

DEFINITION 1 (Penalty(s)): When applying an enhancement to change product  $p$  to  $p'$ , there is a penalty function to measure the change, which is

$$\text{Penalty}(p') = \frac{\sqrt{(p' - p)^2}}{|p|}$$

PROBLEM 1 (Find the enhancement strategy  $s$  to fulfill  $C$  with minimal penalty): Given a target region  $C$ , where  $C \supseteq c$ , an enhanced  $p'$  should dominate  $p$  with the modified region  $c'$  satisfies  $C \subseteq c'$ , while making least penalty. In other words, to:

$$\min. \text{Penalty}(p') \quad (1)$$

$$s.t. \text{Rank}(C) \leq k \quad (2)$$