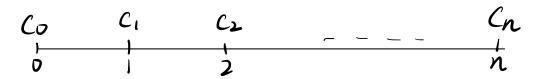
1. Internal Rate of Return



$$C_{K}$$
: cash flows at time K { $C_{K} > 0$: flows in $C_{K} < 0$: flows out

$$C_0 + \frac{C_1}{1+\bar{\iota}} + \frac{C_2}{(1+\bar{\iota})^2} + \cdots + \frac{C_n}{(1+\bar{\iota})^n} = D$$

(1) The time-weighted rate of return (Compound Interest)

①
$$\hat{\imath}_i$$
: IRR from D to $\hat{\tau}_i$

$$F_i = (1+\hat{\imath}_i)A_i \implies \frac{F_i}{A_i} = 1+\hat{\imath}_i$$

2)
$$\hat{\iota}_{L^{2}}$$
 IRR from to $\hat{\iota}_{L}$

$$(F_{1}+C_{1})(1+\hat{\iota}_{L})=F_{2}=\frac{F_{2}}{F_{1}+C_{1}}=1+\hat{\iota}_{L}$$

$$(F_{K}+C_{K})(1+\bar{\iota}_{KH})=A_{1}=\frac{A_{1}}{F_{K}+G_{K}}=1+\hat{\iota}_{KH}$$

To summerize:

time weighted rate of return 0-1:

$$=\frac{F_1}{A_0}\cdot\frac{F_1}{F_1+C_1}\cdot\cdots\cdot\frac{A_1}{F_k+C_k}-1$$

(2) The dollar-weighted rate of return (Simple Interest)

Deposit:
$$A_0$$
 C_1 C_2 C_k

$$yr 1: A_0(Hi) \int C_1(1+(1-t_k)i) C_2(1+(1-t_k)i)$$

$$C_1(1+(1-t_k)i) C_2(1+(1-t_k)i)$$

By Equivalence Principle:

$$A_{i} = A_{0}(1+\overline{\iota}) + \sum_{J=1}^{K} C_{J}(1+(1-t_{J})\overline{\iota})$$

$$= \left(A_{0} + \sum_{J=1}^{K} C_{J}\right) + \left(A_{0} + \sum_{J=1}^{K} C_{J}(1-t_{J})\right)\overline{\iota}$$

$$= \frac{A_1 - (A_0 + \sum C_1)}{A_0 + \sum C_1(1 - t_1)}$$

Dollar-weighted rate of return

P3: 1/1 9/1 12/31
Balance: 100,000 98000 100000 10000

Peposit: -10000 10000

a. Time-weighted rate of return:

$$\frac{98000}{1000001} \times \frac{100000}{98000 - 100000} \times \frac{105000}{1000000 + 100000} - 1$$

= 6,3%

b. Pollar-weighted rate of return:

$$C_2 = 10000$$
 $t_2 = 8/12$

A1= 105000

$$\bar{v} = \frac{A_1 - (A_0 + C_1 + C_2)}{A_0 + \frac{11}{12}C_1 + \frac{4}{12}C_2} = 5.31\%$$

2. Net Present Value

Given rate of return/effective rate $\bar{\imath}$,

$$MPV = Co + \frac{C_1}{1+\bar{i}} + \frac{C_2}{(1+\bar{i})^2} + \cdots + \frac{C_n}{(1+\bar{i})^n}$$

CK : cash flows in/out at time k

PII: time 0: invest 50000

At end of each yr from yr 3-10; returns
$$X$$
 $i=1070$, $NPV=2500$, find X .

Soln: $NPV=2500$
 $C_0=-50000$
 $C_3=--=C_{00}=X$, $C_1=C_2=0$

$$2500 = -50000 + \times 0.5000 + \times 0.$$

Ch 6: Term Structure

1. Spot Rate: Yield rate on an zero-coupon bound.
Given a t-year maturity zero-coupon bond:

K = maturity value / redemption value

$$=) P = \frac{1}{(1+S_0(t))^t}$$

In general: $\frac{\text{time}}{CF}$ $\frac{\text{ti}}{C_1}$ $\frac{\text{ti}}{C_2}$ $\frac{\text{---}}{C_1}$ $\frac{\text{tn}}{C_2}$

$$PV_{cF} = \frac{C_1}{(1+50(t_0)^{t_1}} + \frac{C_2}{(1+50(t_0))^{t_2}} + \cdots + \frac{C_n}{(1+50(t_n))^{t_n}}$$

2. Forward rate of interest

 $\hat{l}_0(n-1,n)$: effective interest rate from time n-1 to n.

Recall that in week I Leed see, the effective interest rate from time t to thi:

$$\overline{v}_{t,t+1} = \frac{a(t+1)-a(t)}{a(t)}$$

Thus, $\bar{v}_0(n-1,n)$ can be obtained by

$$\hat{\iota}_{0}(n-1,n) = \frac{(1+SLn)^{n}}{(1+S_{0}(n-1))^{n-1}} - 1$$

where AV at n-1: $a(n-1) = (1+5.(n-1))^{n-1}$

AV at $n : \alpha(n) = (1+5\alpha(n))^n$