





-2

```
In[1]:= Clear["Global`*"]
       n = .;
       f[x_{y_1} := (x^2 + y^2)^(Abs[n]/2) * Cos[n * ArcTan[y/x]];
       g[x_{y_{1}} := (x^{2} + y^{2})^{(Abs[n]/2)} * Sin[n * ArcTan[y/x]];
       r[x_{y_{1}}] := Sqrt[f[x, y]^{2} + g[x, y]^{2}]
       drx = Integrate[D[r[x, y], x], x];
       dry = Integrate[D[r[x, y], y], y];
       dr[x_, y_] := drx + dry
       dr[x, y]
       \phi[x_{y_{1}}] := ArcTan[y/x];
       I1 = Integrate[(f[x, y] * D[g[x, y], x] - g[x, y] * D[f[x, y], x]) / f[x, y]^2, x];
       I2 = Integrate[(f[x, y] * D[g[x, y], y] - g[x, y] * D[f[x, y], y]) / f[x, y]^2, y];
       d\phi[x_{,}, y_{]} := 1/(1+(g[x, y]/f[x, y])^2)*(I1+I2)
       d\phi[x, y]
       index = (Integrate[d\phi[1, y], \{y, -1, 1\}] + Integrate[d\phi[x, 1], \{x, 1, -1\}] +
             Integrate [d\phi[-1, y], \{y, 1, -1\}] + Integrate [d\phi[x, -1], \{x, -1, 1\}]) / (2 * Pi)
       StreamPlot[\{f[x, y], g[x, y]\} /. n \rightarrow -1, \{x, -3, 3\}, \{y, -3, 3\}]
       StreamPlot[\{dr[x, y], d\phi[x, y]\} /. n \rightarrow 1, \{x, -3, 3\}, \{y, -3, 3\}]
Out[9]= 2 \sqrt{(x^2 + y^2)^{Abs[n]}}
\text{Out[14]=} \  \  \frac{2\,\text{Tan}\left[\,n\,\text{ArcTan}\left[\,\frac{y}{x}\,\right]\,\right]}{1+\,\text{Tan}\left[\,n\,\text{ArcTan}\left[\,\frac{y}{x}\,\right]\,\right]^2}
Out[15]= 0
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-1

0

-3

-2

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