

# **Aggregate Effects of Firing Costs with Endogenous Firm Productivity Growth**

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# Introduction

- Firing cost may generate important **TFP losses**. Two channels:
  1. Static effects: worse allocation of labor **given** a firm-productivity distribution.  
**Distorting hiring and firing choices**
  2. Dynamic effects: shift in the firm-productivity distribution.  
**Higher cost of failure reduce incentives to grow**

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  - Productivity distribution is typically exogenous
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- I quantify the aggregate effects of firing costs accounting for the two channels.

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- **What I do:** Quantify the aggregate implications of firing costs accounting for the two channels
- **How I do it:** Extend the framework in [Hopenhayn and Rogerson \(1993\)](#).
  - Endogenous firm-productivity dynamics
    - Firms can invest resources in affecting tomorrow's productivity ("innovation")
    - "Control-cost" approach: innovation modeled as prob.
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# Preview of results

- Firing costs equivalent to 2.5 monthly wages generates a **3% loss in TFP**
  - Losses raise to 11% if firing costs of 1 year wages
  - **Hopenhayn and Rogerson (1993)** find 2.1% loss from the same level of firing costs

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  - Losses raise to 11% if firing costs of 1 year wages
  - **Hopenhayn and Rogerson (1993)** find 2.1% loss from the same level of firing costs
- **Decomposition** of TFP losses:
  - 55% due to distortion in hiring/firing choices (standard misallocation channel)
  - 22% due to a lower average firm productivity
  - 23% due to the changing shape productivity distribution
- **Take-away**: models with exogenous productivity dynamics underestimate the aggregate implications of firing costs

# Related literature

- **Misallocation**

Hopenhayn and Rogerson (1993), Guner et al. (2008), Restuccia and Rogerson (2008), Hsieh and Klenow (2009), Bartelsman et al. (2013), Hsieh and Klenow (2014), García-Santana et al. (2016)

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- **Frictions with endogenous productivity distribution**

Bhattacharya et al. (2013), Gabler and Poschke (2013), Da-Rocha et al. (2019), López-Martín (2013), Mukoyama and Osotimehin (2019)

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- **“Control-cost” in macroeconomics**

Costain (2017), Turen (2018), Costain et al. (2019)

- **Contribution:** use the “control-cost” approach to model firm innovation

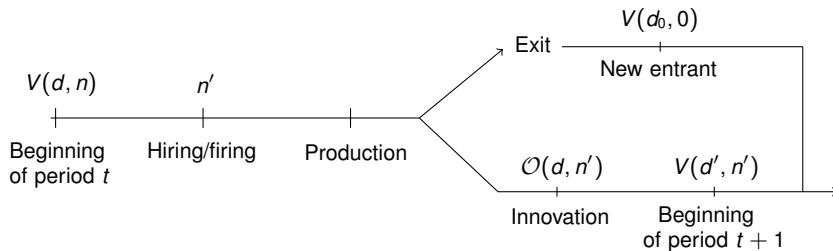
Model

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# Model setup

- I take Hopenhayn and Rogerson (1993) as the **building block**:
  - Representative household: consumption & labor supply
  - Continuum of heterogeneous firms: productivity ( $d$ ) and labor ( $n$ ).
  - Decreasing returns to scale technology with labor as only input
  - Firing is costly:  $\kappa_F w$  per worker fired
  - Exogenous exit: replaced by entrant, with  $E(d_0) = 1$  and  $V(d_0) = \sigma_0^2$ .
- + **Endogenous productivity dynamics**: “innovation”
  - Intensive and extensive margin
  - Firm choices affect the whole distribution of  $d'$ : growth vs. risk
  - Model firm choices as probability distributions: “control-cost”

# Timeline





# Firms

$$V(d, n) = \max_{n'} \underbrace{\Pi(d, n', n)}_{\text{Profits}} + \underbrace{\beta\delta V_E(n')}_{\text{Exit}} + \underbrace{\beta(1 - \delta)\mathcal{O}(d, n')}_{\text{Innovation stage}}$$

- Profits given by:

$$\Pi(d, n', n) = Ae^d(n')^\gamma - wn' - \underbrace{w\kappa_F \max\{0, n - n'\}}_{\text{Firing costs}}$$

- Exogenous exit, prob  $\delta \in (0, 1) \rightarrow$  value of exit:  $V_E(n') = -\kappa_F wn'$ .
- $\mathcal{O}(d, n)$  is the value at the innovation stage.

# Innovation

- Most models assume  $d \sim f(d)$ , but in reality:

$$d' \sim f\left(\underbrace{d, n}_{\text{State}}, \underbrace{x_1, x_2, \dots, x_N}_{\text{Firms actions}}\right) \equiv \mathcal{F}(d, n, X)$$

where  $X$  are total investments.

# Innovation

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where  $X$  are total investments.

- “Control-cost”: choices  $\equiv$  distribution over feasible alternatives.
  - I model  $\mathcal{F}$  indirectly: choose  $\mathcal{F}$  and define cost function for  $X$

$$X = \mathcal{D}(d, n, \mathcal{F})$$

- I divide innovation in two stages:
  - Extensive: Should we innovate?
  - Intensive: Which innovation should we implement?

# Innovation

- **Extensive margin:** Firms choose the probability of innovation  $\lambda$ 
  - Cost given by  $\kappa_I \mathcal{D}(\lambda | \bar{\lambda})$ .
  - $\bar{\lambda} \in (0, 1)$  is a default probability of innovation.
- **Intensive margin:** Firms choose the distribution of productivity  $\pi(d' | d, n)$ 
  - Cost given by  $\kappa_I \mathcal{D}(\pi | \eta)$ .
  - $\eta$  is a default distribution of next period's productivity, with

$$\sum_{i=1}^D \eta(d_i | d) d_i = d(1 - \mu) < d,$$

$\mu > 0$ : non-innovators expect their productivity to decrease

- **Non-innovators:** Productivity distributed according to  $\eta$ .

## Extensive margin

$$\mathcal{O}(d, n) = \max_{\lambda} \underbrace{\lambda \mathcal{O}'(d, n)}_{\text{Innovate}} + \underbrace{(1 - \lambda) \left( \sum_{i=1}^D \eta(d_i | d) V(d_i, n) \right)}_{\text{Not innovate}} - \kappa_I \mathcal{D}(\lambda | \bar{\lambda})$$

- Cost function given by the Kullback-Leibler divergence between  $\lambda$  and  $\bar{\lambda}$ :

$$\mathcal{D}(\lambda | \bar{\lambda}) = \lambda \log \left( \frac{\lambda}{\bar{\lambda}} \right) + (1 - \lambda) \log \left( \frac{1 - \lambda}{1 - \bar{\lambda}} \right)$$

Closed-form solution:

$$\lambda(d, n) = \frac{\bar{\lambda} \exp \left( \kappa_I^{-1} \mathcal{O}'(d, n) \right)}{\bar{\lambda} \exp \left( \kappa_I^{-1} \mathcal{O}'(d, n) \right) + (1 - \bar{\lambda}) \exp \left( \kappa_I^{-1} \mathcal{O}^N(d, n) \right)}$$

## Intensive margin

$$\mathcal{O}^I(d, n) = \max_{\pi} \sum_{i=1}^D \pi(d_i | d, n) V(d_i, n) - \kappa_I \mathcal{D}(\pi | \eta)$$

- Cost function given by Kullback-Leibler divergence btw  $\pi$  and  $\eta$

$$\mathcal{D}(\pi | \eta) = \sum_{i=1}^D \pi(d_i) \log \left( \frac{\pi(d_i)}{\eta(d_i)} \right)$$

Closed-form solution:

$$\pi(z | d, n) = \frac{\eta(z | d) \exp(\kappa_I^{-1} V(z, n))}{\sum_{i=1}^D \eta(d_i | d) \exp(\kappa_I^{-1} V(d_i, n))}$$

# Households

- Simplest household problem as in [Hopenhayn and Rogerson \(1993\)](#)

$$U = \max_{C,L} \ln C - \theta L, \quad \text{s.t. } C = wL + F + \Pi$$

$F \equiv$  aggregate firing costs,  $\Pi \equiv$  aggregate profits.

- First-order condition:

$$\frac{1}{wL + F + \Pi} = \theta \quad \rightarrow \quad w = \frac{\theta^{-1} - F - \Pi}{L}$$

- In the baseline equilibrium I set  $\theta$  such that  $w^* = 1$ .

## Calibration

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# Calibration

- Exogenous parameters:

$\beta = 1.05^{-1} \rightarrow$  Interest rate of 5%

$\delta = 7.56\% \rightarrow$  Average firm age of 9.7

$\gamma = 0.60 \rightarrow$  Standard value

$\psi = 0.50 \rightarrow$  Frisch elasticity of 2

- Data from Central de Balances from 2005 to 2007.

- Unbalanced panel of non-financial Spanish firms.
- Rich information from balance sheet and income statement

# Calibration

- Calibration of innovation  $(\mu, \sigma^2, \bar{\lambda}, \kappa_I)$ :
  - I lack data on innovation (what's innovation in this model?)
  - I follow Garcia-Macia, Hsieh and Klenow (2019) → use employment data.
  - Targets:
    - Firm size distribution
    - Volatility of employment
    - Share of hiring firms
    - Firing and hiring rate (firings/employment and hiring/employment)
- Other parameters:  $(A, \sigma_0^2, \kappa_F)$ . Targets:
  - Relative size entrants
  - Volatility of employment among entrants
  - Share of firing firms

## Calibration. Parameters

| Parameter       |   |      | Description   |
|-----------------|---|------|---|
| $A$             | = | 2.95 | Aggregate productivity term                         |
| $\sigma_0$      | = | 1.10 | Standard deviation of initial productivity draw     |
| $\mu$           | = | 0.07 | Depreciation of productivity (default distribution) |
| $\sigma$        | = | 0.30 | Standard deviation of shocks (default distribution) |
| $\kappa_0$      | = | 0.14 | Cost of innovation, level parameter                 |
| $\kappa_1$      | = | 1.25 | Cost of innovation, shape parameter                 |
| $\bar{\lambda}$ | = | 0.47 | Default probability of innovation                   |
| $\kappa_F$      | = | 0.20 | Firing cost   |

- Default law of motion of  $d$ :  $\log(d') = \log(d) - \hat{\mu} + \sigma\epsilon$  with  $\mu = \exp(\hat{\mu}) - 1$
- Cost of innovation:  $\kappa_I = \kappa_0 \exp(-\kappa_1 d)$

## Calibration. Model fit

| Moment   | Model | Data |
|--|-------|------|
| Average size of entrants                             | 3.53  | 3.40 |
| Coefficient of variation of firm size                | 1.21  | 1.19 |
| Coefficient of variation of firm size among entrants | 1.39  | 1.36 |
| Share of firing firms                                | 0.26  | 0.27 |
| Share of hiring firms                                | 0.35  | 0.34 |
| Firing rate among firing firms                       | 0.19  | 0.20 |
| Hiring rate among hiring firms                       | 0.44  | 0.44 |
| Share of firms with 0-5 workers                      | 0.63  | 0.60 |
| Share of firms with 6-10 workers                     | 0.21  | 0.20 |
| Share of firms with 11-15 workers                    | 0.07  | 0.08 |
| Share of firms with 16-20 workers                    | 0.04  | 0.04 |
| Share of firms with 21-25 workers                    | 0.02  | 0.02 |
| Share of firms with 25+ workers                      | 0.04  | 0.05 |

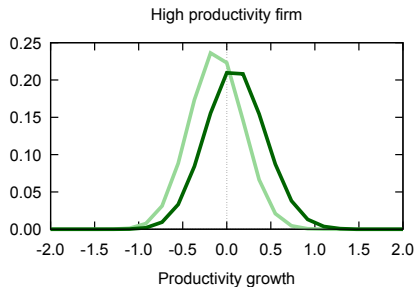
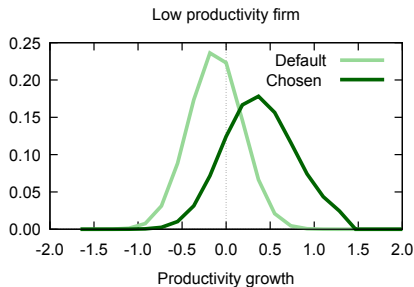
## Results

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# Results

1. Model evaluation: firm growth
2. Effects of firing costs.
3. Decomposing TFP losses from firing costs

# Model evaluation. Firm growth



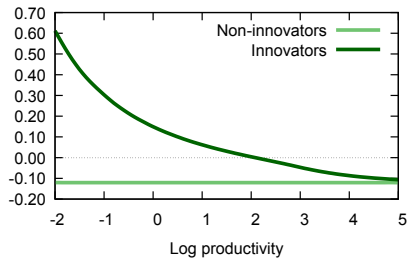
- Growth vs. risk trade-off
  - Low productivity firms expect to grow faster but take more risk
  - High productivity firms decrease their risk at the expense of productivity growth

▷ growth-risk

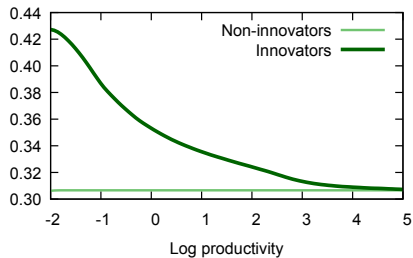
▷ growth-risk size

# Model evaluation. Innovation choices

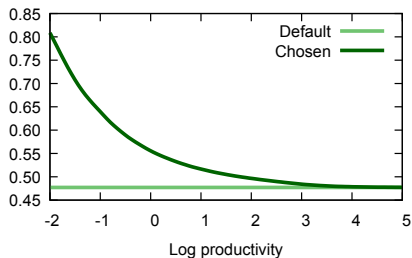
Expected growth rate



Std. deviation growth



Prob. of innovation





# Aggregate effects of firing costs

- Firing costs (may) lower aggregate productivity by distorting hiring/firing choices
  - Growing firms not hiring due to future potential adjustment costs
  - Shrinking firms not firing due to direct adjustment costs
- Firing costs increase the cost of failure:
  - Innovation is risky (and more so the more you want to grow)
  - Firing costs disincentives growth versus risk

# Aggregate effects of firing costs

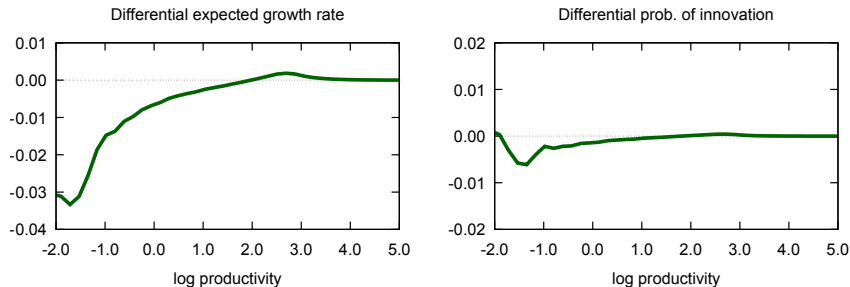
**Table:** Aggregate effects of firing cost (% fall relative to frictionless economy)

|                             | $\kappa_I = 0.20$<br>(2.5 month) | $\kappa_I = 0.40$<br>(5 months) | $\kappa_I = 1.00$<br>(1 year) |
|-----------------------------|----------------------------------|---------------------------------|-------------------------------|
| TFP                         | 3.01                             | 5.08                            | 10.6                          |
| Average productivity        | 1.82                             | 3.10                            | 6.54                          |
| Average productivity growth | 2.22                             | 3.76                            | 7.19                          |
| Innovation expenses         | 3.47                             | 5.86                            | 11.8                          |
| Output                      | 2.50                             | 4.54                            | 9.46                          |
| Employment                  | 2.55                             | 4.67                            | 9.67                          |
| Job destruction rate        | 52.5                             | 68.6                            | 85.7                          |
| Job creation rate           | 30.8                             | 40.3                            | 50.3                          |

▷ PE results

# Aggregate effects of firing costs

Figure: Innovation choices. Experiment,  $\kappa_F = 0.2$  vs.  $\kappa_F = 0$



$\triangleright \kappa_F = 1$

# Aggregate effects of firing costs. Decomposition I

- Olley and Pakes (1996) decomposition:

$$\text{TFP} = \bar{d} + \int_{x \in \mathcal{X}} \tilde{d}(x) \tilde{s}(x) d\mu(x) = \bar{d} + C(d, n)$$

- We can decompose TFP gains as:

$$\frac{\Delta \text{TFP}}{\text{TFP}} = \frac{\Delta \bar{d}}{\text{TFP}} + \frac{\Delta C(d, n)}{\text{TFP}}$$

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- We can decompose TFP gains as:

$$\begin{array}{rclcl} \frac{\Delta \text{TFP}}{\text{TFP}} & = & \frac{\Delta \bar{d}}{\text{TFP}} & + & \frac{\Delta C(d, n)}{\text{TFP}} \\ 3\% & = & 0.7\% & + & 2.3\% \\ & & (22\%) & & (78\%) \end{array}$$

- Changes in average firm productivity explain 22% of the fall in aggregate TFP.

## Aggregate effects of firing costs. Decomposition II

- Olley and Pakes (1996) allows us to disentangle the role of average productivity.
- However, innovation in the model drives the whole distribution of productivity.
- Simulate an economy with no innovation ( $\kappa_I \rightarrow 0$ ) and:

$$d' \sim \begin{cases} \pi(d, n | \kappa_F = 0) & \text{w.p. } \lambda(d, n | \kappa_F = 0) \\ \eta(d) & \text{w.p. } 1 - \lambda(d, n | \kappa_F = 0) \end{cases}$$

where  $\pi(d, n | \kappa_F = 0)$  and  $\lambda(d, n | \kappa_F = 0)$  are innovation choices in the frictionless economy.

$\Rightarrow$  innovation cannot respond to changes in firing costs

# Aggregate effects of firing costs. Decomposition II

Table: Aggregate effects of firing cost (% fall relative to frictionless economy)

|                         | Endogenous Inn. |      |      | Exogenous Inn. |      |      |
|-------------------------|-----------------|------|------|----------------|------|------|
|                         | 0.20            | 0.40 | 1.00 | 0.20           | 0.40 | 1.00 |
| Firing cost, $\kappa_F$ |                 |      |      |                |      |      |
| TFP                     | 3.01            | 5.08 | 10.6 | 1.68           | 2.73 | 5.52 |
| Average productivity    | 1.82            | 3.10 | 6.45 | 0.00           | 0.00 | 0.00 |
| Output                  | 2.50            | 4.54 | 9.46 | 1.74           | 3.38 | 7.05 |
| Employment              | 2.55            | 4.67 | 9.67 | 2.52           | 4.75 | 9.72 |
| Innovation expenses     | 3.47            | 5.86 | 11.8 | 0.00           | 0.00 | 0.00 |

- Endogenous innovation explain 45% of the overall fall in aggregate TFP.
  - 22% due to a decrease in average firm productivity
  - 23% due to changes in the shape of the productivity distribution

## Conclusions

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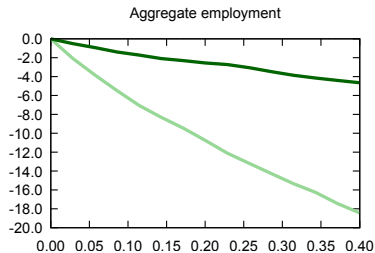
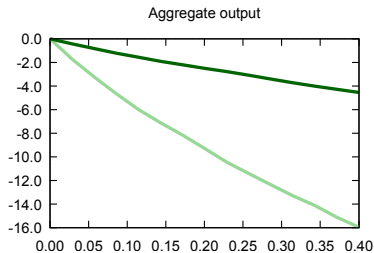
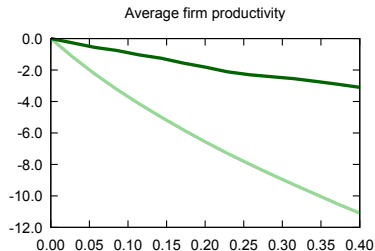
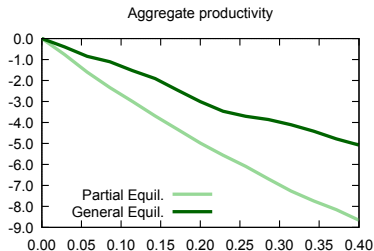
# Conclusions

- Build and calibrate a simple extension of **Hopenhayn and Rogerson (1993)**
  - Posit a flexible innovation technology.
  - Firms have partial control over the whole distribution of next period's distribution
- Firing cost of 2.5 monthly wages generate a 3% fall in aggregate productivity
  - Larger effects than typically found in the literature
  - Distort firing/hiring choices + shaping innovation choices
- Decomposition:
  - 55% due to distortion on hiring/firing choices
  - 22% due to a decrease in average firm productivity
  - 23% due to changes in the shape of the productivity distribution
- **Take-away**: exogenous productivity dynamics largely underestimates the productivity effects of frictions

Thanks for your attention

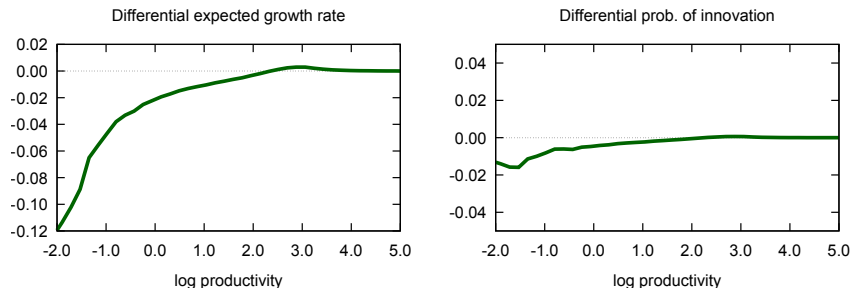
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# Effects of firing costs. GE vs. PE



# Aggregate effects of firing costs

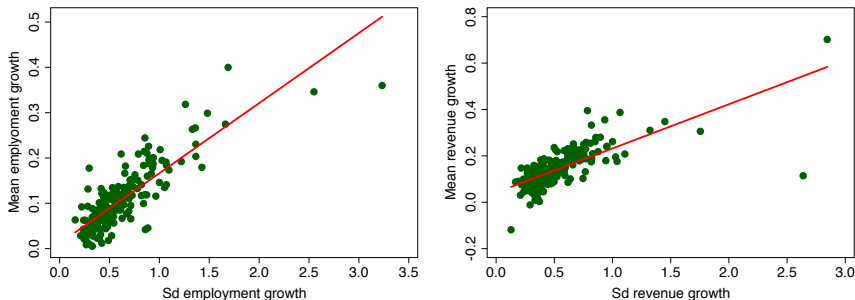
Figure: Innovation choices. Experiment,  $\kappa_F = 1$  vs.  $\kappa_F = 0$



▷ Back

# Growth vs. Risk Trade-off

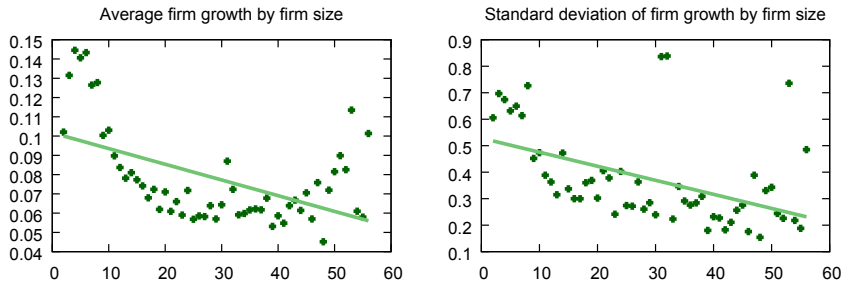
Figure: Sector-year average and standard deviation of employment/revenue growth



► Back

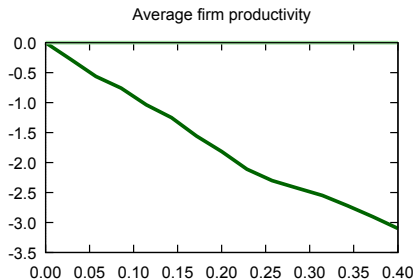
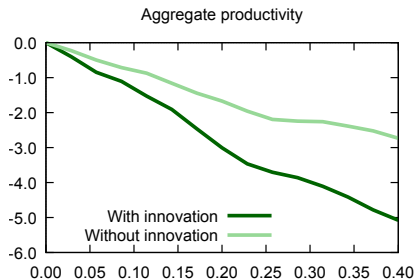
# Growth vs. Risk Trade-off. Firm Size

Figure: Sector-year average and standard deviation of employment/revenue growth



▷ Back

# Effects of firing costs. Endogenous vs. Exogenous innovation



► Back