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0H: Monday 4-5 p.m.

Section Material: Course Material in GitHub web.

Reading: App B, App C, Chapter 1.2

Week 1: Set notation and operations

Experiment — A random experiment is a process in which all possible outcomes are known in advanced, but we can't predict which outcomes will occur

Sample space (52) — the set of all possible outcomes in the experiment

e.g. Experiment: toss a coin $S2 = \{H, T\}$

e.g. Experiment: roll a die $\Omega = \{1, 2, 3, 4, 5, 6\}$

1. Notation:
$$\Omega$$
 - set; A, B - subset of Ω
w - elements of Ω .

(1)
$$W \in A$$
 (w is a member of A)

 $E - \text{belong to}$
 $W \notin A$ (w is NOT a member of A)

A&B: At least one elem in A is NOT in B.

e.g.
$$\Omega = \{1, 2, 3, 4, 5, 6\}$$

$$A = \{2,4,6\}$$
, $B = \{1,2,3,4\}$, $C = \{i\}$

Easy to see

2 E A.

5 & A

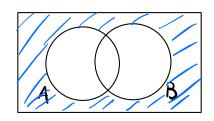
C = B

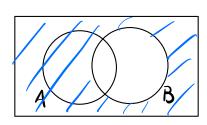
C & A

A 4 B

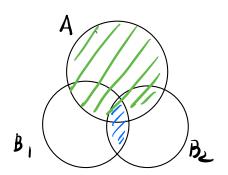
- 2. Set Operatur
 - (1) Union = AUB = { WED: WEA or WEB}
- (2) Intersection: ANB = {WED: WEA and WEB}
- (3) Complement: AC = {WED: WEA}
- (4) Pifference: A \ B = { wED: wEA and w&B}
 - e.g. Back to the previous Example:

3. Pe Morgan's laws: A, B- subsets of 2

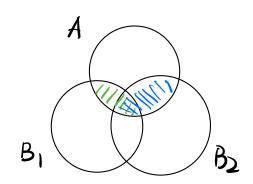




- 4. Distributive Property: A, B, B, B, subsets of 2
- (1) $AU(B_1 \cap B_2) = (AUB_1) \cap (AUB_2)$



(2) $A \cap (B_1 \cup B_2) = (A \cap B_1) \cup (A \cap B_2)$



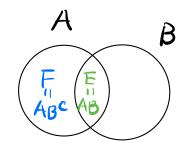
Rmk: Sets A, and Az: If $A_1 \subseteq A_2$, then $A_1 \cap A_2 = A_1, \quad A_1 \cup A_2 = A_2$

e.g. A, B - subsets of D, E=ANB, F=ANBC

(a) Show that E and F are disjoint (ENF=p).

 $f: E \cap F = (A \cap B) \cap (A \cap B')$ $= A \cap B \cap B^{c} = A \cap \phi = \phi$

(b) Show that A = EUF.



Pf: A = AND

= AN (BUB')

= (ANB)U (ANB') (Pistributure law)

= EUF

(c) Show that BUA = BUF.

Pf: BUF = BU (ANB') AB=F

= (BUA) N (BUB') (Distributure law)

= (BUA) N D = BUA