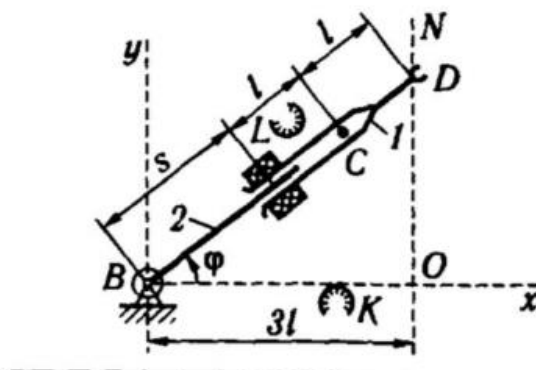


# Homework #5

Author: Guryev Boris

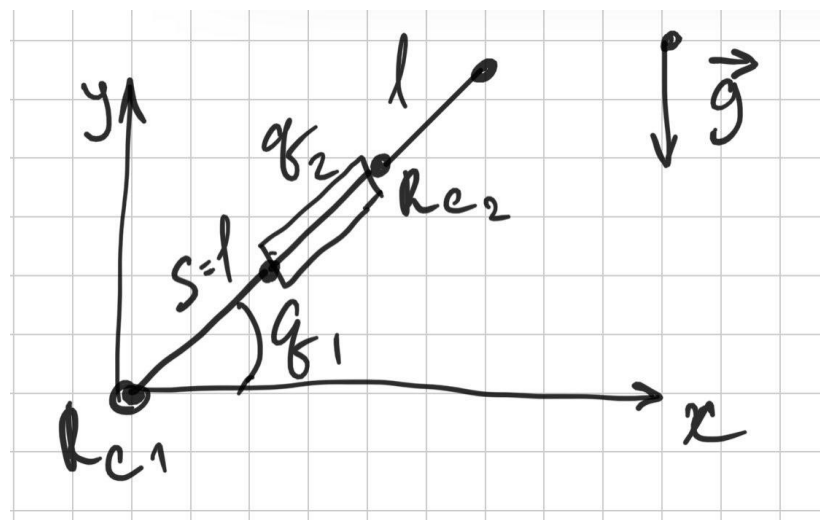
[Github link: github.com/BorisAnimal/RP-robot-dynamic](https://github.com/BorisAnimal/RP-robot-dynamic)

## Robot



$m_1 = 2 \text{ kg}$  (C – center mass)  
 $m_2 = 2 \text{ kg}$  (B – center mass)  
 $I_1 = 1 \text{ kg} \cdot \text{m}^2$   
 $I_2 = 2 \text{ kg} \cdot \text{m}^2$   
 $L = 0,2 \text{ m}$

For simplicity, I reordered joint's numeration. Also, watching schema, I decided that  $S = l_1$  and  $l_1$  is fixed. That means the distance right after  $l_1$  that follows to  $R_{c2}$  is the variable parameter  $q_2$  (prismatic joint, #2). Resulting schema looks like:



Consequently, I got following values for keypoints:

$$O_{c1} = [0, 0, 0]^T$$

$$O_1 = [s \cos(q_1), s \sin(q_1), 0]^T$$

$$O_{c2} = [(s + q_2) \cos(q_1), (s + q_2) \sin(q_1), 0]^T$$

## Lagrange solution

$$D =$$

$$\begin{pmatrix} m_2 q_2^2 + 2 m_2 q_2 s + m_2 s^2 + I_1 + I_2 & 0 \\ 0 & m_2 \end{pmatrix}$$

$$G =$$

$$\begin{pmatrix} g m_2 \cos(q_1) (q_2 + s) \\ g m_2 \sin(q_1) \end{pmatrix}$$

$$C =$$

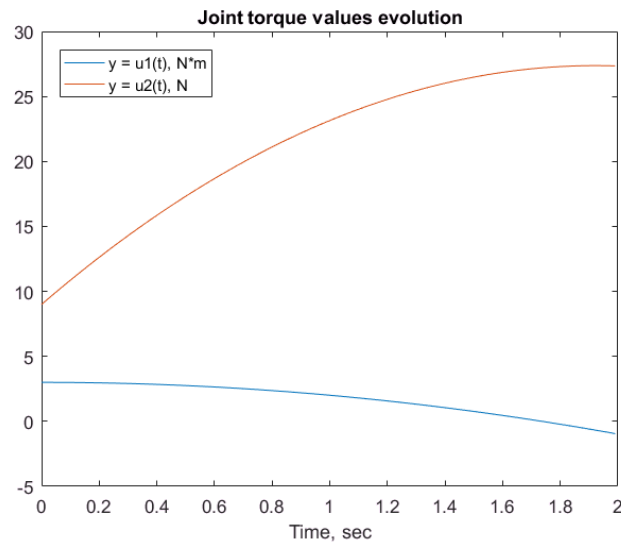
$$\begin{pmatrix} dq_2 m_2 (q_2 + s) & dq_1 m_2 (q_2 + s) \\ -dq_1 m_2 (q_2 + s) & 0 \end{pmatrix}$$

$$\text{tor} = D * q'' + C * q' + G$$

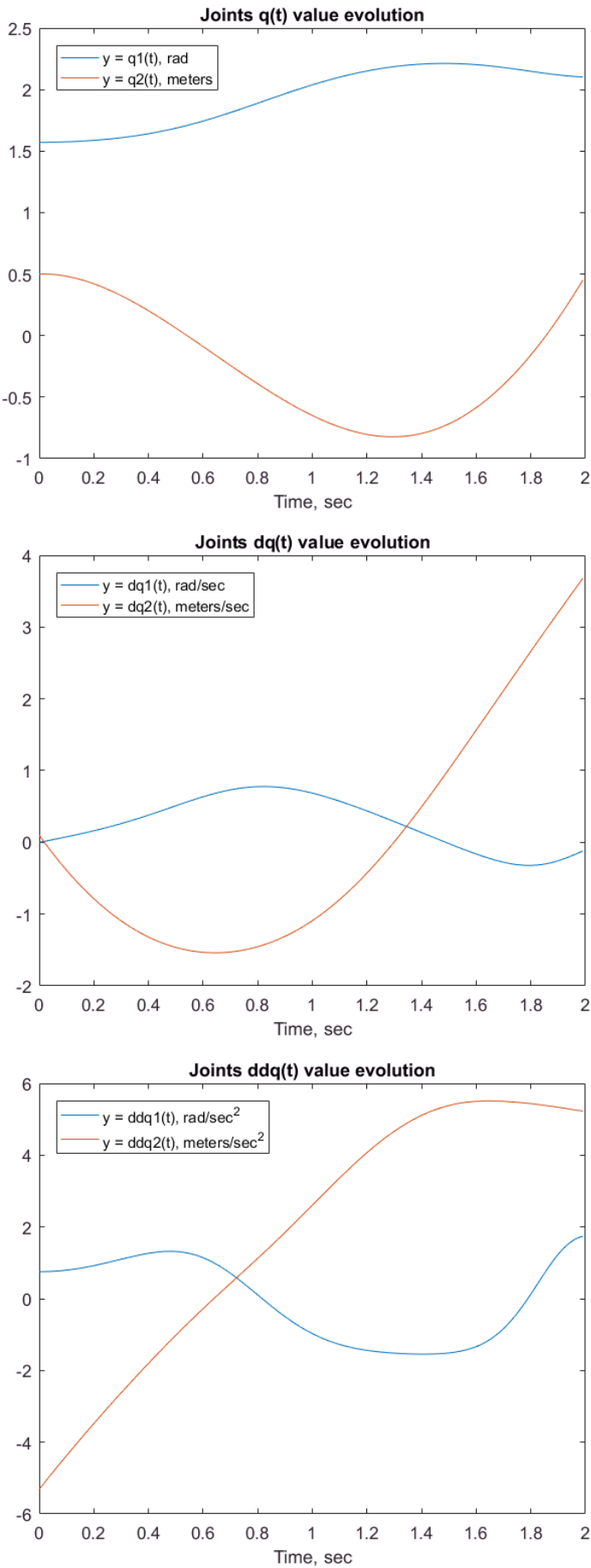
$$\text{tor} =$$

$$\begin{pmatrix} ddq_1 (m_2 q_2^2 + 2 m_2 q_2 s + m_2 s^2 + I_1 + I_2) + g m_2 \cos(q_1) (q_2 + s) + 2 dq_1 dq_2 m_2 (q_2 + s) \\ - m_2 (q_2 + s) dq_1^2 + ddq_2 m_2 + g m_2 \sin(q_1) \end{pmatrix}$$

To test this equations, I used numerical expression for  $q$ ,  $q'$ ,  $q''$  and used  $u(t)$  values as follow:



And the motion of joints performed



Considered model not include friction energy loss and joint limits, so result of  $q_2$  easily limited to extreme values.