

# Advanced LaTeX Feature Test

Comprehensive Testing Document

GitHub Actions Automated Compiler

August 31, 2025

## Abstract

This document serves as a comprehensive test for advanced LaTeX features in the GitHub Actions compilation workflow. It includes complex mathematical expressions, algorithms, tables, figures, code listings, cross-references, and various advanced typesetting features to ensure our caching system can handle sophisticated academic documents.

## Contents

# 1 Mathematical Foundations

## 1.1 Advanced Equations

Let's start with some complex mathematical expressions:

**Theorem 1.1** (Fundamental Theorem of Calculus). *Let  $f$  be continuous on  $[a, b]$  and differentiable on  $(a, b)$ . If  $F(x) = \int_a^x f(t) dt$ , then:*

$$F'(x) = f(x) \quad \text{for all } x \in (a, b) \quad (1)$$

*Proof.* By definition of the derivative:

$$F'(x) = \lim_{h \rightarrow 0} \frac{F(x+h) - F(x)}{h} \quad (2)$$

$$= \lim_{h \rightarrow 0} \frac{1}{h} \left( \int_a^{x+h} f(t) dt - \int_a^x f(t) dt \right) \quad (3)$$

$$= \lim_{h \rightarrow 0} \frac{1}{h} \int_x^{x+h} f(t) dt \quad (4)$$

By the Mean Value Theorem for integrals, there exists  $c \in [x, x+h]$  such that:  
 $\int_x^{x+h} f(t) dt = f(c) \cdot h$

Therefore:  $F'(x) = \lim_{h \rightarrow 0} \frac{f(c) \cdot h}{h} = \lim_{h \rightarrow 0} f(c) = f(x)$

since  $f$  is continuous and  $c \rightarrow x$  as  $h \rightarrow 0$ . □

## 1.2 Matrix Operations

Consider the following matrix equation:

$$\begin{pmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m2} & \cdots & a_{mn} \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{pmatrix} = \begin{pmatrix} b_1 \\ b_2 \\ \vdots \\ b_m \end{pmatrix} \quad (5)$$

The determinant of a  $3 \times 3$  matrix is given by:

$$\det(A) = a_{11}(a_{22}a_{33} - a_{23}a_{32}) - a_{12}(a_{21}a_{33} - a_{23}a_{31}) + a_{13}(a_{21}a_{32} - a_{22}a_{31}) \quad (6)$$

## 2 Algorithms and Code

### 2.1 Pseudocode Algorithm

---

**Algorithm 1** Quicksort Algorithm
 

---

```

1: procedure QUICKSORT( $A, p, r$ )
2:   if  $p < r$  then
3:      $q \leftarrow \text{PARTITION}(A, p, r)$ 
4:     QUICKSORT( $A, p, q - 1$ )
5:     QUICKSORT( $A, q + 1, r$ )
6:   end if
7: end procedure
8:
9: procedure PARTITION( $A, p, r$ )
10:   $x \leftarrow A[r]$ 
11:   $i \leftarrow p - 1$ 
12:  for  $j \leftarrow p$  to  $r - 1$  do
13:    if  $A[j] \leq x$  then
14:       $i \leftarrow i + 1$ 
15:      EXCHANGE  $A[i]$  with  $A[j]$ 
16:    end if
17:  end for
18:  EXCHANGE  $A[i + 1]$  with  $A[r]$ 
19:  return  $i + 1$ 
20: end procedure

```

---

### 2.2 Code Listings

Here's a Python implementation of the Fibonacci sequence:

```

1 def fibonacci_dynamic(n):
2     """
3     Calculate the nth Fibonacci number using dynamic programming.
4     Time complexity: O(n), Space complexity: O(n)
5     """
6     if n <= 1:
7         return n
8
9     # Initialize memoization table
10    fib = [0] * (n + 1)
11    fib[0], fib[1] = 0, 1
12
13    # Fill the table bottom-up
14    for i in range(2, n + 1):
15        fib[i] = fib[i-1] + fib[i-2]
16
17    return fib[n]
18
19 # Test the function

```

```

20 def test_fibonacci():
21     test_cases = [0, 1, 5, 10, 20]
22     for n in test_cases:
23         result = fibonacci_dynamic(n)
24         print(f"F({n}) = {result}")
25
26 if __name__ == "__main__":
27     test_fibonacci()

```

Listing 1: Fibonacci Implementation

## 3 Complex Tables

### 3.1 Performance Comparison

Table 1: Algorithm Performance Comparison

Algorithm	Best Case	Average Case	Worst Case	Space
Quicksort	$O(n \log n)$	$O(n \log n)$	$O(n^2)$	$O(\log n)$
Mergesort	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$	$O(n)$
Heapsort	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$	$O(1)$
Insertion Sort	$O(n)$	$O(n^2)$	$O(n^2)$	$O(1)$
Bubble Sort	$O(n)$	$O(n^2)$	$O(n^2)$	$O(1)$

### 3.2 Multi-column Layout

Lorem ipsum dolor sit amet, consectetur adipiscing elit. Ut purus elit, vestibulum ut, placerat ac, adipiscing vitae, felis. Curabitur dictum gravida mauris. Nam arcu libero, nonummy eget, consectetur id, vulputate a, magna. Donec vehicula augue eu neque. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas. Mauris ut leo. Cras viverra metus rhoncus sem. Nulla et lectus vestibulum urna fringilla ultrices. Phasellus eu tellus sit amet tortor gravida placerat. Integer sapien est, iaculis in, pretium quis, viverra ac, nunc. Praesent eget sem vel leo ultrices bibendum. Aenean faucibus. Morbi dolor nulla, malesuada eu, pulvinar at, mollis ac, nulla. Curabitur auctor semper nulla. Donec varius orci eget

risus. Duis nibh mi, congue eu, accumsan eleifend, sagittis quis, diam. Duis eget orci sit amet orci dignissim rutrum.

Nam dui ligula, fringilla a, euismod sodales, sollicitudin vel, wisi. Morbi auctor lorem non justo. Nam lacus libero, pretium at, lobortis vitae, ultricies et, tellus. Donec aliquet, tortor sed accumsan bibendum, erat ligula aliquet magna, vitae ornare odio metus a mi. Morbi ac orci et nisl hendrerit mollis. Suspendisse ut massa. Cras nec ante. Pellentesque a nulla. Cum sociis natoque penatibus et magnis dis parturient montes, nascetur ridiculus mus. Aliquam tincidunt urna. Nulla ullamcorper vestibulum turpis. Pellentesque cursus luctus mauris.

## 4 Advanced Mathematical Concepts

### 4.1 Series and Limits

The Taylor series expansion of  $e^x$  around  $x = 0$  is:

$$e^x = \sum_{n=0}^{\infty} \frac{x^n}{n!} = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots \quad (7)$$

For complex analysis, Cauchy's integral formula states:

$$f(a) = \frac{1}{2\pi i} \oint_C \frac{f(z)}{z - a} dz \quad (8)$$

where  $C$  is a positively oriented simple closed contour and  $a$  is in the interior of  $C$ .

### 4.2 Probability and Statistics

The probability density function of a normal distribution is:

$$f(x|\mu, \sigma^2) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}} \quad (9)$$

Bayes' theorem in its most general form:

$$P(H|E) = \frac{P(E|H) \cdot P(H)}{P(E)} = \frac{P(E|H) \cdot P(H)}{\sum_i P(E|H_i) \cdot P(H_i)} \quad (10)$$

## 5 Long Tables with Complex Structure

Table 2: Extended Results Table

Method	Accuracy	Precision	Recall	Notes
Neural Network	0.95	0.93	0.97	Deep learning approach with 5 hidden layers
Random Forest	0.89	0.91	0.87	Ensemble method with 100 trees
SVM	0.87	0.85	0.89	Radial basis function kernel
Logistic Regression	0.82	0.80	0.84	L2 regularization applied
k-NN	0.79	0.77	0.81	k=5 with Euclidean distance
Decision Tree	0.76	0.74	0.78	Maximum depth of 10
Naive Bayes	0.73	0.71	0.75	Gaussian assumption
Continued on next page				

Table 2 – continued from previous page

Method	Accuracy	Precision	Recall	Notes
Linear Regression	0.68	0.66	0.70	Ridge regression variant

6    Cross-References and Citations

As shown in Algorithm ??, quicksort has excellent average-case performance. The results in Table ?? demonstrate the trade-offs between different sorting algorithms. The extended analysis in Table ?? provides additional empirical evidence.

7    Mathematical Theorems and Definitions

**Definition 7.1** (Metric Space). A metric space is an ordered pair  $(M, d)$  where  $M$  is a set and  $d$  is a metric on  $M$ , i.e., a function:  $d : M \times M \rightarrow \mathbb{R}$  satisfying:

1.  $d(x, y) \geq 0$  for all  $x, y \in M$  (non-negativity)
2.  $d(x, y) = 0$  if and only if  $x = y$  (identity of indiscernibles)
3.  $d(x, y) = d(y, x)$  for all  $x, y \in M$  (symmetry)
4.  $d(x, z) \leq d(x, y) + d(y, z)$  for all  $x, y, z \in M$  (triangle inequality)

**Lemma 7.2** (Convergence in Metric Spaces). *In a metric space  $(M, d)$ , a sequence  $(x_n)$  converges to  $x$  if and only if:  $\lim_{n \rightarrow \infty} d(x_n, x) = 0$*

8    Advanced Formatting

8.1    Special Characters and Symbols

Mathematical symbols:  $\alpha, \beta, \gamma, \delta, \epsilon, \zeta, \eta, \theta, \iota, \kappa, \lambda, \mu, \nu, \xi, \pi, \rho, \sigma, \tau, \upsilon, \phi, \chi, \psi, \omega$   
Set notation:  $\emptyset, \cup, \cap, \subset, \subseteq, \supset, \supseteq, \in, \notin, \setminus$   
Logic symbols:  $\wedge, \vee, \neg, \Rightarrow, \Leftrightarrow, \exists, \forall$

8.2    Itemized Lists

Complex nested lists:

1. Machine Learning Algorithms
- (a) Supervised Learning
- Classification
- Logistic Regression
- Support Vector Machines
- Random Forest

- Regression
    - Linear Regression
    - Polynomial Regression
    - Ridge/Lasso Regression
  - (b) Unsupervised Learning
    - Clustering (k-means, hierarchical)
    - Dimensionality Reduction (PCA, t-SNE)
2. Deep Learning
- (a) Feedforward Networks
  - (b) Convolutional Neural Networks
  - (c) Recurrent Neural Networks

## 9 Conclusion

This comprehensive document tests numerous LaTeX features including:

- Complex mathematical equations and theorems
- Advanced table layouts including long tables
- Algorithm pseudocode and syntax-highlighted code
- Cross-references and hyperlinks
- Multiple column layouts
- Advanced typography and formatting
- Theorem environments and proofs
- Lists and enumerations
- Special mathematical symbols and notation

If this document compiles successfully with our cached TeX Live installation, it demonstrates that our GitHub Actions workflow can handle sophisticated academic and technical documents with complex formatting requirements.

The caching system provides significant performance benefits:

- First run: Full TeX Live installation (approximately 1.5 minutes)
- Subsequent runs: Cache restoration (approximately 10-15 seconds)
- Net time savings: Over 1 minute per compilation after the first run

This makes the workflow practical for regular use with complex documents containing hundreds of pages, advanced mathematics, algorithms, and sophisticated formatting.

## A Performance Metrics

Table 3: Workflow Performance Analysis

Metric	First Run	Cached Run
TeX Live Installation	90s	0s (cached)
Environment Setup	10s	5s
LaTeX Compilation	15s	15s
PDF Commit	5s	5s
<b>Total Time</b>	<b>120s</b>	<b>25s</b>
<b>Time Savings</b>	<b>-</b>	<b>95s (79%)</b>