Intergenerational Effects of Child-Related Tax Benefits in the US

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Introduction

- Very low fertility rates in developed countries
 - 1.2 in ITA & ESP, 1.4 in AUT, 1.7 in NOR, 1.8 in US, 1.9 in FRA & SWE
 - Increasing attention to pronatalist policies
 Neyer et al (2017) show that EU activities related to fertility relevant family policies have increased over time
 - Examples: paid parental leaves, subsidized childcare, tax benefits, transfers
 Björklund (2006), Erosa et al. (2010), González (2013), Bick (2016)
- Tax benefits are very extended across countries...
 - ... and very generous in the US: \$3,400 per family w/ children (Maag, 2013)
- · Little work on their effects



Tax Benefits in the US

Table: Average tax rate, married couples

| HH Income | Tax rate by # of children | | | | Benefits (2 kids) | |
|-----------------|---------------------------|------|------|------|-------------------|------|
| (× avg. income) | 0 | 1 | 2 | 3 | \$, 2005 | % |
| 0.50 | 0.06 | 0.05 | 0.02 | 0.00 | 1,791 | 0.68 |
| 1.00 | 0.14 | 0.11 | 0.09 | 0.08 | 3,536 | 0.30 |
| 1.50 | 0.18 | 0.16 | 0.15 | 0.14 | 3,778 | 0.16 |

Source: CPS data, 2000-2010.

- Lower and more progressive taxes for larger families
- Where are benefits coming from:
 - $^{\circ}\;$ Specific programs: Child Tax Credit, Child and Dependent Care Tax Credit
 - Others: Standard deduction, Personal Exemption, Earned Income Tax Credit

This Paper

- Quantify the impact of child-related tax benefits in the US tax system on fertility and intergenerational mobility within a GE framework
 - Life cycle model with overlapping generations of heterogeneous households
 - Fertility decisions and parental investments in children's human capital
 - Children's skill formation as in Cunha et al (2010)
 - Progressive taxes with child-related benefits

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 - Today's children will be tomorrow's parents: intergenerational effects
 - Demographic structure has GE implications

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- Why to use a GE framework?
 - Today's children will be tomorrow's parents: intergenerational effects
 - Demographic structure has GE implications
- Why to study effects on intergenerational mobility?
 - \circ Family Economics *meets* Macro \rightarrow *Who* have the children matters

Who have the children matters

- Parents in the US face a quantity-quality trade-off
 - Juhn, et al. (2015, 2018): arrival of a sibling decreases performance on cognitive tests, and the quantity-quality trade-off is stronger among low income mothers
- · As a result, high educated parents...
 - Have less children: 1.7 children, while HS mothers have 2.1 children (CPS)
 - Spend more time with their children: 12% more time (PSID-CDS)
 - Spend more money with their children: 30% more money (Daruich, 2018)

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· Therefore:

- (a) If tax benefits increase fertility, do they decrease children's human capital?
- (b) Are poor families more or less affected?
- (c) How do differences in initial conditions change?
 - Keane and Wolpin (1997), Hugget, et al. (2011): Large share of inequality explained by differences in initial conditions

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- Mechanism:
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 - Benefits are highly progressive: low income families are more affected
- Results decomposition: long-run effects are quantitatively important
- Can we foster fertility without damaging mobility? Education subsidies
 - Cheaper education breaks (to some extend) the quantity-quality trade-off
 - Regressive transfer: high-educated are more affected

Related Literature

Macro models with quantity-quality:

Caucutt et al. (2002), Restuccia and Urrutia (2004), Córdoba et al. (2016), Daruich and Kozlowski (2016), Sommer (2016), Lee and Seshadri (2018), Daruich (2018)

Contribution: policy & endogenous fertility, parental investments and transfers

· Fertility and Public Policy:

Milligan (2005), Björklund (2006), Baughman and Dickert-Conlin (2009), Azmat and González (2010), González (2013)

Contribution: macro framework (GE & intergenerational effects)

Erosa et al. (2010), Bick (2016)

Contribution: evaluation of tax benefits, parental investments

Today's talk

- 1. Model economy
- 2. Calibration
- 3. Policy evaluation
- 4. Conclusions

The Model

Main features

- Life-cycle economy with overlapping generations of married households
 - GE: Aggregate firm combines capital, low-educated labor and high-educated labor
 - o LC: childhood, working age (fertile & infertile ages), and retirement
- + Endogenous fertility and initial conditions (investments and transfer)
 - $^{\circ}$ College choice at independence \rightarrow depends on human capital
 - After college, random matching with marital sorting
- Individual heterogeneity: age, gender, education and productivity
 - o Spouses share assets, children and children's human capital

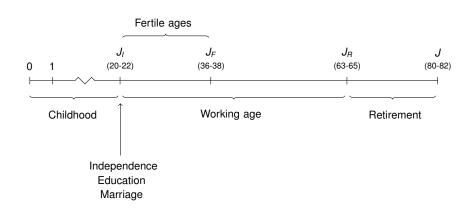
Main features

- Government taxes income to finance some (exogenous) expenditures
 - Tax rate function depends on income, y, and number of kids, n: Heathcote, Storesletten, and Violante (2017)

$$T(y,n) = t(y,n)y \Rightarrow t(y,n) = 1 - \lambda(n) \left(\frac{y}{\overline{y}}\right)^{-\tau(n)}$$

- \circ $\lambda(n)$ drives the level of taxes
- \circ $\tau(n)$ drives the degree of progressivity of taxes

Life-cycle structure



Childhood



• Children are born with an exogenous level of human capital q_0

Children's human capital exhibits dynamic complementarities
 Cunha et al. (2010), del Boca et al. (2014), Attanasio et al. (2017)

$$q' = \left[\mu \bar{q}^{\theta} + (1-\mu)\mathcal{I}(n,m,t)^{\theta} \right]^{\frac{1}{\theta}}$$

- $\circ \ ar{q}$ is the average human capital of children in the hh: $ar{q}=q+(q_0+q)rac{n_0}{n}$.
- \circ μ controls the persistence of human capital $\rightarrow \Delta q' = \alpha + \beta q + \epsilon$
- θ drives how parental investments affect human capital $\Delta q' = \alpha + \beta \ln y + \epsilon$

Childhood



• Parents invest time and money/goods, (t, m):

$$\mathcal{I}(n,m,t) = A_{\mathcal{I}} \left[\varsigma \left(\frac{m}{n^{\psi_1}} \right)^{\gamma} + (1-\varsigma) \left(\frac{t}{n^{\psi_2}} \right)^{\gamma} \right]^{\frac{1}{\gamma}}$$

- \circ $A_{\mathcal{I}}$ is a productivity parameter \rightarrow average growth of human capital
- \circ ς controls the relative weight of money investments \rightarrow ave. time investment
- \circ γ drives the ES between time and money o diff. in time investment
- $\circ \; \psi_{ extsf{1}}$ and $\psi_{ extsf{2}}$ captures economies of scale in time and money investments

Independence

- Initial state given by (gender, skills, assets) $\equiv (g, q, a)$.
 - o g from parental investments
 - o a from parental transfer
- · College choice:

$$E(g,q,a) = E_{\xi_{E}|q,a} \max \left\{ \overbrace{M(g,\overline{e},a)}^{\text{Value of CG}} - \underbrace{\xi_{E}(g,q)}_{\text{Effort cost}}, \overbrace{M(g,\underline{e},a)}^{\text{Value of HS}} \right\}$$

effort cost ξ_E , decreasing in human capital:

$$\ln \xi_E(g,q) \sim N(\mu_E(g,q),1), \quad \mu_E(g,q) = \mu_E^g \exp(-\mu_E^q q) \geq 0$$

• Then, meet spouse and begin adult life ightarrow sorting: $\operatorname{\mathsf{Prob}}(e_m = e_f) = p_M$

Adults



- Standard LC problem: consumption, savings and labor supply of spouses
- Wage rates given by age, gender, education and productivity:

$$\ln \omega(g,e,z,j) = \ln w(e) + \mu(g,e,j) + z_g$$

- ∘ w(e): wage rate per efficiency unit of time
- \circ $\mu(g, e, j)$: deterministic age-profile
- \circ z_q : labor productivity \rightarrow education-specific AR(1)
- Retirees: receive a pension and solve consumption-savings problem

Adults



Gender-specific utility function:

$$U_g(c, l_g, t) = \frac{c^{1-\sigma_c}}{1-\sigma_c} - \kappa_g \frac{(l_g + \frac{\alpha_g}{\alpha_g} t)^{1+\frac{1}{\psi}}}{1+\frac{1}{\psi}}$$

- $\circ \; \; \psi$ is the Frisch elasticity
- $\circ \ \alpha_g \in [0,1]$ captures the fraction of t spent by gender-g parent
- Household maximize joint utility: $U_m(c, I_m, t) + U_f(c, I_f, t)$

Fertile ages



- Fertile households make a pregnancy choice: $k \in \{0, 1\}$
 - Fertility risk: pregnant females have a newborn next period w.p. $p_0(j) \in [0, 1]$
 - \circ Labor productivity loss from childbirth: z_f falls by $\delta_0 \in (0,1)$
- Children stay at home until J_I:
 - While at home, parents invest time and money on their children's human capital
 - Stochastic independence: probability $p_l(n, j) \in [0, 1]$
 - ⇒ Parents make a transfer b to independent children
- · But... why do parents want to have children?
 - Parents derive utility from having kids, and from their kids' human capital

Why do parents have children?

$$U_k(n,q,b) = \eta_n \left(\frac{n^{\sigma_n}}{\sigma_n}\right) + \eta_q n^{\varphi} \left(\frac{q^{\sigma_q}}{\sigma_q}\right) + \eta_b \left(\frac{b^{\sigma_b}}{\sigma_b}\right) - \eta_0 \mathbf{1}\{n > 0\}$$

- Posit a utility function to capture intergenerational altruism:
 - where b is the amount of transfer to independent children
 - \circ η_0 is a fixed cost (example: quality of leisure) \to % childless
- Marginal utility from q increasing in number of children (if $\varphi > 0$).
 - $^{\circ}\,$ The lower the value of arphi the more costly it is to have another child in terms of q
 - $^{\circ}~arphi$ controls the magnitude of the q-q trade-off ightarrow Differential fertility

$$V(e_m, e_f, z_m, z_f, a, n, q, n_0, n_l, j) =$$

$$= \max_{\mathbf{x}} U_m(c, l_m, t) + U_f(c, l_f, t) + U_k(n', q', b) +$$

$$+ \beta E_j [V(e_m, e_f, z'_m, z'_f, a', n', q', n'_0, n'_l, j + 1)]$$

with
$$n' = n - n_l + n_0$$
 and $\mathbf{x} = (c, a', l_m, l_f, k, m, t, b)$

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$$n' = n - n_l + n_0$$
 and $\mathbf{x} = (c, a', l_m, l_f, k, m, t, b)$, and subject to

• Budget contraint:
$$a' + \Psi(n')c + m + b = y + (1+r)a - T(y,n') - \tau_{ss}y$$

with labor income given by $y = \omega_m(e_m,z_m,j)l_m + \omega_t(e_t,z_t-\delta_0n_0,j)l_t$

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- Time constraint: $I_g + \alpha_g t \in [0, 1]$

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- Time constraint: $I_g + \alpha_g t \in [0, 1]$
- Other constraints: k = 0 if $j > J_F$, m = t = 0 if n' = 0 and b = 0 if $n_l = 0$

Calibration

Data

- Panel Study of Income Dynamics (PSID)
 - Panel of US households. Use waves from 2001 to 2009 (biannual).
 - o Information on education, family structure, income.
- Child Development Supplement (CDS)
 - Supplementary study covering children aged 0 to 12 from 1997 PSID families.
 - I use the 2002 and 2007 waves: children aged 5 to 18.
 - Time diary and child's scores in three of the Woodcock Johnson Tests
- Current Population Survey (CPS)
 - · Large cross-section of US households.
 - o ASEC Supplement for the years 2000 to 2010
 - o Information on tax liabilities and income.

Calibration

- Measurement with CDS data: children's human capital & time investment
- Estimate directly from data:
 - Tax function: standard parametric function estimated with CPS data.
 - Income process: age profiles and labor productivity process from PSID.
 - Fertility risk as in Sommer (2016)
 - Children's independence: estimate transition probabilities from PSID.
- Set some parameters to standard values or from related papers.
- · Calibrate remaining parameters internally.

Measurement

· Time investments:

- CDS data contains a detailed time diary: nature and duration of activity, whether parents participate, etc.
- I define t as the total time parents actively participate in child's activity.

| | Time/day | % Share | |
|--------|----------|---------|--|
| Mother | 1h 6 min | 42% | |
| Father | 30 min | 19% | |
| Both | 1h 1m | 39% | |

Measurement

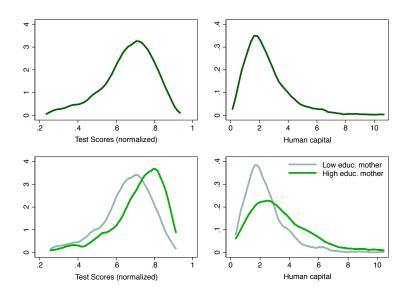
- Children's human capital:
 - CDS data contains children's scores in the Woodcock Johnson Tests.
 - Standard measure of child's skills
 Daruich (2018), Lee and Seshadri (2018), Del Boca et al. (2014)
 - Follow Del Boca et al. (2014): prob. of correct answer, $p_i(q) = q/(1+q)$.
 - Answer to question i is $d_i \in \{0, 1\}$, then:

$$\overline{d} = N^{-1} \sum_{i}^{N} d_{i} \quad \Rightarrow \quad q = \frac{\overline{d}}{1 - \overline{d}}$$

• Highly correlated with college graduation: Corr(e, q) = 0.482

 \triangleright Sample \triangleright Stats q \triangleright Age profile

Children's human capital



Tax function

Table: Parameters of the tax function

| Number of children | 0 | 1 | 2 | 3 |
|--|----------------|----------------|----------------|----------------|
| Level, λ Progressivity, $	au$ | 0.858 0.097 | 0.880 0.101 | 0.893 0.114 | 0.910 0.119 |
| Obs. (1,000) | 65.9 | 40.3 | 44.9 | 15.8 |

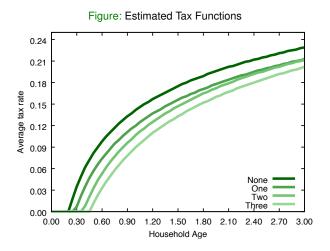
Note: standard errors are all less than 0.01. Tax rate computed as total tax liabilities before tax credits over total household income

· Parametric tax function:

Heathcote, Storesletten, and Violante (2017)

$$t(y, n) = 1 - \lambda(n) \left(\frac{y}{\overline{y}}\right)^{-\tau(n)}$$

Tax function





Aggregate production function

Standard function:

$$Y = AK^{\alpha}L^{1-\alpha}$$
, with $L = \left[aL_0^b + (1-a)L_1^b\right]^{\frac{1}{b}}$

where K is capital, L_0 is low-educated labor and L_1 is high-educated labor

- Set $\alpha = 0.33$ and choose parameters (A, a, b) such that:
 - Interest rate of 3% (annual)
 - Wage of low educated of 10 (normalization)
 - Relative wage of 1.28 (PSID)
- A = 47.9, a = 0.44, b = 0.65

Others

- Income process
 - Fit 2nd order polynomial in age by gender and education
 - Use residuals as measure of labor productivity: fit a AR(1) process.
- · Fertility risk
 - Follow Sommer (2016) (% of infertile females by age)

$$p_0(j) = 1 - \exp(\alpha_0 + \alpha_1 j)$$

- · Children independence
 - Estimate transition probabilities from the data

$$p_0(n,j) = \text{Prob}(n_{i,t} < n_{i,t-3} | n_{i,t-3} = n, \text{age} = j)$$



| Para | meter | Description | Source |
|--------------|-------|---------------------------------------|------------------------------|
| β | 0.98 | Discount factor (annual) | Standard value |
| σ_c | 0.80 | Curvature utility from consumption | Córdoba et al (2016) |
| ψ | 0.50 | Frisch elasticity of labor supply | Standard value |
| α_{m} | 0.54 | % time invested by fathers | CDS |
| α_f | 0.82 | % time invested by mothers | CDS |
| ξ1 | 0.92 | Economies of scale, money investments | Sommer (2016) |
| ξ2 | 0.54 | Economies of scale, time investments | Sommer (2016) |
| q_0 | 1.42 | Initial level of human capital | 25th percentile of q |
| δ_0 | 0.10 | Child penalty | Kleven et al. (2018) |
| p_R | 0.13 | Replacement rate | 50% labor supply, ages 62-65 |
| рм | 0.75 | Share of household with $e_m = e_f$ | PSID |

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- Calibrate 19 parameters using SMM.
 - Preference parameters.
 - Human capital technology and investment function.
 - College effort cost.
- · Targets key moments:
 - Fertility, child's human capital and time investments profiles by maternal education.
 - · Labor supply by gender.
 - o Dynamics of child's human capital.
 - Share of college graduates and elasticity of education to human capital.

Preferences

| Paran | neter | Description | Moment | Model | Data |
|------------|-------|--------------------------------|--|-------|-------|
| κ_m | 4.74 | Disutility labor, males | Average labor supply, male | 0.36 | 0.35 |
| κ_f | 4.32 | Disutility labor, females | Average labor supply, female | 0.24 | 0.23 |
| η_n | 1.05 | Utility n, weight | Completed fertility, HS mother | 2.41 | 2.52 |
| σ_n | 0.51 | Utility n, slope | % of households with 2+ children | 0.53 | 0.52 |
| η_q | 0.96 | Utility q, weight | Average human capital, HS mother | 2.75 | 2.67 |
| σ_q | 0.76 | Utility q, slope | Differential q by maternal educ. | 0.44 | 0.56 |
| φ | 0.16 | Utility q , fam. size param. | Differential fertility by maternal educ. | -0.26 | -0.23 |
| η_b | 0.40 | Utility from b, weight | Rel. wealth at age J_I , HS mother | 0.11 | 0.11 |
| σ_b | 0.51 | Utility from b, slope | Rel. wealth at age J_I , CG mother | 0.16 | 0.17 |
| η_0^0 | 2.70 | Fixed cost, HS mothers | % of childless HS mothers | 0.08 | 0.08 |
| η_0^1 | 2.80 | Fixed cost, CG mothers | % of childless CG mothers | 0.12 | 0.13 |

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| φ | 0.16 | Utility q , fam. size param. | Differential fertility by maternal educ. | -0.26 | -0.23 |
| η_b | 0.40 | Utility from b, weight | Rel. wealth at age J_I , HS mother | 0.11 | 0.11 |
| σ_b | 0.51 | Utility from b, slope | Rel. wealth at age J_I , CG mother | 0.16 | 0.17 |
| η_0^0 | 2.70 | Fixed cost, HS mothers | % of childless HS mothers | 0.08 | 0.08 |
| η_0^1 | 2.80 | Fixed cost, CG mothers | % of childless CG mothers | 0.12 | 0.13 |

Human capital, Investment and College choice

| Paran | neter | Description | Moment | Model | Data |
|---|-----------|-----------------------------|---|-------|------|
| Law c | of motion | of human capital: | | | |
| μ | 0.30 | Share parameter, q | Slope: $\Delta q = \alpha + \beta q + u$ | 0.22 | 0.25 |
| θ | -1.84 | Elasticity parameter | Slope: $\Delta q = \alpha + \beta \ln(y) + u$ | 0.18 | 0.14 |
| Inves | tment fun | ction: | | | |
| $A_{\mathcal{I}}$ | 6.31 | Productivity of investments | Average growth rate of q | 0.22 | 0.25 |
| ς | 0.58 | Share parameter, m | Time investment, HS mothers | 0.23 | 0.25 |
| γ | 0.31 | Elasticity parameter | Time investment, CG mothers | 0.25 | 0.28 |
| Colle | ge choice | <u> </u> | | | |
| $\mu_{\scriptscriptstyle F}^{\scriptscriptstyle f}$ | 0.96 | Fixed effort cost, females | Share of high educated females | 0.27 | 0.26 |
| $\mu_F^{\bar{m}}$ | 11.6 | Fixed effort cost, males | Share of high educated males | 0.29 | 0.27 |
| μ_E^f μ_E^m μ_E^1 | 0.23 | Variable cost of education | Slope of $e = \alpha + \beta q + u$ | 0.11 | 0.12 |

Human capital, Investment and College choice

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| Nontargeted moments Data Model Source | | | | |
|---------------------------------------|---------------------|------|-------|--------|
| Pata Model Source | Nontargeted moments | Data | Model | Source |

| Nontargeted moments | Data | Model | Source |
|--|------|-------|--------|
| Intergenerational persistence of education | 0.16 | 0.15 | PSID |

| Nontargeted moments | Data | Model | Source |
|--|-------|-------|--------|
| Intergenerational persistence of education | 0.16 | 0.15 | PSID |
| Income elasticity of fertility, HS mother | -0.21 | -0.17 | PSID |
| Income elasticity of fertility, CG mother | -0.02 | -0.01 | PSID |

| Nontargeted moments | Data | Model | Source |
|---|-------|-------|--------------------|
| Intergenerational persistence of education | 0.16 | 0.15 | PSID |
| Income elasticity of fertility, HS mother | -0.21 | -0.17 | PSID |
| Income elasticity of fertility, CG mother | -0.02 | -0.01 | PSID |
| Correlation time and goods investments | 0.88 | 0.87 | Daruich (2018) |
| Share of expenditures spent on children $(n = 1)$ | 0.26 | 0.22 | Lino et al. (2015) |
| Share of expenditures spent on children $(n = 2)$ | 0.39 | 0.39 | Lino et al. (2015) |

| Nontargeted moments | Data | Model | Source |
|---|-------|-------|--------------------|
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| Share of expenditures spent on children ($n = 2$) | 0.39 | 0.39 | Lino et al. (2015) |

| Replicating Spanish transfer policy * | Data | Model | Source |
|---------------------------------------|------|-------|-----------------|
| Fertility increase (%) | 6.32 | 7.50 | González (2013) |

 $^(^*)$ A universal transfer of 2.1 median female monthly income per birth. Spain 2007

Policy Evaluation

Policy Evaluation

- Question: what are the effects of child-related tax benefits?
 - On they increase fertility?
 - If so, do they generate a fall in human capital?
 - How is intergenerational mobility affected?
- Policy implementation: eliminate child-dependent benefits

$$t^*(y, n) = t(y, 0) - \frac{\tau_0}{2}$$

where $\tau_0 = 0.05$ is such that the policy is revenue neutral

$$\int_{\mathcal{S}} t(y,n)y(\mathbf{s})dF(\mathbf{s}) = \int_{\mathcal{S}} [t(y,0) - \tau_0]y(\mathbf{s})dF^*(\mathbf{s})$$

39

Aggregate effects

| | No Benefits | Tax Benefits (Baseline) | % Change |
|-------------------------|-------------|-------------------------|----------|
| Completed fertility | 1.81 | 2.11 | 16.3 |
| Fertility of mothers | 2.08 | 2.32 | 12.0 |
| Share of mothers | 0.87 | 0.91 | 3.82 |
| Human capital at J_l | 6.11 | 5.07 | -17.1 |
| College graduation rate | 0.37 | 0.28 | -25.0 |

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- Tax benefits are effective at fostering fertility. Two channels
 - o Effect (a): Benefits reduce the cost of children
 - Effect (b): ↑ Fertility → ↑ Labor share → ↓ K/L → ↓ Wages → ↑ Fertility
 Why? parents cannot afford sufficiently high level of human capital → more kids
- · Both intensive and extensive margin

Aggregate effects

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- But they decrease children's human capital...
 - o Families are now larger: lower productivity of parental investments
 - ⇒ Number of children is a key determinant of the cost of human capital
 - · Lower income: money investments relatively more expensive
- · Reduction in college graduation rate: higher effort cost

Heterogeneous effects

| | ŀ | High School | | | College Graduate | | | |
|------------------------|------|-------------|-------|------|------------------|-------|--|--|
| | No | Tax | % Chg | No | Tax | % Chg | | |
| Completed fertility | 1.86 | 2.21 | 18.8 | 1.74 | 1.90 | 8.74 | | |
| Fertility of mothers | 2.10 | 2.41 | 14.9 | 2.05 | 2.14 | 4.92 | | |
| Share of mothers | 0.90 | 0.92 | 3.41 | 0.86 | 0.88 | 3.63 | | |
| Human capital at J_i | 5.54 | 4.61 | -19.1 | 6.59 | 6.12 | -9.36 | | |
| College graduation | 0.30 | 0.23 | -29.1 | 0.41 | 0.39 | -12.3 | | |

Heterogeneous effects

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|------------------------|------|-------------|-------|------|------------------|-------|--|--|
| | No | Tax | % Chg | No | Tax | % Chg | | |
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| College graduation | 0.30 | 0.23 | -29.1 | 0.41 | 0.39 | -12.3 | | |

- HS mothers are relatively more affected: 18.8% vs. 8.7%
 - Effect (a): Tax benefits are highly progressive
 - $^{\circ}~$ Effect (b): Wage of low educated fall relatively more (13% vs. 7%)

Heterogeneous effects

| | ŀ | High School | | | College Graduate | | | |
|------------------------|--------------|-------------|-------|------|------------------|-------|--|--|
| | No Tax % Chg | | No | Tax | % Chg | | | |
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- Consequently, human capital of children with HS mothers fall relatively more
 - Increase in differential human capital
 - o Increase in differential college graduation rate
- Intergenerational persistence of education increases from 0.11 to 0.15

Policy Evaluation

Two forces at play:

(a) Relative Price Effect:

Taxes distort relative price between number of children and their human capital.

(b) Income Effect:

Decreases in income induce parents to substitute children by children's human capital (quantity-quality trade-off)

- Disentangle relative importance:
 - Taking the economy without tax benefits as starting point...
 - 1. Add tax benefits without adjusting prices nor taxes \rightarrow effect (a)
 - 2. Let prices and taxes adjust \rightarrow effect (b)

Results decomposition

| | No Ben. | | Benefits | | Prices | | Tax Ben. |
|----------------------------|---------|---|----------|---|--------|---|----------|
| Completed fertility | 1.81 | + | 0.62 | _ | 0.32 | = | 2.11 |
| Fertility mothers | 2.08 | + | 0.18 | + | 0.06 | = | 2.32 |
| Share of mothers | 0.87 | + | 0.17 | _ | 0.13 | = | 0.91 |
| Differential fertility | -0.12 | _ | 0.23 | + | 0.03 | = | -0.32 |
| Human capital at J_l | 6.11 | _ | 0.43 | _ | 0.61 | = | 5.07 |
| Differential human capital | 1.05 | + | 0.30 | + | 0.16 | = | 1.51 |
| College graduation rate | 0.37 | - | 0.04 | _ | 0.05 | = | 0.28 |

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- GE and intergenerational effects ("Prices") are quantitatively important:
 - Significant reduction in the share of mothers
 - o 25% of the effects on fertility of mothers
 - $^{\circ}\,$ More than 50% of the effects on children's human capital

Results decomposition

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- GE and intergenerational effects ("Prices") are quantitatively important:
 - o 25% of the effects on fertility
 - More than 50% of the effects on children's human capital
- · Most of the inequality effect due to design of benefits

· Problem:

Tax benefits foster fertility at the expense of lower interg. mobility

· Question:

Is there a policy able to foster both fertility and children's human capital?

- Subsidies to education reduce the cost of children's human capital, which in turn, reduces the cost of children.
- · Implementation:

$$\mathcal{I}(n,m,t) = A_{\mathcal{I}} \left[\varsigma \left(\frac{m(1+\tau)}{n^{\psi_1}} \right)^{\gamma} + (1-\varsigma) \left(\frac{t}{n^{\psi_2}} \right)^{\gamma} \right]^{\frac{1}{\gamma}}$$

Key difference: CG parents spend more on children's human capital (regressive transfer)

| | No Benefits | Tax Benefits | Subsidy |
|----------------------------|-------------|--------------|---------|
| Completed fertility | 1.82 | 2.11 | 2.01 |
| Differential fertility | -0.12 | -0.32 | -0.10 |
| Share of mothers | 0.87 | 0.91 | 0.95 |
| Human capital at J_l | 6.11 | 5.07 | 6.30 |
| Differential human capital | 1.05 | 1.51 | 1.06 |
| College graduation | 0.37 | 0.28 | 0.38 |
| Interg. Persist. education | 0.11 | 0.15 | 0.10 |

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- Effective at increasing fertility: 62% of the increase with tax benefits
 - Regressive transfer: 12% increase among CG and 10% among HS
 - Education subsidies reduce the cost of children for CG relatively more.
- More effective than tax benefits at the extensive margin
 - Cost of education is an important barrier for parenthood

| | No Benefits | Tax Benefits | Subsidy |
|----------------------------|-------------|--------------|---------|
| Completed fertility | 1.82 | 2.11 | 2.01 |
| Differential fertility | -0.12 | -0.32 | -0.10 |
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- As opposed to tax benefits, education subsidies do not reduce human capital
 - Reduce the cost of children by reducing the cost of human capital
 - o Parents spend less money, and the government more than compensates
- · No cost in terms of intergenerational mobility

Conclusions

Conclusions

- I propose a GE life cycle model with fertility choices and parental investments in children's human capital, estimated with US data
 - Rich degree of heterogeneity
 - Suitable for family-policy analysis
- Evaluate quantitative impact of child-related tax benefits:
 - Significant effects on fertility and parental investments
 - Stronger for low income families: reduces the gap in initial conditions
 - o Both relative price distortion and GE effects are important
- Education subsidies increases fertility w/o damaging intergenerational mobility

Take-aways

- 1. We should evaluate pronatalist policies beyond their effects on fertility
- 2. Short-run inequality *versus* long-run inequality

Thanks for your attention

Some references

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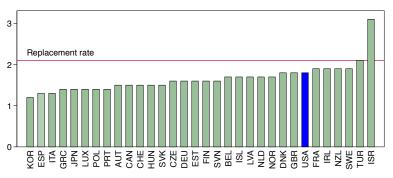
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Additional material

Low fertility rates

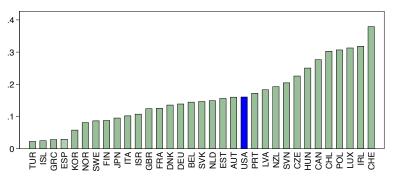
Figure: Total Fertility Rate (2016)



Source: OECD Family Database.

Tax benefits are widely extended

Figure: Tax Benefits for families with 2 children (2017)



Source: OECD Family Database.

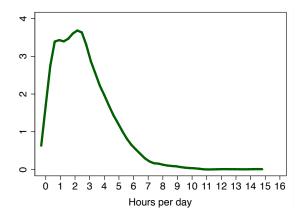
Notes: Tax benefits measured as the relative difference in tax rates between a married household with 133% of the average income and 2 children and a family with the same level of income but no children. Example: in Italy, the tax benefits are of 10%, meaning that a family with 2 kids and 133% of the average Italian household income pays 10% lower taxes than a family with the same level of income and no children.

CDS Sample

- Start in 1997 collecting info on children aged 0 to 12 from PSID families, and follow them over time.
- I use the 2002 and 2007 waves (children aged 6 to 18).
- · Time diary:
 - Obtailed info on child's activities: nature, duration, whether parents participate, etc.
- Test scores (Woodcock Johnson Tests)
 - Standard measure of child's cognitive skills.
 - Large number of yes-or-no questions.
- Includes individual identifiers for children and parents: link with PSID data.
- Information on 4,530 children: 1,892 also in PSID when adult.



Time Investments



Children's Human Capital

Table: Children's (normalized) scores in the Woodcock Johnson Tests

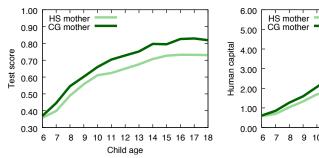
| | Obs. | Mean | Std | Min | Max |
|-------------------------|-------|-------|-------|-------|-------|
| Applied Problem Solving | 4,125 | 0.608 | 0.144 | 0.050 | 1.000 |
| Passage Comprehension | 4,047 | 0.590 | 0.159 | 0.023 | 1.000 |
| Letter-Word | 4,125 | 0.741 | 0.170 | 0.086 | 0.983 |

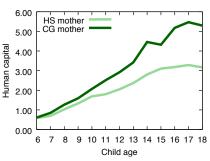
Children's Human Capital

Table: Summary statistics, children's human capital measures

| | Obs | Mean | Std | Corr(q,e) |
|-------------------------|-------|-------|-------|-----------|
| Applied Problem Solving | 4,122 | 2.091 | 2.358 | 0.449 |
| Passage Comprehension | 4,037 | 1.875 | 1.678 | 0.300 |
| Letter-Word | 4,109 | 6.303 | 8.274 | 0.336 |
| All test | 4,024 | 2.590 | 1.981 | 0.482 |

Human capital by age





Income taxes in the US

| _ | Gross income Adjustments to gross income |
|-------------|--|
| = - - | Adjusted gross income Standard deduction Personal exemptions, or Itemized deductions |
| = | Taxable Income Taxes |
| = - - | Tax imposed Nonrefundable credits Refundable credits. |
| = | Tax liability after credits |

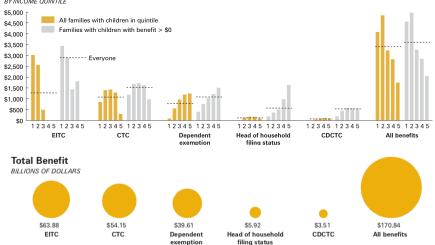
Income taxes in the US

Sources of child-depdendencies

- Standard deduction: singles w/ children can claim "head of household" filling status, who enjoy higher standard deduction.
- Personal exemptions: extra amount per dependent child (phase out)
- Itemized deductions: interests paid on education loans, and higher education expenses (both limited and for higher education).
- Children and dependent care tax credit (CDCTC): non-refundable credit for the care of dependents (phase out)
- Child tax credit (CTC): refundable credit of \$1,000 per eligible child (phase out)
- Earned income tax credit (EITC): higher credit rate, maximum credit and phase out threshold.
- Tax rates: heads of households enjoy lower tax rates.

Maag (2013)

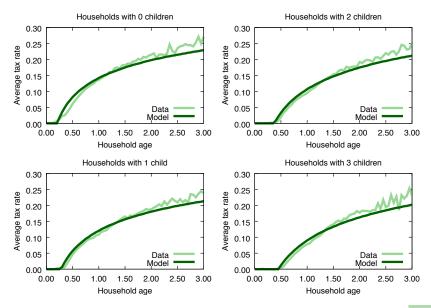
Average Benefit of Child-Related Tax Benefits for Families with Children at Various Income Levels



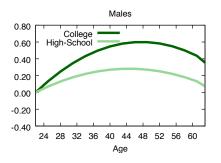
CPS Sample

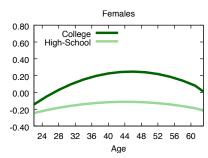
- Annual Survey of Economic Conditions Supplement to the CPS.
 - Years 2000 to 2010.
 - Large sample size:
 Allows for clustering by the number of children in the household.
- Tax-related variables from the Census Bureau's tax model
 - Using info from: IRS, the American Housing Survey, and the State Tax Handbook.
- Sample selection:
 Keep married households filling joint returns and positive income.

Tax function



Income profiles





- Construct hourly wages for full-time workers.
- Fit 2nd order polynomial in age, by education and gender.
- Normalize $\mu(m, \overline{e}, J_I) = \mu(m, \underline{e}, J_I) = 0$.

Income profiles

• Take residuals as our measure of labor productivity. Estimate (by education):

$$z_{i,t} = \alpha + \rho z_{i,t-2} + \epsilon_{i,t}$$

• Measurement error: instrument $z_{i,t-2}$ with $z_{i,t-4}$ (biannual observations)

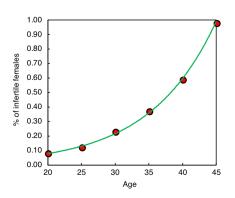
Table: Labor productivity process estimation

| | Low educated | High educated |
|--------------------------------|--------------|---------------|
| Autocorrelation, ρ_e | 0.824 | 0.902 |
| Std of innovations, σ_e | 0.406 | 0.392 |

Fertility risk

Follow Sommer (JME 2016): use data from medical literature on infertility.

$$p_0(b,j) = \begin{cases} 1 - \exp(\alpha_0 + \alpha_1 j) & \text{if } b = 1 \text{ and } j \leq J_F \\ 0 & \text{otherwise} \end{cases}$$



Children independence

Probability that a child becomes adult given by:

$$\rho_{l}(n,j) = \frac{\sum_{i=1}^{N} \mathbf{1}\{n_{i,t} < n \land n_{i,t-3} = n \land \text{age} = j\}}{\sum_{i=1}^{N} \mathbf{1}\{n_{i,t-3} = n \land \text{age} = j\}}$$

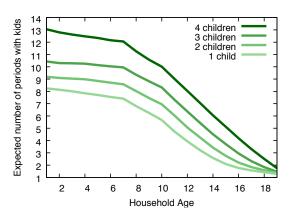
• Results (PSID data):

Table: Children ageing process

| | | Mother's age | | | | |
|-------------------|-------|--------------|-------|-------|--|--|
| Age | 20-28 | 29-37 | 38-46 | >46 | | |
| Model age (j) | 1-3 | 4-6 | 7-9 | >9 | | |
| $p_l(n = 1, j)$ | 0.029 | 0.037 | 0.288 | 0.501 | | |
| $p_l(n = 2, j)$ | 0.025 | 0.041 | 0.309 | 0.579 | | |
| $p_l(n = 3, j)$ | 0.049 | 0.105 | 0.399 | 0.718 | | |
| $p_l(n \ge 4, j)$ | 0.125 | 0.140 | 0.455 | 0.720 | | |

Children independence

Figure: Expected number of years with children, by age and number of children



Computation

- High dimensional problem: more than 120,000 grid points in the state space
- Choice set depends on the state
 - Young households choose whether to have a kid
 - Parents decide on investments
 - o etc.
- Up to 6 continuous choice variables (+1 discrete)
- Value function is not differentiable: solution requires global methods
- Solution:
 - Parallel computing (OpenMP)
 - Solve household problem using Nelder–Mead method