· Notes on Revised Submission for Homework: After the solution is released.

Step 1: Self-gracle (Evaluation for initial submission)

Step 2; Do a revision

Step 3: Self-grade for the second time

(Full marks if finished, and this is your final

grade for the homework)

Note: both two self-grade should be reported in the first page of your honework.

- More examples on Counting Methods:

52 cards => 4 suits { Spades | Clubs | Hearts | Diamonds

each suits => 13 ranks (Ace, 2, ---, 10, J, Q, K)

Poker hands consist of 5 cards out of 52

Thus, $\binom{52}{5}$ ways to choose (without ordering)

Now, we consider the following events:

· Ao = { Poker hands has exactly one pair}

one pairs = two cards with the same rank but

different suits.

Step 1: Choose the pairs

(13) ways to choose the ranks

(4) ways to choose the suits

Step 2: For the remaining three single cords

(12) ways to choose the ranks

43 ways to choose the suits

so $\#A_0 = {\binom{13}{1}} {\binom{4}{2}} {\binom{12}{3}} \cdot 4^3$

· A, = { Poker hands has exactly two pairs with diff rank}

Step 1: For the two pairs

(13) ways to choose the ranks

(4) (4) ways to choose the suits

Step 2: For the remaining one single cards

(1) ways to choose the ranks

4 ways to choose the suits

 $\# A = \binom{13}{2} \binom{4}{2}^2 \binom{11}{4} \cdot 4$

* $A_2 = \{ \text{ Five cards with } \frac{\text{ranks in a sequence}}{\text{not all in the same suit } \}$

Step 1: Choose the ranks

=) 10 ways to choose the rank Step 2: Choose the suits.

(In total: Each card has 4 suits,

DAU in the same suits: 4 suits in total =) 4 ways

 \Rightarrow Not all in the same suits: 4^5-4 ways (Addition rule) $\#A_2=10(4^5-4)$

· Az = { Five cards of the same suits, but not in a sequential ranks}

Step 1: Chouse the suits
4 suits in total => 4 ways to chouse

Step 2: Choose the ranks

{ In total:
$$\binom{13}{5}$$
 ways to choose a rank

In a sequential rank: 10 ways to choose

Not in a sequential rank: $\binom{13}{5} - 10$ ways (Addition rule)

$A_5 = 4 \left(\binom{13}{5} - 10 \right)$

- Multinomial Coefficients

n items in total, assigning labels $1, 2, \dots, \Gamma$ to n items s.t.

$$\begin{cases} k_{1} & \text{items} & \text{receive label 1} \\ k_{2} & \text{items} & \text{receive label 2} \end{cases} = k_{1} + k_{2} + \cdots + k_{r}$$

$$\vdots & = n$$

$$k_{r} & \text{items} & \text{receive laber r} \end{cases}$$

Then, the number of ways to label is

$$\binom{n}{k_1 \ k_2 - - k_r} = \frac{n!}{(k_1!)(k_2!) - - (k_r!)}$$

e.g. 52 cards in total, 4 players with each one holding 13 cards.

$$61 \text{ cards}$$
 $13 / 3 / 3 / 3$

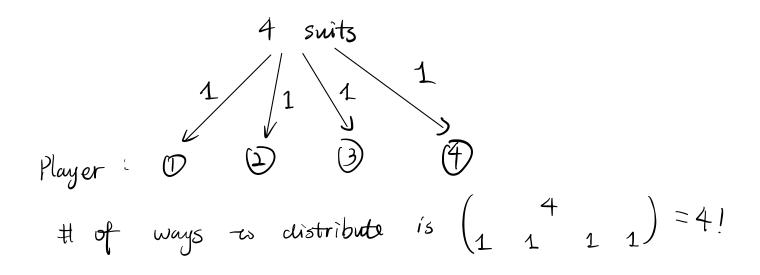
Player: 0 0 0 0 1

if ways - w distribute cards is

$$\begin{pmatrix} 52 \\ 13 & 13 & 13 \end{pmatrix} = \frac{52!}{(13!)^4}$$

of ways to distribute cards is (9 13 13 13)

Now, $B_2 = \{ \{ \{ \{ \} \} \} \} \}$ cards of the some suit $\{ \} \}$



-Q2A on Homework 1 (if time permits)

Next time: Conditional Probability & HW2.