Functional and logic programming
- **written exam -**

Important:
1. Subjects are graded as follows: By default - 1p; A – 2p; B - 4p; C - 3p.
2. Prolog problems will be resolved using SWI Prolog. The following are required: (1) explanation of the code and of the reasoning behind it; (2) recursive model that solves the problem, for all the predicates used; (3) specification of every predicate (parameters and their meaning, flow model, type of the predicate - deterministic/non-deterministic).
3. Lisp problems will be resolved using Common Lisp. The following are required: (1) explanation of the code and of the reasoning behind it; (2) recursive model that solves the problem, for each function used; (3) specification of every function (parameters and their meaning).

A. Given the following PROLOG predicate definition **f(list, integer),** with the flow model (i, o):

```
f([], -1):-!.
f([_|T], Rez):- f(T,S), S<1, !, Y is S+2.
f([H|T], Rez):- f(T,S), S<0, !, Y is S+H.
f([_|T], Rez):- f(T,S), Y is S.
```

Rewrite the definition in order to avoid the recursive call **f(T,S)** in all clauses. Do NOT redefine the predicate. Justify your answer.

B. Write a PROLOG program that generates the list of permutations of the set 1..N, having the property that the absolute value of the difference between 2 consecutive values from the permutation is >=2. Write the mathematical models and flow models for the predicates used. For example, for N=4 ⇒ [[3,1,4,2], [2,4,1,3]] (not necessarily in this order).

C. Write a Lisp function to substitute an element **e** by other element **e1** at all odd levels of a nonlinear list. The superficial level is assumed 1. **A MAP function shall be used.**
Example, for the list (1 d (2 d (d))), **e**=d and **e1**=f the result is (1 f (2 d (f))).