-186
                                                                                                                                                                 164
216
-262
276
117
268
137
-851
                                                                                                                                             349
-267
230
-344
167
244
777
  5 U M M A R Y
 ** Congratulations!! R matrix data have been generated successfully!

** Congratulations!! Q matrix data have been generated successfully!

*** The simulation results are all Pass!!

** Get finish at cycle: 67
```

Pattern 3: Pattern4:

```
START!!! Simulation Start .....
        -6
77
-70
-1
102
19
88
61
                                     123
68
20
109
20
-124
-98
92
295
-429
111
476
0
0
0
Output Q matrix golden

-33 436 -

-135 -465 -

-558 144

28 -45 -

-855 -6 -6 -6 -787 -
                                                   -5
-618
263
-507
-92
-376
262
-357
                                                                                 207
-463
-813
240
197
-136
81
                                 739
0
result:
                                                                  571
50
99
-57
-52
-298
385
677
                                                    -5
-618
263
-507
-92
-376
262
-357
                       436
-465
144
                                                                                                493
218
-347
222
213
-90
400
-615
                                                                                                             341
487
529
-222
-418
15
-323
-277
 ------ S U M M A R Y
         $finish called from file "qr_cordic_tb.v", line 233.
$finish at simulation time 3725000
V C S S i m u l a t i o n R e p o r t
Time: 3725000 ps
CPU Time: 2.460 seconds; Data structure si
                                                       Data structure size: 10.2Mb
```

```
START!!! Simulation Start .....
                                                     -84
-75
103
44
-9
105
-102
62
 R matrix calculated result:

875 0 -65

0 847 -774

0 0 462
                                                      462
0
0
0
0
Output Q matrix golden pattern:
-459 584 47
-327 391 -499 -
-270 -66 77 -
-260 214 281
-772 130 -365
0 693 74
0 0 759
0 0 0
Q matrix calculated result:
-459 584 47
-327 391 -499 -
-270 -66 77 -
-260 214 281
-772 130 -365
0 693 74
0 0 759
0 0 0
                                                                        239
-406
-254
549
39
103
-85
667
                                                                                                                                        -110
26
-879
-103
-349
263
219
-186
                                                                           239
-406
-254
549
39
103
-85
667
                                                                                                                                        -110
26
-879
-103
-349
263
219
-186
                                                                                               319
-482
-238
-409
 ** Congratulations!! R matrix data have been generated successfully! **

** Congratulations!! Omatrix data have been generated successfully! **

** The simulation results are all Pass!! **

** Get finish at cycle: 67
                   -- Congratulations !! --
  Data structure size: 10.2Mb
```