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In[67]:= Clear["Global`*"]
σ = 10; b = 8 / 3; r = 28;
f[x_, y_, z_] := σ * (y - x);
g[x_, y_, z_] := r * x - y - x * z;
h[x_, y_, z_] := x * y - b * z;
s = Solve[f[x, y, z] == 0 && g[x, y, z] == 0 && h[x, y, z] == 0, {x, y, z}]
J[x_, y_, z_] := {{D[f[x, y, z], x], D[f[x, y, z], y], D[f[x, y, z], z]},
  {D[g[x, y, z], x], D[g[x, y, z], y], D[g[x, y, z], z]},
  {D[h[x, y, z], x], D[h[x, y, z], y], D[h[x, y, z], z]}};
Eigenvalues[J[x, y, z] /. s[[1]]] (* (1) Has eigenvalues larger than one → unstable *)
Eigenvalues[J[x, y, z] /. s[[2]]]
(* (2) and (3) have imaginary eigenvalues → unstable *)
Eigenvalues[J[x, y, z] /. s[[3]]]

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Out[72]= $\left\{ \{x \rightarrow 0, y \rightarrow 0, z \rightarrow 0\}, \{x \rightarrow -6\sqrt{2}, y \rightarrow -6\sqrt{2}, z \rightarrow 27\}, \{x \rightarrow 6\sqrt{2}, y \rightarrow 6\sqrt{2}, z \rightarrow 27\} \right\}$

Out[73]= $\left\{ \frac{1}{2} \times (-11 - \sqrt{1201}), \frac{1}{2} \times (-11 + \sqrt{1201}), -\frac{8}{3} \right\}$

Out[74]= $\left\{ \frac{1}{3} \sqrt{-41.6...}, \frac{1}{3} \sqrt{0.282... + 30.6... i}, \frac{1}{3} \sqrt{0.282... - 30.6... i} \right\}$

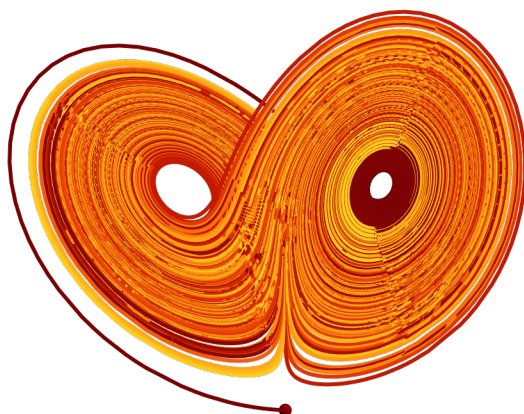
Out[75]= $\left\{ \frac{1}{3} \sqrt{-41.6...}, \frac{1}{3} \sqrt{0.282... + 30.6... i}, \frac{1}{3} \sqrt{0.282... - 30.6... i} \right\}$

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In[85]:= Clear["Global`*"]
 $\sigma = 10$ ;  $b = 8/3$ ;  $r = 28$ ;
(*Plotting code courtesy of Wolfram Mathematica guides at: https://reference.wolfram.com/language/example/VisualizeTheLorenzAttractor.html*)
s = NDSolve[{x'[t] ==  $\sigma$  * (y[t] - x[t]), y'[t] ==  $r$  * x[t] - y[t] - x[t] * z[t],
  z'[t] == x[t] * y[t] - b * z[t], x[0] == y[0] == z[0] == 0.01},
  {x, y, z}, {t, 0, 400}, MaxSteps -> 1000000];
Show[ParametricPlot3D[Evaluate[{x[t], y[t], z[t]} /. s], {t, 0, 400},
  PlotPoints -> 1000, PlotStyle -> Directive[Thick, RGBColor[.8, 0, 0]],
  ColorFunction -> (ColorData["SolarColors", #4] &)],
Graphics3D[{ColorData["SolarColors"][0],
  Sphere[First[({x[t], y[t], z[t]} /. s) /. t -> 0], .75]}], RotationAction -> "Clip",
Boxed -> False, SphericalRegion -> False, Axes -> False, ImageSize -> 500]

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Out[88]=



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In[60]:= Clear["Global`*"]
f[x_, y_, z_] :=  $\sigma$  * (y - x);
g[x_, y_, z_] :=  $r$  * x - y - x * z;
h[x_, y_, z_] := x * y - b * z;
J[x_, y_, z_] := {{D[f[x, y, z], x], D[f[x, y, z], y], D[f[x, y, z], z]},
  {D[g[x, y, z], x], D[g[x, y, z], y], D[g[x, y, z], z]},
  {D[h[x, y, z], x], D[h[x, y, z], y], D[h[x, y, z], z]}};
J[x, y, z]
Tr[J[x, y, z]]

```

Out[65]= {{- σ , σ , 0}, { $r - z$, -1, -x}, {y, y, -b}}

Out[66]= -1 - b - σ