

Functional and logic programming

- written exam -

Important:

1. Subjects are graded as follows: By default - 1p; A – 2p; B - 4p; C - 3p.
2. Prolog problems will be resolved using SWI Prolog. The following are required: (1) explanation of the code and of the reasoning behind it; (2) recursive model that solves the problem, for all the predicates used; (3) specification of every predicate (parameters and their meaning, flow model, type of the predicate - deterministic/non-deterministic).
3. Lisp problems will be resolved using Common Lisp. The following are required: (1) explanation of the code and of the reasoning behind it; (2) recursive model that solves the problem, for each function used; (3) specification of every function (parameters and their meaning).

A. Given the following PROLOG predicate definition **f(integer, integer)**, with the flow model (i, o):

f(100, 1):-!.

f(K,X):-K1 is K+1, **f(K1,Y)**, Y>1, !, K2 is K1-1, X is K2+Y.

f(K,X):-K1 is K+1, **f(K1,Y)**, Y>0.5, !, X is Y.

f(K,X):-K1 is K+1, **f(K1,Y)**, X is Y-K1.

Rewrite the definition in order to avoid the recursive call **f(J,V)** in all clauses. Do NOT redefine the predicate. Justify your answer.

B. Write a PROLOG program that generates the list of all subsets of k elements in arithmetic progression. Write the mathematical models and flow models for the predicates used. For example, for $L=[1,5,2,9,3]$ and $k=3 \Rightarrow [[1,2,3],[1,5,9],[1,3,5]]$ (not necessarily in this order).

C. An n-ary tree is represented in Lisp as (node subtree1 subtree2 ...).. Write a function to return the list of nodes on even levels, in increasing level order (0, 2, ...). The root level is assumed zero. **A MAP function shall be used.**

Example for the tree (a (b (g)) (c (d (e (h))) (f))) => (a g d f h)