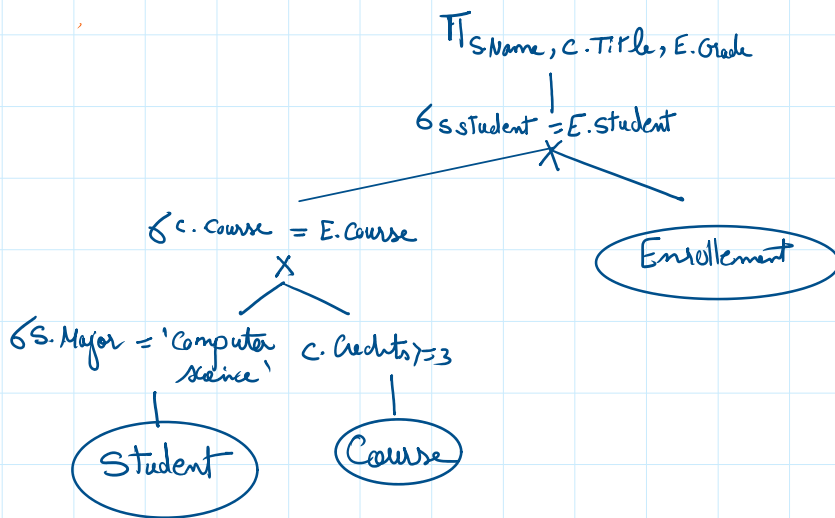
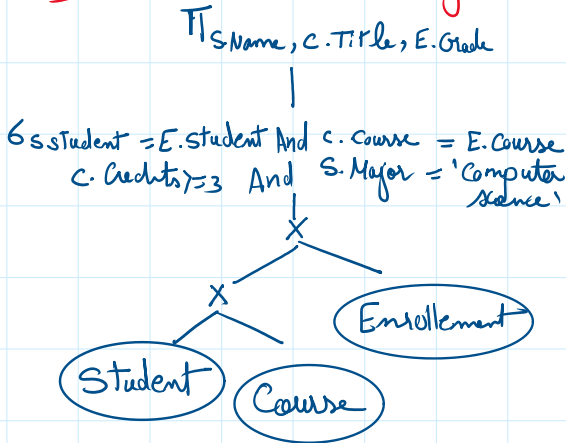


```

SELECT S.Name, C.Title, E.Grade
FROM STUDENT S, COURSE C, ENROLLMENT E
WHERE S.StudentID = E.StudentID
AND C.CourseID = E.CourseID
AND S.Major = 'Computer Science'
AND C.Credits >= 3;

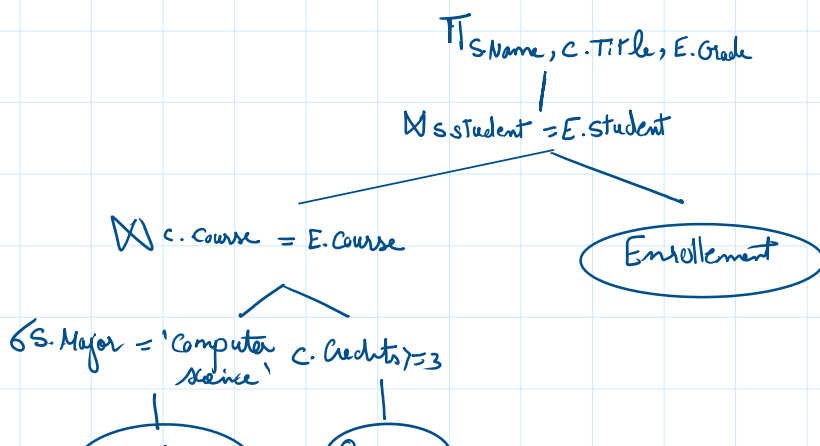
```

## Initial Relational Algebra

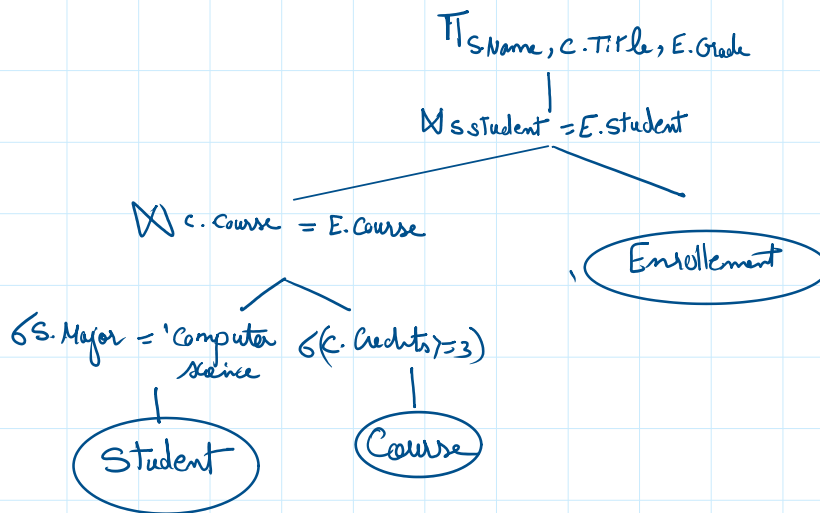
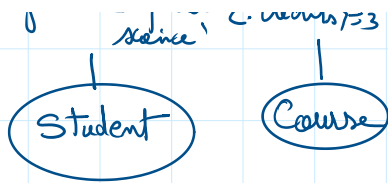


• push selection down

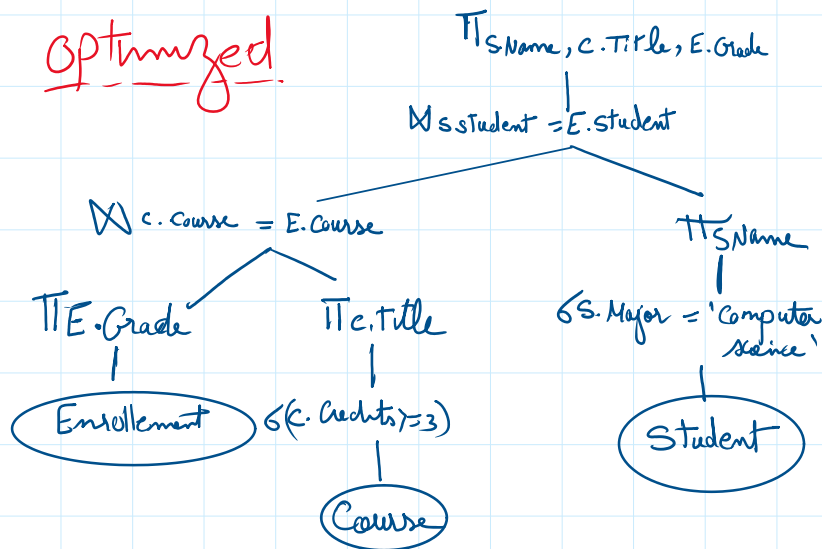
- Apply  $\sigma_{Major='cs'}$  to student early
- Apply  $\sigma_{Credits \geq 3}$  to Course early



- Replace Cartesian product followed by selection with  $\bowtie$  join
- Apply projection  $\Pi$  early to reduce tuple size



Optimized



cs Students ← σ<sub>major = 'Computer Science'</sub>(Students)

$Credits \leftarrow \sigma_{Credits \geq 3}(Course)$

$CSEnroll \leftarrow Credits \bowtie_{\substack{c.CourseID \\ = E.CourseID}} Enrollment$

$Join \leftarrow CSEnroll \bowtie_{\substack{s.StudentID \\ = E.StudentID}} CSStudents$

$Result \leftarrow \pi_{\substack{name, \\ title, Grade}}(Join)$

$CSStudents \leftarrow \sigma_{\substack{major = 'computer \\ science'}}(Students)$

$Credits \leftarrow \sigma_{Credits \geq 3}(Course)$

$CSStudents2 \leftarrow \pi_{\substack{StudentID}}(CSStudents)$

$Credits2 \leftarrow \pi_{\substack{C.title}}(Credits)$

$Enroll2 \leftarrow \pi_{\substack{E.grade}}(Enrollment)$

$CSEnroll \leftarrow Credits2 \bowtie_{\substack{c.CourseID \\ = E.CourseID}} Enroll2$

$Join \leftarrow CSEnroll \bowtie_{\substack{s.StudentID \\ = E.StudentID}} CSStudents2$

$Result \leftarrow \pi_{\substack{name, \\ title, Grade}}(Join)$