



I/IV B. Tech. Even Semester :: A.Y. 2024-25

Linear Algebra & Calculus for Engineers (23MT1001)

CO-2 Home Assignment Problems

1. Compute the first and second order partial derivatives of $f(x, y) = \sin(xy) + x^2 \log_e y$
2. Given $x = r \cos \theta, y = r \sin \theta$ Find the value of $\frac{\partial(x, y)}{\partial(r, \theta)}$.
3. Apply Taylor's series to expand $f(x, y) = x^2 + xy + y^2$ in powers of $(x-1)$ and $(y-2)$.
4. Determine the maxima and minima of $f(x, y) = 2x + 2y - 2xy - 2x^2 - y^2$.
5. Given $x + y + z = a$ find the maximum of $x^m y^n z^p$
6. Show that if the perimeter of a triangle is constant, the triangle has maximum area when it is equilateral.
7. Determine the solution of the initial value problem $(D^2 - 5D + 6)y = e^{4x}$, given that $y(0) = 0, y'(0) = 1$.
8. Determine charge q and current i in the LCR circuit with inductance 1H, resistance 12 ohms, capacitance $(1/35)F$, $E(t) = 0$.
9. Determine the charge and current in an LCR series circuit when inductance 3 H, resistance 6 ohms capacitance $1/3 F$, and $E(t) = \sin 2t$.
10. The motion of a mass spring system without damping is described by the initial value problem $\frac{d^2x}{dt^2} + 8\frac{dx}{dt} + 16x = \cos 3t, x(0) = 0, x'(0) = 1$ where x is the distance of the mass from the equilibrium position, downward being taken as positive direction. Calculate the displacement of the motion.