

Prob 1

Decision Variable:

1. Amount borrowed each month: B_i , $i = 1 \sim 5$
2. Amount of payment delayed each month: D_i , $i = 1 \sim 6$
3. Short-term loan taken at the beginning: Loan

Objective:

Minimize the total cost =

$$\text{MIN}(\sum_{i=1}^5 B_i * 0.015 + \frac{\sum_{i=1}^6 D_i}{.98} + \text{Loan} * (1.01^6) - M_i)$$

Note: M_i = Monthly interest earned, $i = 2 \sim 6$

Constraints:

The beginning balance of the month = The ending balance of the previous month

$B_i \leq \text{Accounts Receivable}_i * 0.75$

$D_i < \text{Planned Payments of the Month}_i$

$\text{Balance}_i = \text{Balance}_{i-1} + \text{Accounts Receivable}_i + \text{delay}_i + \text{borrow}_i + \text{Interest Earned}_i - \text{Planned Payment}_i - \text{Loan Repayment}_i$

Optimal Solution:

	Borrow	Payment	Payment Delayed	Monthly Balance
1	0.000000	1.8	0.0	0.609594
2	0.242486	1.6	0.0	0.250000
3	1.050000	2.2	0.0	0.250000
4	0.000000	1.2	0.0	0.280373
5	0.000000	0.8	0.0	1.476650
6	0.000000	1.2	0.0	0.766183

Prob 2

Decision Variable:

U_i : Number of untrained programmers to be retained in month i

T_i : Number of programmers to be trained in month i

L_i : Number of untrained programmers to be laid off in month i

Note: $i = 1 \sim 6$

Objective:

Minimize $Z = \sum_{i=1}^6 (3000U_i + 3300T_i)$

Constraints:

Layoff Constraints: $U_i - L_i \geq 0$ for $i \in \{1, 2, \dots, 6\}$

Training Completion Constraints: $T_i \leq 0.9(U_i - L_i)$ for $i \in \{1, 2, \dots, 6\}$

Initial Workforce Constraint: $U_1 + T_1 = 145$

Turnover Constraints: $0.95(U_i - L_i) \geq U_{i+1}$ for $i \in \{1, 2, \dots, 5\}$

Additional Constraints for Part (b):

If June demand = 125 and April demand = 150:

$T_4 = T_6 = 0$ && $U_4 + 1.2T_4 \geq 150$

Optimal Solution:

Part(a)

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Status: Optimal
Layoff_1 = 8.113
Layoff_2 = 0.0
Layoff_3 = 0.0
Layoff_4 = 0.0
Layoff_5 = 0.0
Layoff_6 = 0.0
Trained_1 = 0.0
Trained_2 = 33.1983
Trained_3 = 67.8723
Trained_4 = 92.5803
Trained_5 = 111.226
Trained_6 = 119.102
Trainee_1 = 36.887
Trainee_2 = 38.5267
Trainee_3 = 27.4534
Trainee_4 = 20.7173
Trainee_5 = 8.75123
Trainee_6 = 0.0
Untrained_1 = 145.0
Untrained_2 = 98.6887
Untrained_3 = 61.0066
Untrained_4 = 34.6209
Untrained_5 = 15.2802
Untrained_6 = 7.07763
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Part(b)

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Status: Optimal
Layoff_1 = 5.76564
Layoff_2 = 0.0
Layoff_3 = 0.0
Layoff_4 = 0.0
Layoff_5 = 8.51449
Layoff_6 = 14.0145
Trained_1 = 0.0
Trained_2 = 35.3109
Trained_3 = 72.4778
Trained_4 = 100.242
Trained_5 = 100.242
Trained_6 = 100.242
Trainee_1 = 39.2344
Trainee_2 = 41.2966
Trainee_3 = 30.8486
Trainee_4 = 0.0
Trainee_5 = 0.0
Trainee_6 = 0.0
Untrained_1 = 145.0
Untrained_2 = 98.9234
Untrained_3 = 58.8752
Untrained_4 = 29.7101
Untrained_5 = 28.2246
Untrained_6 = 18.7246
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