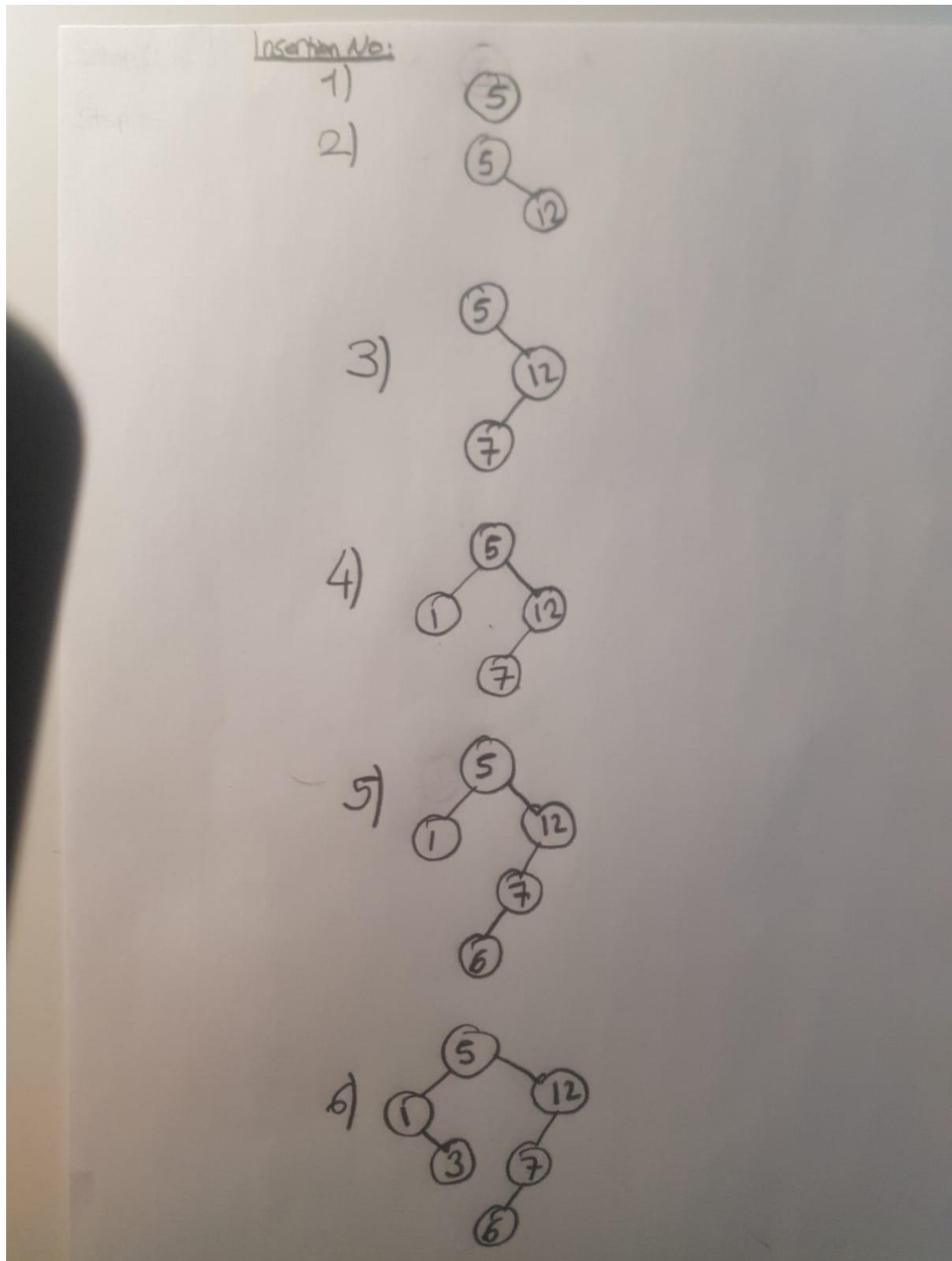


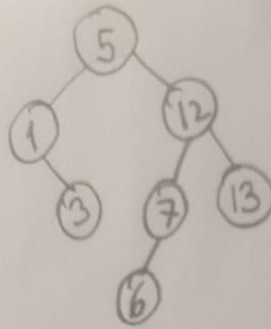
Name: Mehmet Bora Kurucu ID: 21703404 Section: 2

Q1A)

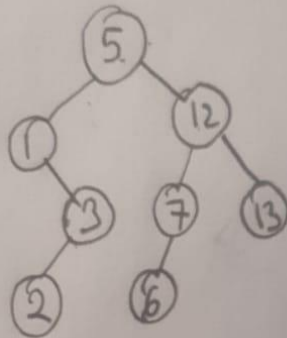


Insertion

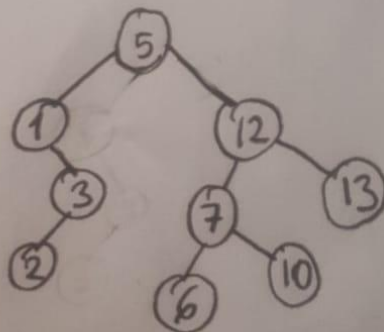
7)



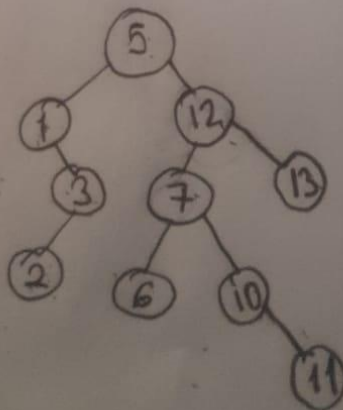
8)



9)



10)



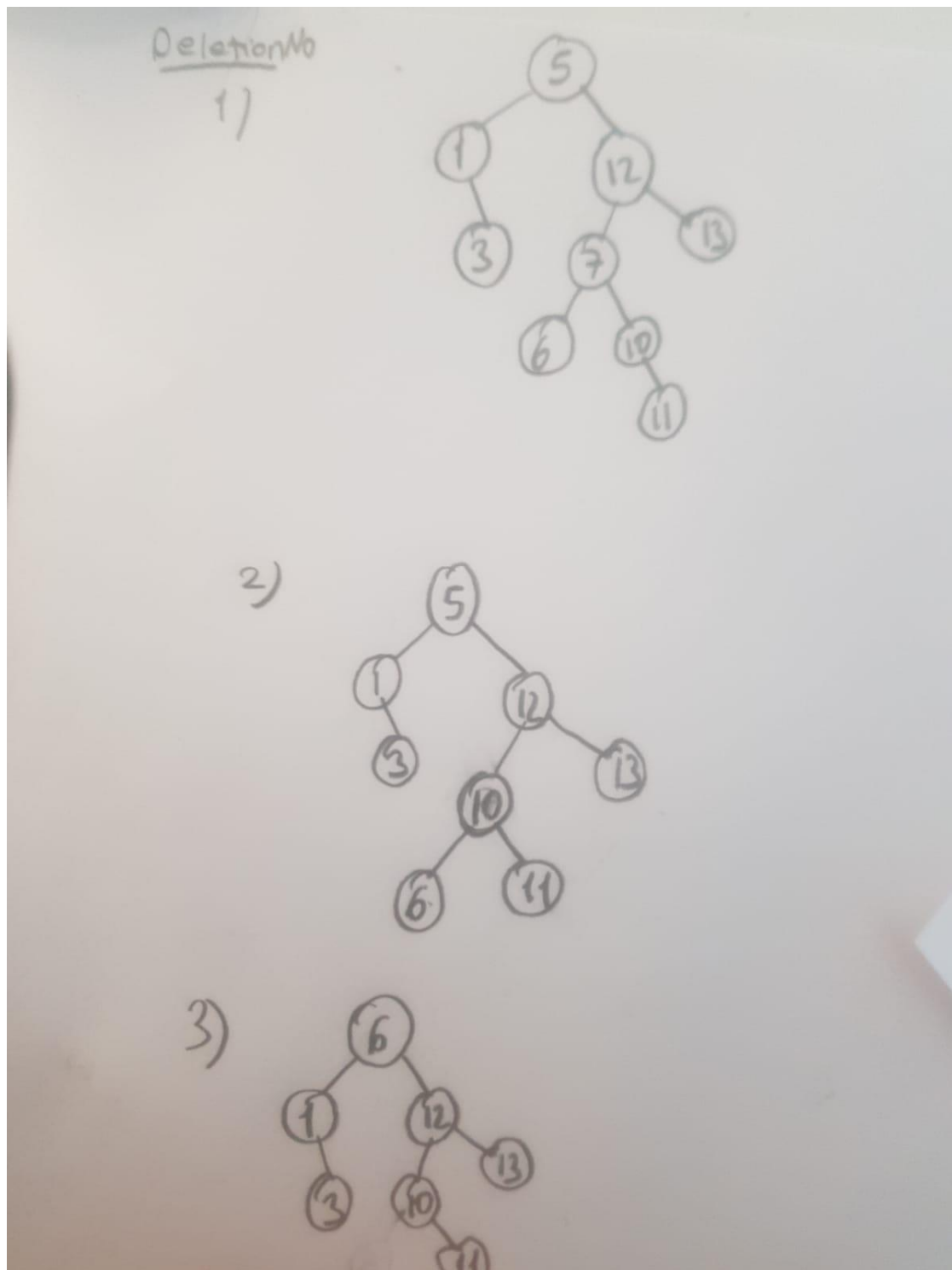
Q1B)

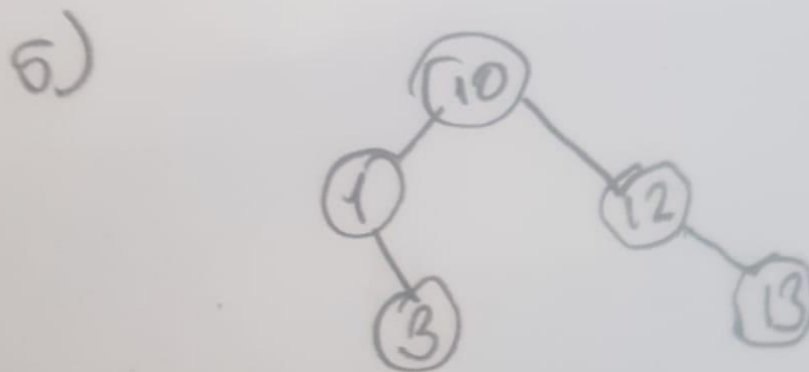
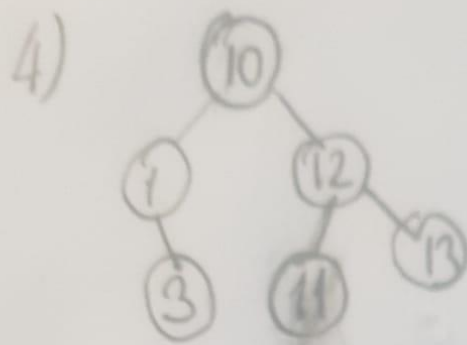
Inorder Traversal: 1 2 3 5 6 7 10 11 12 13

Preorder Traversal: 5 1 3 2 12 7 6 10 11 13

Postorder Traversal: 2 3 1 6 11 10 7 13 12 5

Q1C)





Q3)

insertItem(int key):

Calls void insertItem(BSTNode *& root,int key). Which finds proper place with recursion and inserts the item.

Average Time Complexity is when the function is considered as $T(n)=T(n/2)+1$. This is when it goes to one of the sides for most of the times. This can be represented as $T(n) = T(n/2^k) + k$, therefore $T(n)$ is $O(\log n)$.

Worst Time Complexity occurs when the list is linear. It becomes similar with the case of arrays it behaves like a linearly organized data structure. It scans the items one by one to find the target. Therefore the worst case becomes $O(n)$.

deleteItem(int key):

Calls void deleteItem(BSTNode *& root,int key). Which finds proper place with recursion and deletes the item according to it's children number.

Average Time Complexity is when the function is considered as $T(n)=T(n/2)+1$. This is when it goes to one of the sides for most of the times. This can be represented as $T(n) = T(n/2^k) + k$, therefore $T(n)$ is $O(\log n)$.

Worst Time Complexity occurs when the list is linear. It becomes similar with the case of arrays it behaves like a linearly organized data structure. It scans the items one by one to find the target. Therefore the worst case becomes $O(n)$.

retrieveItem(int key);

Calls void retrieveItem(BSTNode *& root,int key). Which finds proper place with recursion and retrieves the item.

Average Time Complexity is when the function is considered as $T(n)=T(n/2)+1$. This is when it goes to one of the sides for most of the times. $T(n) = T(n/2^k) + k$ then $T(n)$ is $O(\log n)$.

Worst Time Complexity occurs when the list is linear. It becomes similar with the case of arrays it behaves like a linearly organized data structure. It scans the items one by one to find the target. Therefore the worst case becomes $O(n)$.

inorderTraversal(int& length);

Calls void inorderTraversal(BSTNode * root,int& length,int *&arr,int &index) which does inorder traversal, simultaneously increases index and puts the values into array.

It is a traversal, it has to visit every node one time. So both Average Time Complexity and Worst Time Complexity is $O(n)$.

bool containsSequence(int* seq, int length);

Calls containsSequence(BSTNode * root,int* arr, int length) which find lowest common ancestor of array's last element and the tree This takes $O(\log n)$ in average(it goes to one of the subtrees), worst is $O(n)$ (if tree is linearly shaped).

After finding it, it calls traverseFromStart(BSTNode * root,int * arr,int &length,int &track) which checks if the array is a inorder subtree. This takes $O(\log n)$ in average(it goes to one of the

subtrees), worst is $O(n)$ (if tree is linearly shaped). To conclude Average Time Complexity of ContainsSequence is $O(\log n)$ and the Worst is $O(n)$.

int countNodesDeeperThan(int level);

It calls void countNodesDeeperThan(BSTNode * root,int level,int &count,int start), which makes a level order traversal until it reaches to the desired level, after that it does inorder traversal.

if level is dependent on n , for instance $n/2, 3n, n$:

Time complexity of the level order traversal would be $O(n^2)$ in both average or worst. Since they are $O(n)$ for inorder traversal, it would be $O(n^2)$ for both average and worst case.

Else:

Time complexity of level order is $O(1)$. So only inorder traversal is considered. Then both Average and Worst Time complexities are $O(n)$.

int maxBalancedHeight();

This function calls int calcHeight(BSTNode * root) which makes a postorder traversal, and decides the height according to the heights of its left and right subtrees. Since it is a traversal it visits every node, both average and worst case time complexities are $O(n)$.

int findLength(BSTNode * root);

Finds number of items by traversing the tree. Since it is a traversal it visits every node, both average and worst case time complexities are $O(n)$.

void printAr(int * arr,int length);

Prints the array. It is used to print the inorder traversal. If length is dependent on tree's size, in my usage it is, both tree and the array has n elements so both average and worst case time complexities are $O(n)$.

