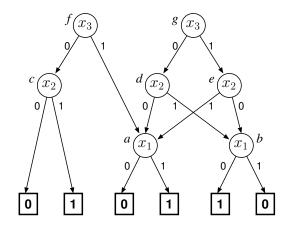
CPRE/SE/COMS 412, COMS 512 HOMEWORK 7

Reminder: present your own work and properly cite any sources used. Solutions should be presented satisfying the *other student viewpoint*. If you need clarification, contact the instructor: asminer@iastate.edu.

Question 1 20 points

For the BDD forest shown below, draw the BDD obtained from the operation $apply(f, \land, g)$.



Question 2 20 points

Prove or disprove the following path formula equivalences.

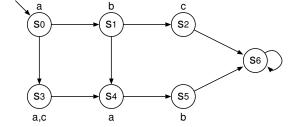
1.
$$XF \psi \stackrel{?}{\equiv} FX \psi$$

2.
$$XG\psi \stackrel{?}{\equiv} GX\psi$$

Question 3 15 points

For the Kripke structure below,

- 1. enumerate all possible paths starting from state s_0 , and
- 2. for each path, determine if the path formula $(a \cup b) \cup c$ is satisfied.



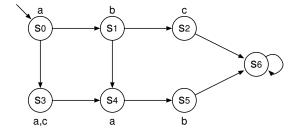
CPRE/SE/COMS 412, COMS 512 HOMEWORK 7

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Question 4 (optional for 412)

20 points

For the Kripke structure below, draw the tableau graph for path formula $\psi = (a \cup b) \cup c$. Using the tableau graph, determine if the model satisfies properties $\mathsf{E}\,\psi$ and $\mathsf{E}\,\neg\psi$.



Question 5 (optional for everyone)

20 points

Consider the CTL formula $\phi = \mathsf{E} \, ((\mathsf{E} \, a \, \mathsf{U} \, b) \, \mathsf{U} \, c)$, and the LTL formula $\mathsf{E} \, \psi$ for path formula $\psi = (a \, \mathsf{U} \, b) \, \mathsf{U} \, c$. Prove or disprove the following.

- 1. For any Kripke structure M and state s in M, $M, s \models \phi \stackrel{?}{\rightarrow} M, s \models \mathsf{E} \psi$
- 2. For any Kripke structure M and state s in M, $M, s \models \mathsf{E} \psi \stackrel{?}{\to} M, s \models \phi$

Question 6 (optional for everyone)

15 points

Prove or disprove the path formula equivalence:

$$\mathsf{FGF}\,\psi \ \stackrel{?}{\equiv} \ \mathsf{GF}\,\psi$$