

## Feedback — II. Linear regression with one variable

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### Question 1

Consider the problem of predicting how well a student does in her second year of college/university, given how well they did in their first year. Specifically, let  $x$  be equal to the number of "A" grades (including A-, A and A+ grades) that a student receives in their first year of college (freshmen year). We would like to predict the value of  $y$ , which we define as the number of "A" grades they get in their second year (sophomore year).

Questions 1 through 4 will use the following training set of a small sample of different students' performances. Here each row is one training example. Recall that in linear regression, our hypothesis is  $h_{\theta}(x) = \theta_0 + \theta_1 x$ , and we use  $m$  to denote the number of training examples.

$x$	$y$
3	4
2	1
4	3
0	1

For the training set given above, what is the value of  $m$ ? In the box below, please enter your answer (which should be a number between 0 and 10).

You entered:

Your Answer

Score

Explanation

1

✖

0.00

Total

0.00 / 1.00

**Question Explanation**

$m$  is the number of training examples. In this example, we have  $m=4$  examples.

**Question 2**

For this question, continue to assume that we are using the training set given above. Recall our definition of the cost function was  $J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$ . What is  $J(0, 1)$ ? In the box below, please enter your answer (use decimals instead of fractions if necessary, e.g., 1.5).

**You entered:**

0.5

**Your Answer****Score****Explanation**

0.5

✔

1.00

Total

1.00 / 1.00

**Question Explanation**

When  $\theta_0 = 0$  and  $\theta_1 = 1$ , we have  $h_{\theta}(x) = \theta_0 + \theta_1 x = x$ . So,

$$\begin{aligned}
 J(\theta_0, \theta_1) &= \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2 \\
 &= \frac{1}{2 * 4} ((1)^2 + (1)^2 + (1)^2 + (1)^2) \\
 &= \frac{4}{8} \\
 &= 0.5
 \end{aligned}$$

**Question 3**

Suppose we set  $\theta_0 = -2, \theta_1 = 0.5$ . What is  $h_\theta(6)$ ?

You entered:

1

Your Answer	Score	Explanation
1	✓ 1.00	
Total	1.00 / 1.00	

#### Question Explanation

Setting  $x = 6$ , we have  $h_\theta(x) = \theta_0 + \theta_1 x = -2 + 0.5 * 6 = 1$

## Question 4

Let  $f$  be some function so that  $f(\theta_0, \theta_1)$  outputs a number. For this problem,  $f$  is some arbitrary/unknown smooth function (not necessarily the cost function of linear regression, so  $f$  may have local optima). Suppose we use gradient descent to try to minimize  $f(\theta_0, \theta_1)$  as a function of  $\theta_0$  and  $\theta_1$ . Which of the following statements are true? (Check all that apply.)

Your Answer	Score	Explanation
<input checked="" type="checkbox"/> If the learning rate is too small, then gradient descent may take a very long time to converge.	✓ 0.25	If the learning rate is small, gradient descent ends up taking an extremely small step on each iteration, and therefore can take a long time to converge.
<input type="checkbox"/> If $\theta_0$ and $\theta_1$ are initialized so that $\theta_0 = \theta_1$ , then by symmetry (because we do simultaneous updates to the two parameters), after one iteration of gradient descent, we will still have $\theta_0 = \theta_1$ .	✓ 0.25	The updates to $\theta_0$ and $\theta_1$ are different (even though we're doing simultaneous updates), so there's no particular reason to expect them to be the same after one iteration of gradient descent.

<input checked="" type="checkbox"/> If $\theta_0$ and $\theta_1$ are initialized at the global minimum, the one iteration will not change their values.	✓ 0.25	At the global minimum, the derivative (gradient) is zero, so gradient descent will not change the parameters.
<input type="checkbox"/> No matter how $\theta_0$ and $\theta_1$ are initialized, so long as $\alpha$ is sufficiently small, we can safely expect gradient descent to converge to the same solution.	✓ 0.25	This is not true, because depending on the initial condition, gradient descent may end up at different local optima.
Total	1.00 / 1.00	

## Question 5

Suppose that for some linear regression problem (say, predicting housing prices as in the lecture), we have some training set, and for our training set we managed to find some  $\theta_0, \theta_1$  such that  $J(\theta_0, \theta_1) = 0$ . Which of the statements below must then be true? (Check all that apply.)

Your Answer	Score	Explanation
<input type="checkbox"/> We can perfectly predict the value of $y$ even for new examples that we have not yet seen. (e.g., we can perfectly predict prices of even new houses that we have not yet seen.)	✓ 0.25	Even though we can fit our training set perfectly, this does not mean that we'll always make perfect predictions on houses in the future/on houses that we have not yet seen.
<input checked="" type="checkbox"/> Our training set can be fit perfectly by a straight line, i.e., all of our training examples lie	✓ 0.25	If $J(\theta_0, \theta_1) = 0$ , that means the line defined by the equation " $y = \theta_0 + \theta_1 x$ " perfectly fits all of our data.

perfectly on some straight line.

■ Gradient descent is likely to get stuck at a local minimum and fail to find the global minimum.



0.25

The cost function  $J(\theta_0, \theta_1)$  for linear regression has no local optima (other than the global minimum), so gradient descent will not get stuck at a bad local minimum.

■ For this to be true, we must have  $y^{(i)} = 0$  for every value of  $i = 1, 2, \dots, m$ .



0.25

So long as all of our training examples lie on a straight line, we will be able to find  $\theta_0$  and  $\theta_1$  so that  $J(\theta_0, \theta_1) = 0$ . It is not necessary that  $y^{(i)} = 0$  for all of our examples.

Total

1.00 /

1.00