

$$I = \int_0^{2r} \arccos\left(\frac{x}{2r}\right) e^{\frac{-(x-0.5)^2}{2\sigma^2}} dx$$