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OH: See Canvas

Section Material: Course Material in GitHub web.

Reading: App B, App C, Chapter 1.2

Week 1: Set notation and operations

Experiment — A random experiment is a process in which all possible outcomes are known in advanced, but we can't predict which outcomes will occur

Sample space (S2) — the set of all possible outcomes in the experiment

e.g. Experiment: toss a coin $S2 = \{H, T\}$

e.g. Experiment: roll a die $\Omega = \{1, 2, 3, 4, 5, 6\}$

1. Notation:
$$\Omega$$
 - set; A, B - subset of Ω
w - elements of Ω .

(1)
$$W \in A$$
 (w is a member of A)

 $E - \text{belong to}$
 $W \notin A$ (w is NOT a member of A)

A&B: At least one elem in A is NOT in B.

e.g.
$$\Omega = \{1, 2, 3, 4, 5, 6\}$$

$$A = \{2,4,6\}$$
, $B = \{1,2,3,4\}$, $C = \{i\}$

Easy to see

2 E A.

5 & A

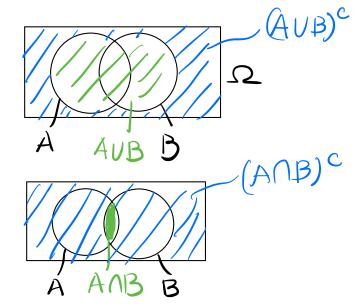
C = B

C & A

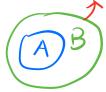
A 4 B

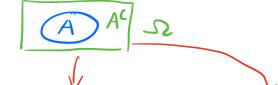
- 2. Set Operatur
 - (1) Union = AUB = {WED: WEA or WEB}
- (2) Intersection: ANB = {WED: WEA and WEB}
- (3) Complement: AC = {WED: WEA}
- - e.g. Back to the previous Example:

3. Pe Morgan's laws: A, B- subsets of 2



- 4. Distributive Property: A, B, B, B, subsets of 2
- (1) $A \cup (B_1 \cap B_2) = (A \cup B_1) \cap (A \cup B_2)$
- (2) $A \cap (B_1 \cup B_2) = (A \cap B_1) \cup (A \cap B_2)$
- 5. Some useful results:
- (1) If $A \subseteq B$, then $A \cup B = B$ and $A \cap B = A$.

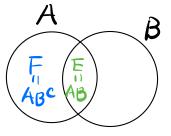




- (2) For any set A, $A \cap A^c = \phi$ and $A \cup A^c = S2$
- HWI, PI: A, B subsets of I , E=ANB, F=ANBC
- (a) Show that E and F are disjoint (ENF=p)
- 野: ENF = (ANB) N(ANBY

$$= A \cap B \cap B^{c} = A \cap \phi = \phi$$

(b) Show that A = EUF.



$$\underline{\mathbf{M}}: A = A \cap \Omega \quad (b/c \ A \subseteq \Omega)$$

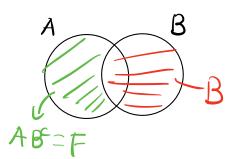
= A (BUB')

= (ANB) U (ANB^c) (Pistributure law)

= EUF

(C) Show that AUB=FUB

Pt: FUB= (ANBC) UB AB=F



= AUB (b/c AUB = s)