



Department of BES-I

**COURSE: Data Structures**

**COURSE CODE: 24SC1203**

Topic:

**NAME OF THE TOPIC:**  
**Construction of B-Tree**

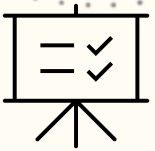
Session – 32

## AIM OF THE SESSION



To familiarize students with the basic concept of B-Tree.

## INSTRUCTIONAL OBJECTIVES



This Session is designed to:

1. Demonstrate The Concept of B-Tree.
2. Describe the concept of m-way ordered Balanced Tree.
3. List out the operations possible on the construction of B-Tree.
4. Describe the each operation.
5. List out the advantages and applications of B-Tree.

## LEARNING OUTCOMES



At the end of this session, you should be able to:

1. Define Construction of B-Tree.
2. Describe three different ordered of B-Tree. And their operations.
3. Summarize definition, types and operations of construction of B-Tree and its applications.

# Construction of B-Tree

## INTRODUCTION

- B-Tree is a balanced m-way tree.
- Generalization of BST in which a node can has more than one key and more than two children.
- Maintain Sorted (ascending order) data.
- All leaf nodes must be at same level.
- B-Tree of order m has following properties
  - \* Every node has maximum m no of children
  - \* Minimum children : leaf node  $\rightarrow 0$   
root  $\rightarrow 2$   
internal nodes  $\rightarrow \text{ceiling}(m/2)$

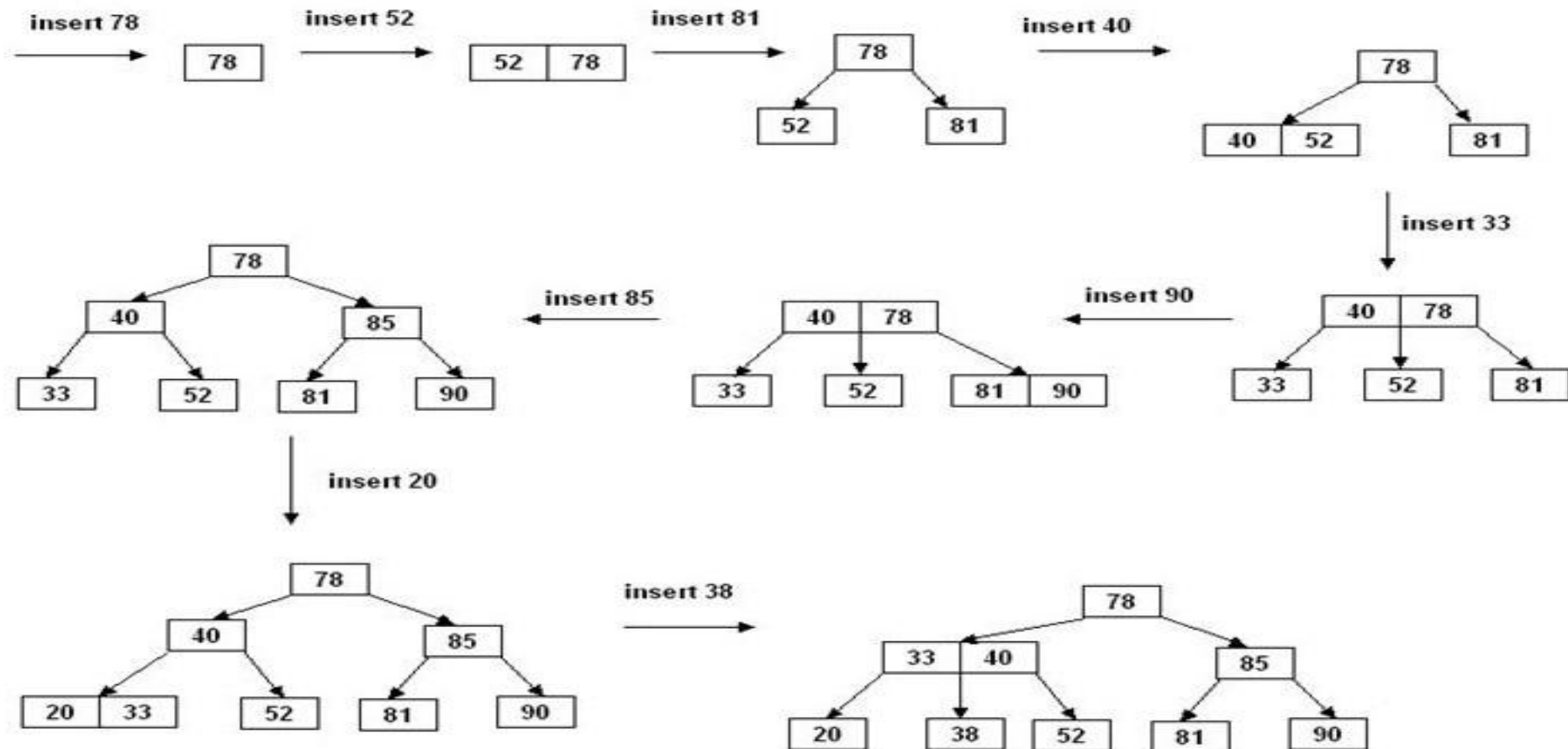
# Construction of B-Tree

## INTRODUCTION

- Every node has maximum  $(m-1)$  keys.
- Minimum keys:
  - Root  $\rightarrow 1$ .
  - All other nodes  $\rightarrow \text{ceiling}(m/2) - 1$ .

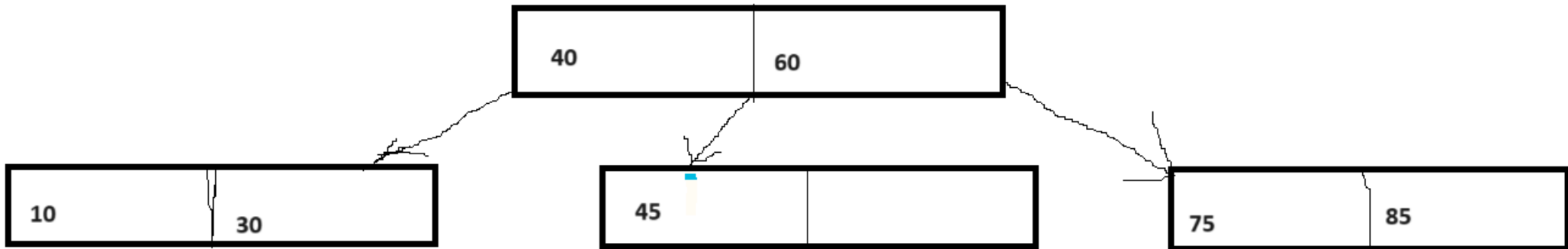
## Example of Construction of B-Tree 3 order

- Example: Insert the keys 78, 52, 81, 40, 33, 90, 85, 20, and 38 in this order in an initially empty B-tree of order 3



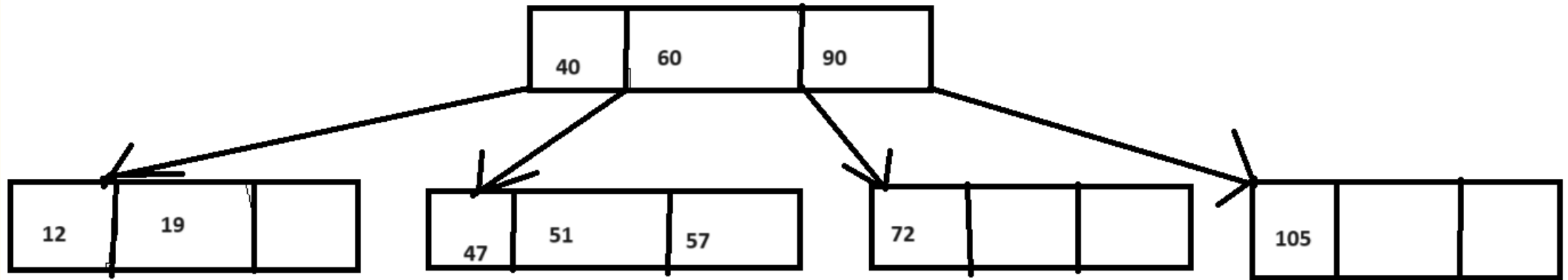
### 1. Order 3 balanced B-Tree:

- Here, each node can hold max 2 keys.



### Order 4 balanced B-Tree:

- Here, each node can hold max 3 keys.



In a B-Tree, we can perform the following operations...

- ❖ Insertion
- ❖ Deletion
- ❖ Display



# Steps for insertion an element in a B-Tree

(Cont..)

- Always insert element at leaf node and in sorted manner.
- Before insert check no of keys at that node. Maximum no of keys are possible in a node is  $m-1$ .
- Explain with example:
- Insert all the following numbers in a B-Tree having  $m=4$ .

6, 3, 12, 10, 5.

As  $m=4$ , so maximum no of keys are possible in a node is 3.

First insert 6:



Next Insert 3. As 3 is less than 6 so it comes at left side of 6.

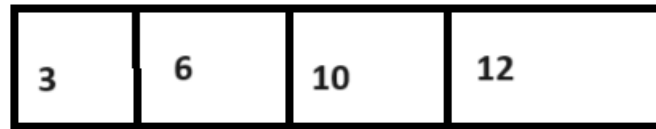


## Insertion

- Next Insert 12. As 12 is greater than 3 as well as 6. So it comes right side of 6.



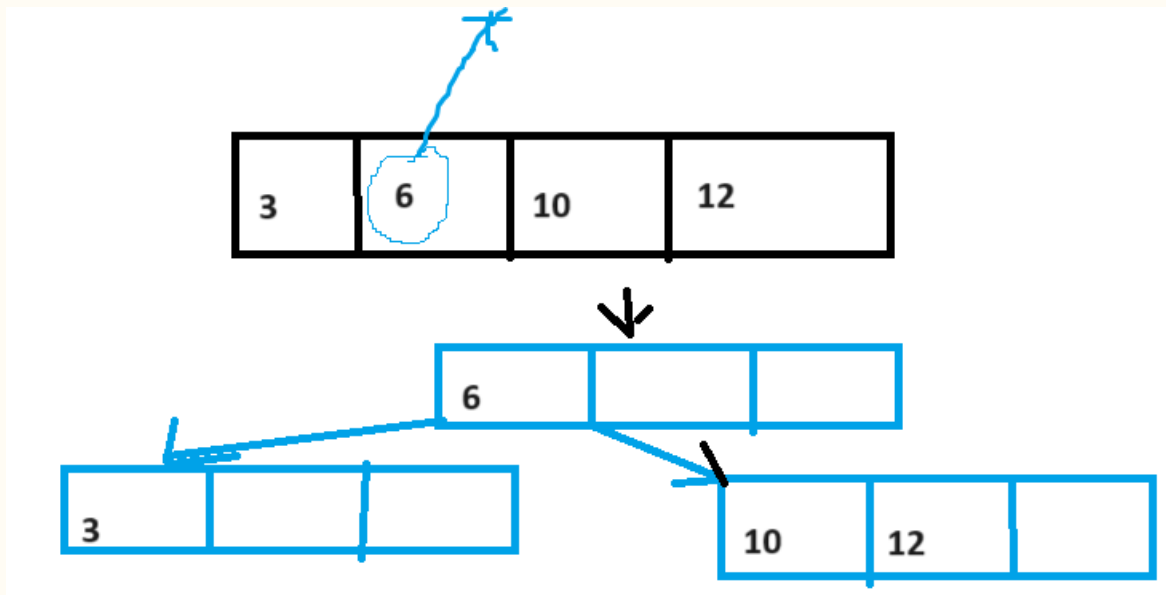
- Next insert 10. 10 is greater than 6 but less than 12. so it comes in between 6 and 12



But here, the problem is number keys of the above node are 4 which is more than the value of  $m-1$  (as  $m=4$ ). So we have to send the middle element of the node towards the up node.

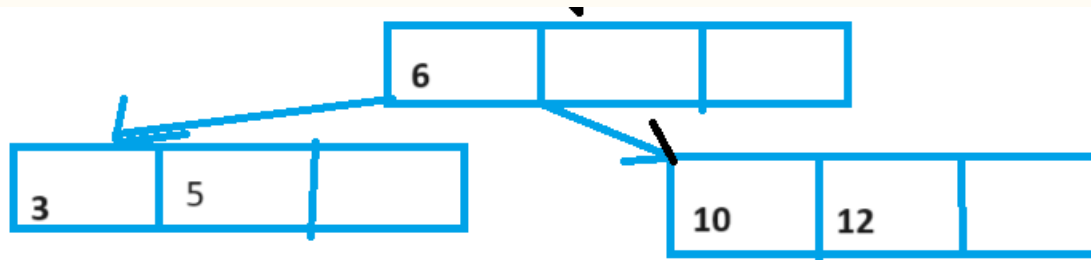
# Insertion

Here middle elements are 6 and 10. We can send any one. If we send 6 to upwards then it is called Left Biased. If we send 10 to upwards then it is called Right Biased. Let, we consider Left Biased.



## Insertion

Next element is 5. We have to check from root node. 5 is less than 6, so it goes to the left child node of 6. Next we have to compare with 3. 5 is greater than 3 so it comes right side of 3. Always insert at leaf node.



### **Advantages of a B-Tree**

- B-Tree can Balance themselves
- High throughput and concurrency
- Efficient use of storage space

### **Disadvantages of B-Tree**

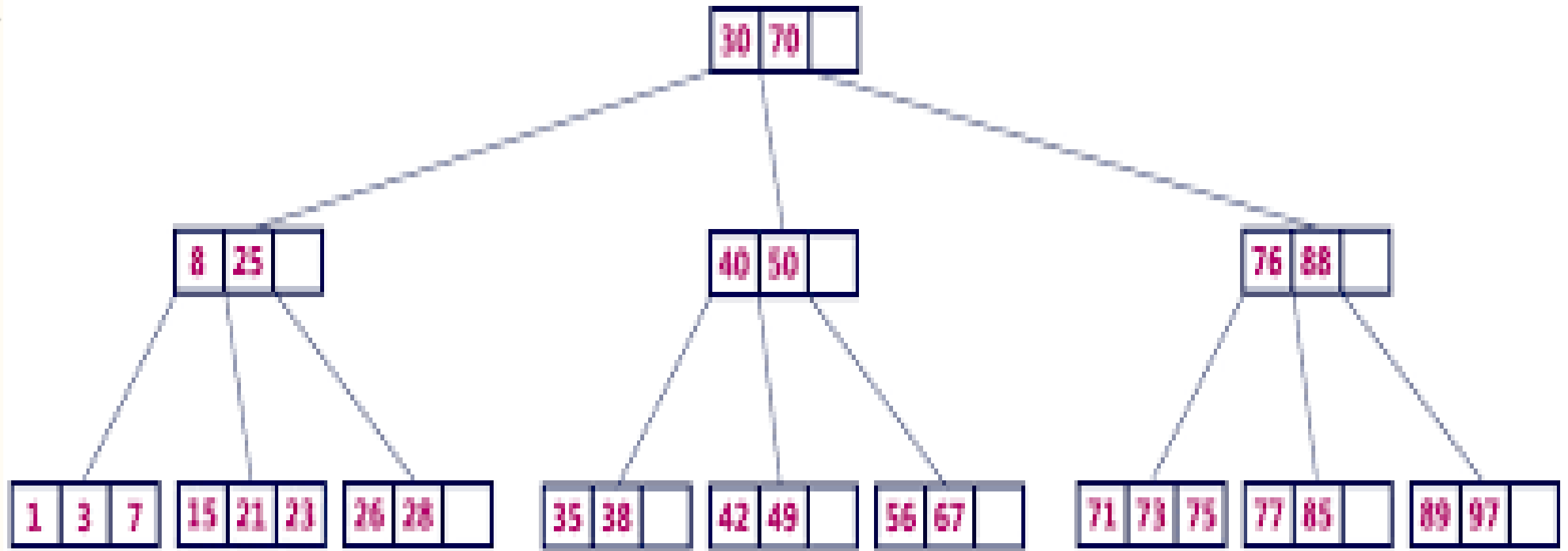
- B-Tree require more space
- Not efficient for write-heavy workloads.
- slow

### **Applications/Uses of B-Tree in real life**

- Database system
- File Organisation
- Information Retrieval

# EXAMPLES

## B-Tree of Order 4



- B-Tree is a  $m$ -way balanced tree.
- Store data in sorted way.
- If the order is  $m$  then each node can have maximum  $m-1$  keys.
- Always insert element into leaf node.
- If the no of keys reaches at  $m-1$  of a node then middle element of the node has to move up.

## SELF-ASSESSMENT QUESTIONS

1. How many max keys are there in a node of order  $m$ ?

- a)  $m$
- b)  $m+1$
- c)  $m/2$
- d)  $m-1$

2. Which of the following is false about a construction of B-Tree?

- a) Max no of keys of a node is  $m-1$
- b) If the order is  $m$ , then a node can have max  $m$  no of children
- c) Time complexity for deleting the last node is  $O(n)$
- d) All Leaf nodes are in same level.



- 1. Describe About Construction of B-Tree.**
- 2. Define order of the B-Tree.**
- 3. List out the different properties of B-Tree.**
- 3. Analyze the time complexity of B-Tree.**
- 4. Summarize What is B-Tree, its types and operations possible on it?**

## **Reference Books:**

1. Mark Allen Weiss, Data Structures and Algorithm Analysis in C, 2010 , Second Edition, Pearson Education.
2. Ellis Horowitz, Fundamentals of Data Structures in C: Second Edition, 2015
3. A.V.Aho, J. E. Hopcroft, and J. D. Ullman, “Data Structures And Algorithms”, Pearson Education, First Edition  
Reprint 2003.

## **Sites and Web links:**

1. <https://nptel.ac.in/courses/106102064>
2. <https://in.udacity.com/course/intro-to-algorithms--cs215>
3. <https://www.coursera.org/learn/data-structures?action=enroll>

**THANK YOU**



**Team – Data Structures**