

HW2- Advanced Data Analysis

1. (4pt) Suppose you have three different feeds that may affect the size of eggs that chickens lay. You randomly assign 10 chickens to each one of the three feeds and record the size of the eggs (maximum length, in centimeters) that the chickens lay the following week. The null hypothesis is that all the chicken feeds have the same effect on the length of the major axis. The alternative is that the feed has some causal effect. A partial output is

| Source | df | SS | MS | F |
|--------|----|-------|----|---|
| feed | — | 23.43 | — | — |
| error | — | — | — | — |
| total | — | 28.10 | — | — |

- (a) (2pt) Complete the table above
- (b) (2pt) Test the null hypothesis is that all the chicken feeds have the same effect on the length of the major axis against the alternative is that the feed has some causal effect. Use $\alpha = 0.05$.
2. (10pt) Suppose you want to compare the types of popcorn popper and the brand of popcorn with respect to their yield (in terms of cups of popped corn). Factor A is the type of popper: oil-based versus air-based. Factor B is the brand of popcorn: gourmet versus national brand versus generic. For each combination of popper type and brand, you took three separate measurements. The ANOVA table is

| Source | df | SS | MS | F |
|-------------------|----|-------|----|---|
| Propper (A) | — | 4.5 | — | — |
| Corn (B) | — | 15.75 | — | — |
| Interaction (A*B) | — | — | — | — |
| Error | — | 1.67 | — | — |
| Total | — | 22.00 | — | — |

- (a) (2pt) Complete the table above.
- (b) (2pt) Test H_0 : No interaction against H_1 : there is an interaction, use $\alpha = 0.05$.
- (c) (2pt) It is decided to fit a model without an interaction and the partial results are

| Source | df | SS | MS | F |
|-------------|----|-------|----|---|
| Propper (A) | — | 4.5 | — | — |
| Corn (B) | — | 15.75 | — | — |
| Error | — | — | — | — |
| Total | — | 22.00 | | |

- (d) (2pt) Complete the table above.
- (e) (2pt) Test H_0 : No popper effect against H_1 : there is a popper effect. Use $\alpha = 0.05$
- (f) (2pt) Test H_0 : No corn effect against H_1 : there is a corn effect. Use $\alpha = 0.05$.
3. (6pt) In this exercise A and B are two fertilizers types, M, N, O and P are four wheat types and y_{ijk} values are wheat yields in bushels per plot (one third of an acre) corresponding to the different combinations of fertilizer type type and wheat type. Also, assume that this data was obtained by using a completely randomized experimental design. (see HW2data.csv)
- (a) (1pt) Construct an interaction plot? Does it suggest that there is an interaction between fertilizer type and wheat type?
- (b) (2pt) Test H_0 : No interaction against H_1 : there is an interaction, use $\alpha = 0.05$.
- (c) (1.5pt) Fit a model without an interaction and test H_0 : No fertilizer effect against H_1 : there is a fertilizer effect. Use $\alpha = 0.05$ if you reject H_0 , use Tukey's method to do pairwise comparisons of the different fertilizer types.
- (d) (1.5pt) Test H_0 : No wheat effect against H_1 : there is a wheat effect. Use $\alpha = 0.05$ if you reject H_0 , use Tukey's method to do pairwise comparisons of the different wheat types.