

# Ciel and Gondolas

时间限制：4s

内存限制：512 MB

提交地址：<https://www.luogu.com.cn/problem/CF321E>

## 题面翻译

有一只叫 Ciel 的狐狸正在排队去做摩天轮，队列中有  $n$  个人。

摩天轮上有  $k$  个吊舱，我们按照如下方式分配吊舱：

1. 第一个吊舱有  $q_1$  只狐狸，就是第  $1 \sim q_1$  只狐狸。
2. 第二个吊舱有  $q_2$  只狐狸，就是第  $q_1 + 1 \sim q_1 + q_2$  只狐狸。
3. 第三个吊舱有  $q_3$  只狐狸，就是第  $q_1 + q_2 + 1 \sim q_1 + q_2 + q_3$  只狐狸。

以此类推，最后  $q_k$  只狐狸坐进第  $k$  个吊舱。

显然，我们需要保证  $\sum_{i=1}^k q_i = n$ 。

每只狐狸都不想和陌生狐坐在一起，所以我们给出矩阵  $u_{i,j}$ ，表示第  $i$  只狐狸和第  $j$  只狐狸的陌生值，保证  $u_{i,j} = u_{j,i}$ ， $u_{i,i} = 0$ 。

我们定义一个吊舱的陌生值为吊舱中每一对人的陌生值之和，总陌生值为每一个吊舱的陌生值之和，输出总陌生值的最小值。

## 题目描述

Fox Ciel is in the Amusement Park. And now she is in a queue in front of the Ferris wheel. There are  $n$  people (or foxes more precisely) in the queue: we use first people to refer one at the head of the queue, and  $n$ -th people to refer the last one in the queue.

There will be  $k$  gondolas, and the way we allocate gondolas looks like this:

- When the first gondolas come, the  $q_1$  people in head of the queue go into the gondolas.
- Then when the second gondolas come, the  $q_2$  people in head of the remain queue go into the gondolas. ...
- The remain  $q_k$  people go into the last ( $k$ -th) gondolas.

Note that  $q_1, q_2, \dots, q_k$  must be positive. You can get from the statement that  $\sum_{i=1}^k q_i = n$  and  $q_i > 0$ .

You know, people don't want to stay with strangers in the gondolas, so your task is to find an optimal allocation way (that is find an optimal sequence  $q$ ) to make people happy. For every pair of people  $i$  and  $j$ , there exists a value  $u_{ij}$  denotes a level of unfamiliar. You can assume  $u_{ij} = u_{ji}$  for all  $i, j$  ( $1 \leq i, j \leq n$ ) and  $u_{ii} = 0$  for all  $i$  ( $1 \leq i \leq n$ ). Then an unfamiliar value of a gondolas is the sum of the levels of unfamiliar between any pair of people that is into the gondolas.

A total unfamiliar value is the sum of unfamiliar values for all gondolas. Help Fox Ciel to find the minimal possible total unfamiliar value for some optimal allocation.

## 输入格式

The first line contains two integers  $n$  and  $k$  ( $1 \leq n \leq 4000$  and  $1 \leq k \leq \min(n, 800)$ ) — the number of people in the queue and the number of gondolas. Each of the following  $n$  lines contains  $n$  integers — matrix  $u$ , ( $0 \leq u_{ij} \leq 9$ ,  $u_{ij} = u_{ji}$  and  $u_{ii} = 0$ ).

Please, use fast input methods (for example, please use `BufferedReader` instead of `Scanner` for Java).

## 输出格式

Print an integer — the minimal possible total unfamiliar value.

### 样例 #1

#### 样例输入 #1

```
5 2
0 0 1 1 1
0 0 1 1 1
1 1 0 0 0
1 1 0 0 0
1 1 0 0 0
```

#### 样例输出 #1

```
0
```

### 样例 #2

#### 样例输入 #2

```
8 3
0 1 1 1 1 1 1 1
1 0 1 1 1 1 1 1
1 1 0 1 1 1 1 1
1 1 1 0 1 1 1 1
1 1 1 1 0 1 1 1
1 1 1 1 1 0 1 1
1 1 1 1 1 1 0 1
1 1 1 1 1 1 1 0
```

#### 样例输出 #2

```
7
```

## 样例 #3

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### 样例输入 #3

```
3 2
0 2 0
2 0 3
0 3 0
```

### 样例输出 #3

```
2
```

## 提示

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In the first example, we can allocate people like this: {1, 2} goes into a gondolas, {3, 4, 5} goes into another gondolas.

In the second example, an optimal solution is : {1, 2, 3} | {4, 5, 6} | {7, 8}.

在第一个样例中，我们可以这样分配：{1, 2}上一个吊舱，{3, 4, 5}上另一个吊舱。

在第二个样例中，一个最佳解是：{1, 2, 3} | {4, 5, 6} | {7, 8}。