Advanced Data Analysis HW4

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1. (a)

Answer:

I expect there's a positive correlation between sales of cigarettes and Age, because the people with higher ages tend to smoke more cigarettes, the proportion of people smoking within young people is relatively small.

I expect there's a negative correlation between sales of cigarettes and HS, because people with higher education are more aware of the harm of smoking and are tend to somke less.

I expect there's a positive correlation between sales of cigarettes and Income, because with more money, people can afford more cigarettes.

I don't expect there's a correlation between sales of cigarettes and Black, because there's no supporting evidence that black people are mode likely to smoke more than others.

I expect there's a negative correlation between sales of cigarettes and Female, because there are a lot more men smoking than women, the higher the proportion of the women, the less the proportion of people smoking.

I expect there's a negative correlation between sales of cigarettes and Price, the less the price is, the more people can afford the cigarettes.

(b)

Answer:

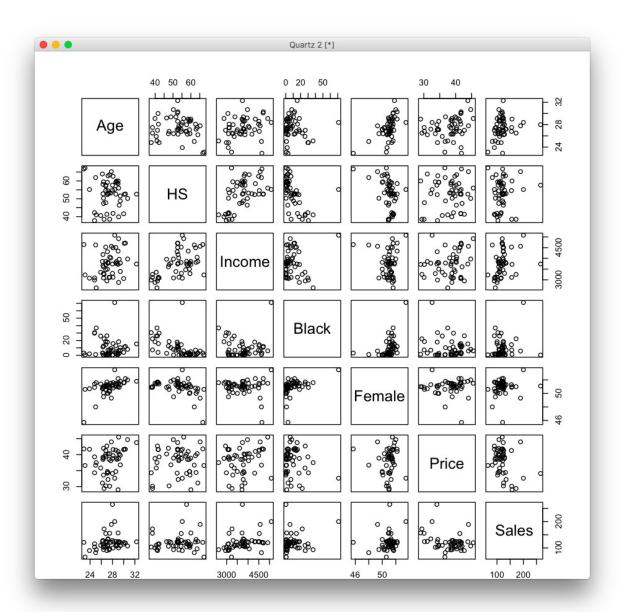
```
1 > data = read.table("DATACIGARETTE.txt", header = TRUE)
2 > mat.data <- data.matrix(data[,2:8])
3 > cor((mat.data))
```

so the pairwise correlation coefficient matrix is:

```
Age
                             Income
                                          Black
                                                      Female
                                                                 Price
Age 1.00000000
                 -0.09891626 0.25658098
                                          -0.04033021 0.55303189
                                                                   0.24775673
 0.22655492
HS = -0.09891626 1.00000000 0.53400534
                                          -0.50171191 -0.41737794 0.05697473
 0.06669476
                                 1.00000000
Income 0.25658098
                     0.53400534
                                              0.01728756
                                                           -0.06882666 0.21455717
 0.32606789
Black -0.04033021 -0.50171191 0.01728756
                                           1.00000000
                                                        0.45089974
 0.18959037
                     -0.41737794 -0.06882666 0.45089974
                                                         1.000000000 \quad 0.02247351
Female 0.55303189
 0.14622124
                                            -0.14777619 \ 0.02247351
                                                                     1.00000000
Price 0.24775673
                   0.05697473
                               0.21455717
  -0.30062263
                   0.06669476
                               0.32606789
Sales 0.22655492
                                            0.18959037
                                                         0.14622124
                                                                      -0.30062263
 1.00000000
```

```
1 > pairs (data [, 2:8])
```

The corresponding scatter plot is:



(c)

Answer:

```
1 > results = lm(Sales ~ Age+HS+Income+Black+Female+Price , data=data)
2 # install.packages('car')
3 > library(car)
4 > vif(results)
```

The VIF for 6 variables are:

```
1 Age HS Income Black Female Price
2 2.300617 2.676465 2.325164 2.392152 2.406417 1.142181
```

(d)

Answer:

Yes, there are outlying Sales observations in the regression model relating Sales to the six predictors.

```
1 > r = rstudent(results)
_{2} > data [abs(r) > 3,]
    State Age HS Income
                           Black Female Price Sales
2 29 NV
          27.8
                 65.2
                       4563
                              5.7 49.3
                                         44.0
                              0.3 \ 51.1
                57.6
                                               265.7
3 30 NH 28.0
                       3737
                                         34.1
```

As we can see from the result, NV and NH are the two states that have outlying Sales observations in the regression model relating Sales to the six predictors.

(e)

Answer:

```
1 > results = lm(Sales ~ Age+HS+Income+Black+Female+Price , data=data)
2 > lev = hat(model.matrix(results))
3 > lev

1 0.148834504030601 0.580160351053579 0.0496985364502016 0.13709423363853
0.0601062187168606 0.130138939805311 0.174671432351856 0.109964259157845
0.719712840922186 0.2984807799694 0.0992462576906176 0.216903455841289
0.092060813754798 0.078138923121058 0.0863031077553889 0.0600834204236368
0.0600531614367214 0.229271714316211 0.147216983914844 0.0592277100717082
0.082438148474407 0.111768500306865 0.0788600537461464 0.0595424855799236
0.220268293959589 0.0538126742130819 0.07535749988127 0.0713061951148198
0.171156408722539 0.0663450574293963 0.112543589203342 0.205163482615724
0.125210794051503 0.189612219012305 0.0977942068782977 0.0427023659576899
0.0747312407280888 0.194824611487451 0.110848283936785 0.107728709447137
0.157387827636549 0.0702636797470909 0.0861059621640753 0.073209300335295
0.310573704010913 0.0646432821046025 0.121378178796484 0.06441386857486
0.139413729014416 0.0386706972156815 0.0845573052310269
```

According to the common rule we will flag any observation whose leverage value satisfies

$$h_{ii} > \frac{2p}{n} = \frac{12}{51}$$

```
1 > data [which (lev > 12/51) ,1]

2 > lev [lev > 12/51]

1 AK DC FL UT

2 0.580160351053579 0.719712840922186 0.2984807799694 0.310573704010913
```

Thus, according to the rule above, we get 4 states who have high leverage: AK, DC, FL, UT. (f)

Answer:

Typically, points with Cook's distance greater than 1 are classified as being influential, so we calculate Cook's distance for every state's data:

```
1 > cook = cooks.distance(results)
2 > cook
```

Then we get the 51 Cook's distance:

 $\begin{array}{c} 1 \quad 0.000872312260768373 \quad 0.11046568368098 \quad 0.000231406438616766 \quad 0.00533644985289951 \\ 0.00087184813943891 \quad 0.00487422897991362 \quad 0.000903689085754166 \quad 0.0247623942663158 \\ 0.272772360871267 \quad 0.00031718427842994 \quad 0.00228486844474409 \quad 0.149108047215374 \\ 0.00577305260600313 \quad 0.000515725336002152 \quad 0.000235292422912618 \quad 0.0022195814166927 \\ 0.0011742764662855 \quad 0.0293108038740074 \quad 0.0091907941594545 \quad 0.0046197884422297 \\ 0.00853949173434342 \quad 5.43666855436729e-05 \quad 0.000993543307494363 \\ 0.000416583654710988 \quad 0.00357717450931961 \quad 0.00181158830548335 \quad 0.00222167629931825 \\ 0.0106704252779454 \quad 0.226884733564416 \quad 0.243073931655456 \quad 0.00865807771956428 \\ 0.00862556323250348 \quad 0.0128750489379433 \quad 0.0514726373485391 \quad 0.000694147592466878 \\ 0.000198786969647856 \quad 0.000926126973805015 \quad 0.000632210801320141 \\ 0.00231792501997608 \quad 3.5406858359337e-07 \quad 0.00559710600247828 \quad 0.0021868920733631 \\ 0.000167678660476866 \quad 0.000276633855805063 \quad 0.0861896935150744 \quad 0.00441253690931487 \\ 0.0144781318896138 \quad 0.00554156138259945 \quad 0.00241683043673791 \quad 0.000216940322227759 \\ 6.00182901861485e-05 \end{array}$

No one is greater than 1, so there's no influential points according to the rule of Cook's distance. (g)

Answer:

```
1 > results = lm(log(Sales) \sim Age+HS+Income+Black+Female+Price, data=data)

2 > r = rstudent(results)

3 > data[abs(r)>3,]
```

```
State Age HS Income Black Female Price Sales
2 29 NV 27.8 65.2 4563 5.7 49.3 44.0 189.5
3 30 NH 28.0 57.6 3737 0.3 51.1 34.1 265.7
```

As we can see from the result, NV and NH are the two states that have outlying Sales observations in the regression model relating Sales to the six predictors.

```
1 > lev = hat(model.matrix(results))
2 > lev
```

According to the common rule we will flag any observation whose leverage value satisfies

$$h_{ii} > \frac{2p}{n} = \frac{12}{51}$$

```
1 > data [which (lev > 12/51), 1]

2 > lev [lev > 12/51]
```

```
1 AK DC FL UT
2 0.580160351053579 0.719712840922186 0.2984807799694 0.310573704010913
```

Thus, according to the rule above, we get 4 states who have high leverage: AK, DC, FL, UT. Typically, points with Cook's distance greater than 1 are classified as being influential, so we calculate Cook's distance for every state's data:

```
1 > cook = cooks.distance(results)
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```

Then we get the 51 Cook's distance:

 $\begin{array}{c} 0.00359045513224516 \quad 0.240240855616072 \quad 0.00121318532616218 \quad 0.00940000348486041 \\ 0.000293993996183841 \quad 0.000845445364141786 \quad 0.00157627217231795 \quad 0.0336654337125128 \\ 0.14134926250704 \quad 4.17359595508581e-08 \quad 0.00203727701223271 \quad 0.270758042867878 \\ 0.00458499785548776 \quad 0.000451889520957869 \quad 9.31888737750166e-06 \quad 0.00184184619189831 \\ 0.000560973161470141 \quad 0.0319246707978281 \quad 0.0204097590400288 \quad 0.00921415105332014 \\ 0.00810736995024783 \quad 7.12278615229615e-05 \quad 0.00254520116778151 \quad 0.0002981214100366 \\ 0.00317957208142376 \quad 0.00184483532854467 \quad 0.00116873114507587 \quad 0.0108404640748746 \\ 0.242062092944229 \quad 0.161220045757967 \quad 0.0123781360184546 \quad 0.0103388197355609 \\ 0.0176912765990876 \quad 0.0540788613509783 \quad 0.00205060932036119 \quad 4.12952664005199e-05 \\ 0.000879330434682632 \quad 0.0030802159952135 \quad 0.00441873438600284 \quad 8.57636871488496e-05 \\ 0.005679380081201 \quad 0.00398597075671328 \quad 0.000654080555535082 \quad 0.00040384707347726 \\ 0.238154414273449 \quad 0.00956732233083818 \quad 0.0132426216290245 \quad 0.00700748304948474 \\ 0.00221365370129141 \quad 0.000195642965139178 \quad 0.00154531793916012 \\ \end{array}$

No one is greater than 1, so there's no influential points according to the rule of Cook's distance.

2. (a)

Answer:

In order to test the hypothesis, we have a full model:

$$y_{ijk} = \mu + \alpha_B D_{i,B} + \alpha_C D_{i,C} + \beta_N D_{j,N} + \beta_O D_{j,O} + \beta_P D_{j,P} + \epsilon_{ij,k}$$

and a reduced model:

$$y_{ijk} = \mu + \beta_N D_{i,N} + \beta_O D_{i,O} + \beta_P D_{i,P} + \epsilon_{ij,k}$$

We will reject the Null Hypothesis if the two models are different:

```
> data = read.csv("/Users/lleiou/Google Drive/
                                                       Courses/4th term/Advanced-Data-
     Analysis/HW/Question/HW4/Oildata.csv")
2 > colnames (data)
3 > full = lm(Mileage ~ factor(Rgasoline) + factor(GasolineAd), data = data)
4 > reduce1 = lm(Mileage ~ factor(GasolineAd), data = data)
5 > anova (reduce1, full)
Res. Df RSS
                        Sum of Sq
                                               Pr(>F)
          3496.295
2 37
3 35
          3466.153
                        30.14234
                                    0.1521834 \quad 0.859396
```

Since the p-value of the test is $0.859396 > \alpha = 0.05$, we cannot reject the Null Hypothesis that $\alpha_B = \alpha_C = 0$ (b)

Answer:

In order to test the hypothesis, we have a full model:

$$y_{ijk} = \mu + \alpha_B D_{i,B} + \alpha_C D_{i,C} + \beta_N D_{j,N} + \beta_O D_{j,O} + \beta_P D_{j,P} + \epsilon_{ij,k}$$

and a reduced model:

$$y_{ijk} = \mu + \alpha_B D_{i,B} + \alpha_C D_{i,C} + \epsilon_{ij,k}$$

We will reject the Null Hypothesis if the two models are different:

```
> full = lm(Mileage ~ factor(Rgasoline) + factor(GasolineAd), data = data)
> reduce2 = lm(Mileage ~ factor(Rgasoline), data = data)
> anova(reduce2, full)
```

```
1 Res.Df RSS Df Sum of Sq F Pr(>F)
2 38 3592.151 NA NA NA NA
3 35 3466.153 3 125.9986 0.4240966 0.736912
```

Since the p-value of the test is $0.736912 > \alpha = 0.05$, we cannot reject the Null Hypothesis that $\beta_N = \beta_O = \beta_P = 0$