



I/IV B. Tech. Even Semester :: A.Y. 2024-25

Linear Algebra & Calculus for Engineers (23MT1001)

CO-2

Tutorial-4

1. Compute all first and second order partial derivatives of $f(x, y) = e^{xy} + 3x^2 - 5y^3$ and verify $f_{xy} = f_{yx}$.
2. Compute the first and second order partial derivatives of $z = x^2 y^3 + \sin x \cos y$.
3. Verify $\frac{\partial^2 u}{\partial x \partial y} = \frac{\partial^2 u}{\partial y \partial x}$ for the function $u = \tan^{-1}\left(\frac{x}{y}\right)$.
4. Given $u = e^x \cos y$, $x = t^2 + 1$, $y = 2t$ then find the total derivative $\frac{du}{dt}$.
5. Given $u = \log(x + y + z)$, $x = e^t$, $y = \sin t$, $z = \cos t$ then find the total derivative $\frac{du}{dt}$.
6. Find the Jacobian $\frac{\partial(u, v)}{\partial(x, y)}$ of following functions:
 - (a). $u = x^2 - 2y$, $v = 5x + 7y$
 - (b). $u = x(1 - y)$, $v = xy$
7. Find the Jacobian $\frac{\partial(u, v, w)}{\partial(x, y, z)}$ of $u = \frac{yz}{x}$, $v = \frac{xz}{y}$, $w = \frac{xy}{z}$.

Tutorial-5

1. Apply Taylor's series to expand $f(x, y) = x^3 + 2xy + y^3$ in powers of $(x+1)$ and $(y+2)$ up-to second degree terms.
2. Applying Taylor's series expansion expand the function $f(x, y) = e^x \sin y$ at $(-1, \pi/4)$ up to the terms of second degree.
3. Examine the maximum and minimum for the function $f(x, y) = x^3 + y^3 - 63(x + y) + 12xy$.
4. The sum of three numbers is constant. Prove that their product is maximum when they are equal.
5. Evaluate minimum values of $x^2 + y^2 + z^2$, given that $ax + by + cz = p$.
6. A rectangular box open at the top is to have a volume of 32 cubic ft. Find the dimensions of the box requiring least material for its construction
7. The temperature T at any point (x, y, z) in space is $T = kxyz^2$. Find the highest temperature on the surface of the unit sphere of $x^2 + y^2 + z^2 = 1$.

Tutorial-6

1. Solve the DE $\frac{d^3y}{dx^3} - 9\frac{d^2y}{dx^2} + 23\frac{dy}{dx} - 15y = 0$.
2. Solve the DE $y''' + 4y'' + 4y' = 0$.
3. Determine the solution of the initial value problem $\frac{d^2y}{dx^2} - 8\frac{dy}{dx} + 15y = 2$, given that $y(0) = 0$, $y'(0) = 1$.
4. Determine the charge on the capacitor in an LRC series circuit at t when inductance 1 H, resistance 4Ω , capacitance 0.25 F, $E(t) = 0$ V, $q(0) = 5$ C, and $i(0) = 0$ A.
5. Determine the charge on the capacitor in an LC series circuit at t when inductance 1 H, capacitance 1 F, $E(t) = e^t$ V, $q(0) = 2$ C, $i(0) = 0$ A.
6. The motion of a mass spring system without damping is described by the initial value problem $\frac{d^2x}{dt^2} + 3\frac{dx}{dt} + 2x = e^{4t}$, $x(0) = 0$, $x'(0) = 1$, where x is the distance of the mass from the equilibrium position, downward being taken as positive direction. Calculate the displacement of the motion.
7. The motion of a mass spring system without damping is described by the initial value problem $\frac{d^2x}{dt^2} + 4x = \cos 3t$, $x(0) = 0$, $x'(0) = 0$, where x is the distance of the mass from the equilibrium position, downward being taken as positive direction. Identify the displacement of the motion.