

### 3/ Discrete 2D Fourier transform

$$F(\underline{u_i}, \underline{v_j}) = \sum_{\substack{\underline{j} \\ \text{sampled frequency}}} \sum_i f(\underline{x_i}, \underline{y_j}) e^{-j(\underline{u_i} \cdot \underline{x_i} + \underline{v_j} \cdot \underline{y_j})}$$

sampled points

gives magnitude (size)  
a phase (time)

properties? Shift invariance (of magnitude)  
rotates with image  
scales with  $1/\text{scaling}$ .

applications? speed up algorithms  
window & filtering  
analysis (e.g. gait/texture)  
invariance (above).

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# Image sampling & the Fourier transform

(9-71)

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0). Fourier transform = real +  $j \times$  imaginary  
 = mag + phase

1/. sampling? high = good lot many points  
 low = could have fewer points

2/. Nyquist's sampling theorem.  
 uses Fourier

	high	sampling	rate	$\Rightarrow$	spectra	separate
	good	"	"	"	"	touch
	low	"	"	"	"	collide

Sampling rate =  $2 \times$  max frequency  
 speech max 6 kHz. Sample @ 12 kHz  
 images? digital? take two points/  
 texture of interest.