The Malthusian Hypothesis

Ömer Özak

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Economic Growth and Comparative Development

Phases of Development: Standard of Living

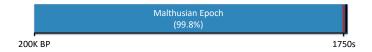
Phases of Development: Standard of Living

- The Malthusian Epoch
- The Post-Malthusian Regime

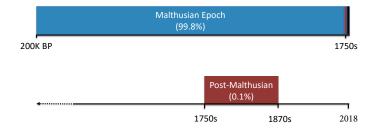
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- The Modern Growth Regime

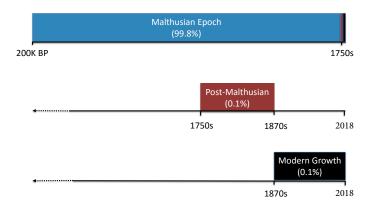
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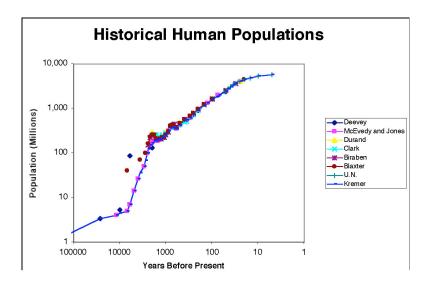
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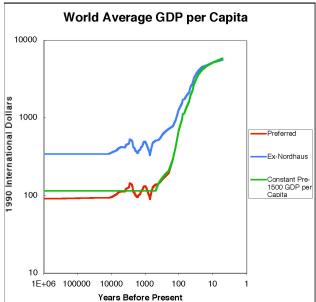
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 - Similar levels of income per-capita in the long-run

World Population 100,000 BP-1950CE



World GDP per capita 100,000 BP-1950CE

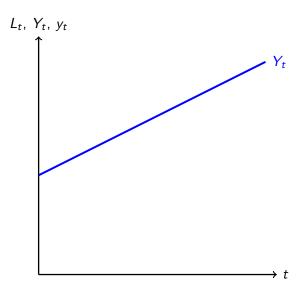


Malthus' Theory

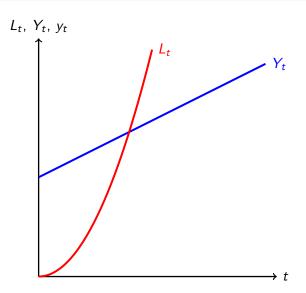
Population and income growth

"I think I may make fairly two postulata. First, that food is necessary to the existence of man. Secondly, that the passion between the sexes is necessary and will remain nearly in its present state ... Assuming then my postulata as granted, I say, that the power of population is infinitely greater than the power in the earth to produce subsistence for man. Population, when unchecked, increases in a geometrical ratio. Subsistence increases only in an arithmetical ratio. A slight acquaintance with numbers will show the immensity of the first power in comparison of the second. By the law of our nature which makes food necessary to the life of man, the effects of these two unequal powers must be kept equal. This implies a strong and constantly operating check on population from the difficulty of subsistence. This difficulty must fall somewhere and must necessarily be severely felt by a large portion of mankind...."

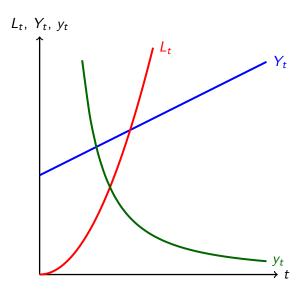
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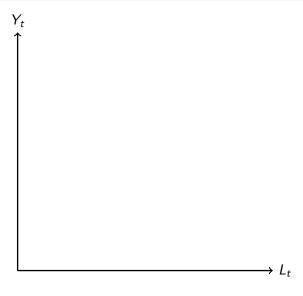
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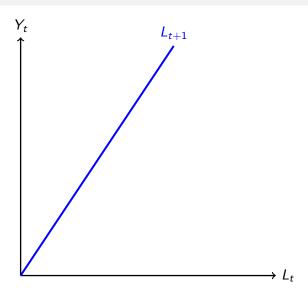


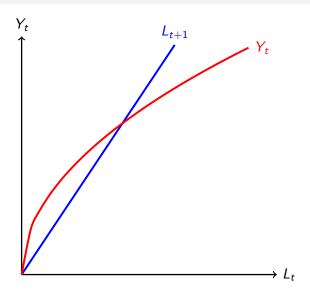
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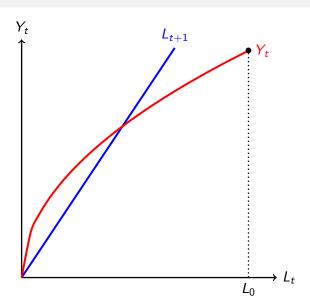
Population size constrained by resources

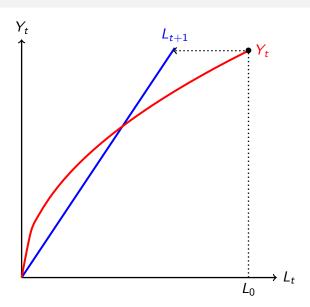
"This natural inequality of the two powers, of population, and of production in the earth, and that great law of our nature which must constantly keep their efforts equal, form the great difficulty that appears to me insurmountable in the way to the perfectibility of society...The checks which repress the superior power of population, and keep its effects on a level with the means of subsistence, are all resolvable into moral restraint, vice and misery.... this constantly subsisting cause of periodical misery has existed ever since we have had any histories of mankind, does exist at present, and will for ever continue to exist, unless some decided change takes place in the physical constitution of our nature."

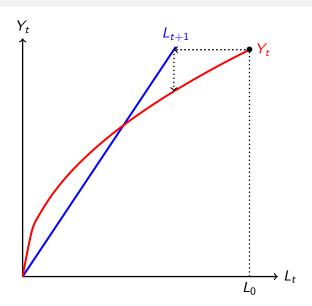


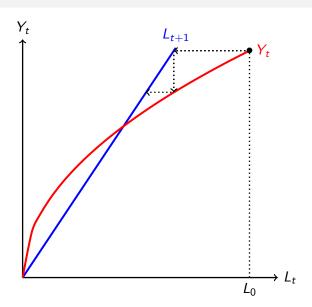


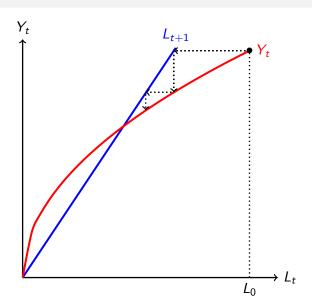


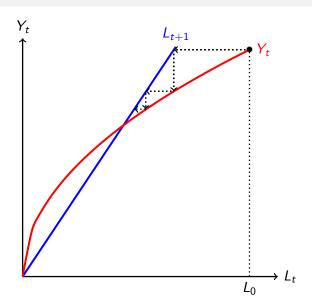


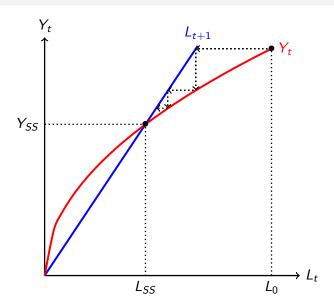


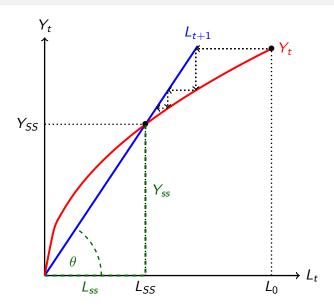




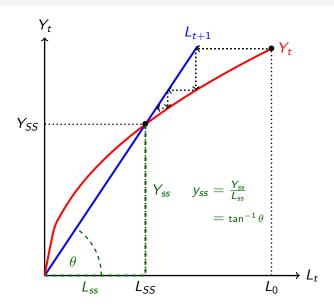








Population and income



Malthus' Theory

Dynamics for Living Creatures

"Among plants and animals the view of the subject is simple. They are all impelled by a powerful instinct to the increase of their species; and this instinct is interrupted by no reasoning, or doubts about providing for their offspring. Where ever therefore there is liberty, the power of increase is exerted; and the superabundant effects are repressed afterwards by want of room and nourishment, which is common to animals and plants; and among animals, by becoming prey of others".

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 - rat population explosion

Rat Attack!

Let's see this phenomenon unfold

- Matuam
- How it spreads
- Bamboo explosion
- Reproductive behavior
- Rat explosion

Malthus' Theory

Positive checks on population size

"are extremely various, and include every cause ... which in any degree contributes to shorten the natural duration of human life. Under this head, therefore, may be enumerated all unwholesome occupations, severe labour and exposure to the seasons, extreme poverty, bad nursing of children, great towns, excesses of all kinds, the whole train of common diseases and epidemics, wars, plague, and famine."

Malthus' Theory

• Preventive checks on population size

"Impelled to the increase of his species by an equally powerful instinct, reason interrupts his career, and asks him whether he may or not bring beings into the world, for whom he cannot provide the means of subsistence. . . . Will he not lower his rank in life? Will he not subject himself to greater difficulties than he at present feels? Will he not be obliged to labour harder? And if he has a large family, will his utmost exertions enable him to support them? May he not see his offspring in rags and misery, and clamoring for bread that he cannot give them?"

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 $1950 - 8.542$

4.3% population growth per year!

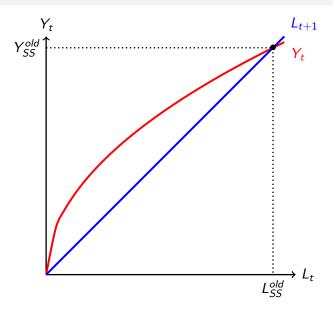
Population	Crude Birth Rate
Hutterites (1948)	45.9
Algeria (Moslems) (1949)	34.1
Jamaica (1948)	30.9
Israel (1948)	26.8
United States (1948)	24.2

Crude Birth Rate: births/1000 people

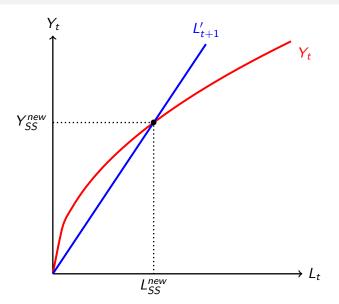
Population	Fertility Ratios
Hutterites (1948)	96.3
Algeria (Moslems) (1949)	63.
Jamaica (1948)	49.
Israel (1948)	45.8
United States (1948)	42.3

Fertility Ratio: Children under 5 years of age, per 100 females 15 to 49.

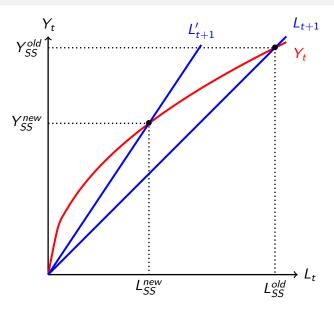
Effect of positive or preventive checks



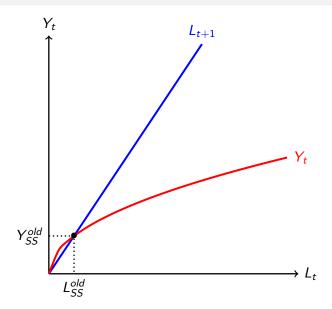
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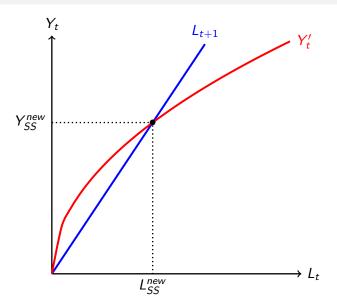
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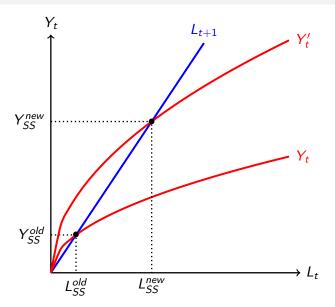
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Malthusian Dynamics - Prominent Examples

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 - (1M Famine death & 1M emigration to the New World)

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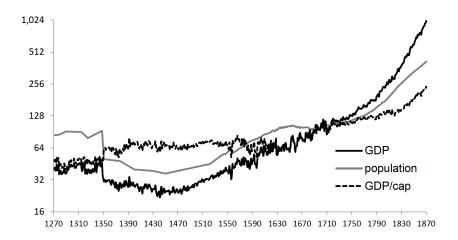
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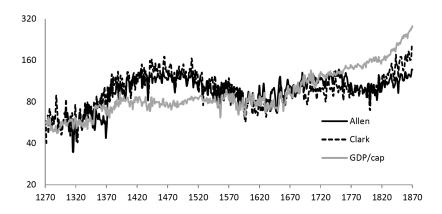
Malthusian Adjustments to the Black Death: England, 1348-1750CE



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- Population size affects technological progress, specialization and economies of scale

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 - \implies level not really important (of course "subsistence" is lower bound)

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- Output per worker produced at time t

$$y_t = \frac{Y_t}{L_t} =$$

$$Y_t = (AX)^{\alpha} L_t^{1-\alpha} \qquad 0 < \alpha < 1$$

- $L_t \equiv$ labor employed in period t
- $X \equiv land$
- $A \equiv$ technological level
- $AX \equiv$ effective resources
- Output per worker produced at time t

$$y_t = \frac{Y_t}{L_t} = \left[\frac{AX}{L_t}\right]^{\alpha}$$

• Land is fixed over time

- Land is fixed over time
 - Surface of planet earth

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- Labor evolves endogenously

- Land is fixed over time
 - Surface of planet earth
- Labor evolves endogenously
 - Determined by households' fertility rate

• Live for 2 period

- Live for 2 period
 - Childhood: (1st Period):

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 - Childhood: (1st Period):
 - Passive economic agents

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 - Consume fixed amount of their parental resources

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 - Consume fixed amount of their parental resources
 - Adulthood (2nd Period):
 - Work

- Live for 2 period
 - Childhood: (1st Period):
 - Passive economic agents
 - Consume fixed amount of their parental resources
 - Adulthood (2nd Period):
 - Work
 - Allocate income between consumption and children

Preferences and Budget Constraint

• Preferences of an adult at time t

$$u_t =$$

Preferences and Budget Constraint

Preferences of an adult at time t

$$u_t = (n_t)^{\gamma} (c_t)^{1-\gamma} \qquad \qquad 0 < \gamma < 1$$

Preferences and Budget Constraint

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Preferences of an adult at time t

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- Budget constraint:

$$\rho n_t + c_t \leq y_t$$

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$$u_t = (n_t)^{\gamma} (c_t)^{1-\gamma} \qquad \qquad 0 < \gamma < 1$$

- $n_t \equiv$ number of children of individual t
- ullet $c_t \equiv ext{ consumption of individual } t$
- Budget constraint:

$$\rho n_t + c_t \leq y_t$$

• $\rho \equiv {\rm cost} \ {\rm of} \ {\rm raising} \ {\rm a} \ {\rm child}$

$$c_t =$$

$$c_t = (1 - \gamma)$$

$$c_t = (1 - \gamma)y_t$$

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t =$$

$$c_t = (1 - \gamma)y_t$$

$$ho n_t = \gamma$$

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

• Optimal expenditure on consumption and children

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$$n_t = \frac{\gamma}{\rho}$$

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$$\rho n_t = \gamma y_t$$

$$n_t = \frac{\gamma}{\rho} y_t =$$

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$$\rho n_t = \gamma y_t$$

$$n_t = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho}$$

• Optimal expenditure on consumption and children

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

$$n_t = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

• Optimal expenditure on consumption and children

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

Optimal number of children

$$n_t = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

• Since $y_t = (AX/L_t)^{\alpha}$

$$L_{t+1} =$$

$$L_{t+1}=n_t$$

$$L_{t+1} = n_t L_t$$

• The evolution of the size of the working population

$$L_{t+1} = n_t L_t$$

where

$$n_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

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• The evolution of the size of the working population

$$L_{t+1} = n_t L_t$$

where

$$n_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

$$L_{t+1} = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha} L_t = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

$$L_{t+1} = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

The evolution of the size of the working population

$$L_{t+1} = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• Steady-State: $L_{t+1} = L_t = \bar{L}$

• The evolution of the size of the working population

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$$\bar{L} = \frac{\gamma}{\rho} (AX)^{\alpha} \bar{L}^{1-\alpha}$$

• The steady-state level of the size of the working population

$$\bar{L} =$$

The evolution of the size of the working population

$$L_{t+1} = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• Steady-State: $L_{t+1} = L_t = \bar{L}$

$$\bar{L} = \frac{\gamma}{\rho} (AX)^{\alpha} \bar{L}^{1-\alpha}$$

• The steady-state level of the size of the working population

$$\bar{L} = (\frac{\gamma}{\rho})^{1/\alpha} (AX)$$

The evolution of the size of the working population

$$L_{t+1} = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

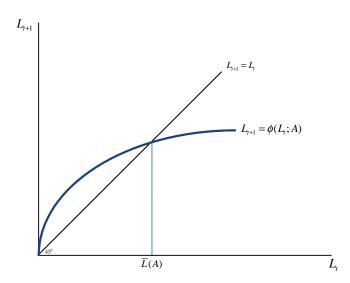
• Steady-State: $L_{t+1} = L_t = \bar{L}$

$$\bar{L} = \frac{\gamma}{\rho} (AX)^{\alpha} \bar{L}^{1-\alpha}$$

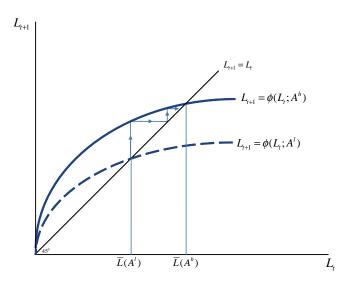
• The steady-state level of the size of the working population

$$ar{L} = (rac{\gamma}{
ho})^{1/lpha}(AX) \equiv ar{L}(A)$$

Population Dynamics



Adjustment of Population to Advancements in Technology



$$y_{t+1} =$$

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha}$$

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha}$$

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

The time path of income per worker

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

$$n_t = \frac{\gamma}{\rho} y_t$$

• The time path of income per worker

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

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$$n_t = \frac{\gamma}{\rho} y_t$$

$$y_{t+1} = = \frac{y_t}{n_t^{\alpha}} =$$

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$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

$$n_{t} = \frac{\gamma}{\rho} y_{t}$$

$$y_{t+1} = \frac{y_{t}}{n_{t}^{\alpha}} = \frac{y_{t}}{\left[\frac{\gamma}{\rho}\right]^{\alpha} y_{t}^{\alpha}}$$

The time path of income per worker

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

where

$$n_{t} = \frac{\gamma}{\rho} y_{t}$$

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$$y_{t+1} = \left[\frac{
ho}{\gamma}\right]^{lpha}$$

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$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha}$$

The time path of income per worker

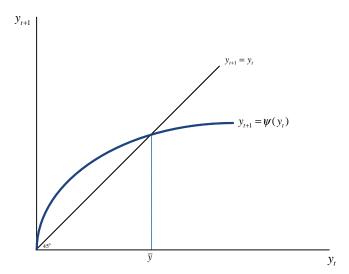
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$$y_{t+1} = \left[\frac{
ho}{\gamma}\right]^{lpha} y_t^{1-lpha} \equiv \psi(y_t)$$



$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha}$$

The time path of income per worker

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha}$$

• Steady-State $y_{t+1} = y_t = \bar{y}$

$$\bar{y} =$$

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The time path of income per worker

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The steady-state level of income per worker

$$\bar{y} =$$

The time path of income per worker

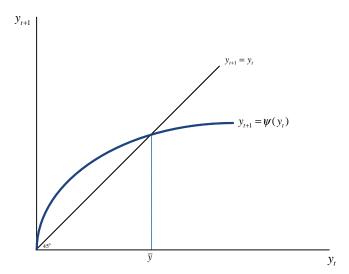
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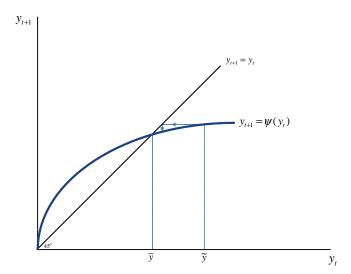
$$\bar{y} = \left[\frac{\rho}{\gamma}\right]^{\alpha} \bar{y}^{1-\alpha}$$

The steady-state level of income per worker

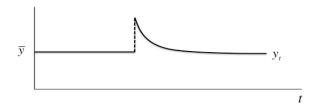
$$\bar{\mathbf{y}} = \left[\frac{\rho}{\gamma}\right]$$

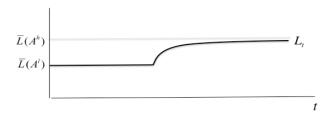


The Effect of Technological Advancement on income per Worker



The Effect of Technological Advancement on the Time Path of Population and Income per Worker





The Effect of Advancement in Technology or Land Productivity

 Increases the short-run and the steady-state level of the working population

$$\frac{\partial L_t}{\partial A} > 0$$
 and $\frac{\partial \bar{L}}{\partial A} > 0$

 Increases the level of income per capita in the short-run but does not affect the steady-state levels of income per worker

$$\frac{\partial y_t}{\partial A} > 0$$
 and $\frac{\partial \bar{y}}{\partial A} = 0$

• Variations in technology and land quality across countries will be reflected primarily in variation in population density:

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 - Technological superiority will result primarily in higher population density without any sizable effect on income per-capita in the long-run

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 - Technological superiority will result primarily in higher population density without any sizable effect on income per-capita in the long-run
 - Superior land quality will result primarily in higher population density without any sizable effect on income per-capita in the long-run

Empirical Hurdles

• Objective:

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 - Omitted Variables Bias:
 - 3rd factor (e.g., ability) affected Population & Technology

• Exploit exogenous sources of cross-country variation in technological level

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 - unaffected by the population in 1500

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 - Historical origins (thousands of years earlier):
 - unaffected by the population in 1500
 - Exogenous source of variations in these historical forces

• The transition from hunter-gatherer tribes to agricultural communities:

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 - Emergence of non-food-producing class:

- The transition from hunter-gatherer tribes to agricultural communities:
 - Emergence of non-food-producing class:
 - $\bullet \implies \mathsf{Knowledge} \ \mathsf{creation} \ (\mathsf{science}, \ \mathsf{technology} \ \& \ \mathsf{written} \ \mathsf{languages})$

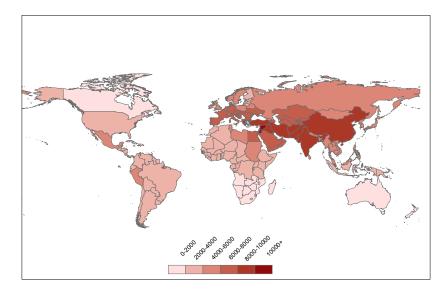
- The transition from hunter-gatherer tribes to agricultural communities:
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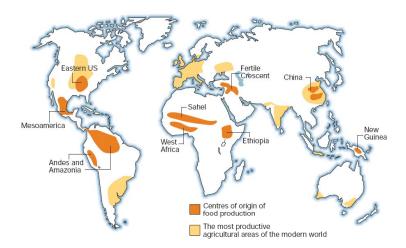
- The transition from hunter-gatherer tribes to agricultural communities:
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 - Technological head start and its persistent effect via:
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- Variations in biogeographical characteristics conducive for the NR :
 - \Longrightarrow Origins of the observed patterns of comparative development

Variation in the Onset of the Neolithic Revolution



Independent Origins



 Geographical factors that maximized biodiversity (climate, latitude, landmass)

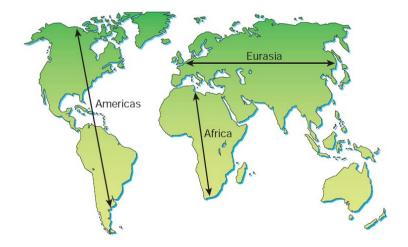
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 - Availability of domesticable species of plants and animals
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- Orientation of continents:
 - \Longrightarrow Diffusion of agricultural practices along similar latitudes

Orientation of Continents



• The domination of Euro-Asia in the pre-colonial era reflects:

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 - Larger number of domesticable species of plants and animals
 - East-West orientation
 - ullet Technological head start and its effect on development
- Earlier onset of the Neolithic Revolution:
 - Technological superiority

• Resolving: reverse causality

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 - Variation in the onset of the Neolithic Revolution (NR) across the globe - a proxy for variation in the technological level
- Resolving: omitted variable bias (i.e., 3rd factor (e.g., ability)) affected population & NR
 - Variation in prehistoric domesticable species of plants and animals IV for the timing of the NR

The Neolithic Revolution & Technological Level: 1000 BCE-1500 CE

	Technology Level 1000BCE-1500CE						
	1000BCE		1CE		1500CE		
	(1)	(2)	(3)	(4)	(5)	(6)	
Years Since Neolithic Revolution	0.72***	0.47***	0.56***	0.28**	0.74***	0.34***	
	(0.06)	(0.12)	(0.06)	(0.12)	(0.06)	(0.10)	
Continental FE	No	Yes	No	Yes	No	Yes	
Additional Geographical Controls	No	Yes	No	Yes	No	Yes	
Adjusted- R^2	0.51	0.60	0.31	0.63	0.55	0.82	
Observations	112	111	134	133	113	112	

Notes: Standardized coefficients from an Ordinary Least Squares (OLS) regression. Heteroskedasticity robust standard error estimates are reported in parentheses; *** denotes statistical significance at the 1% level, ** at the 5% level, and * at the 10% level, all for two-sided hypothesis tests.

$$\ln P_{i,t} = \alpha_{0,t} + \alpha_{1,t} \ln T_{i,t} + \alpha_{2,t} \ln X_i + \alpha'_{3,t} \Gamma_i + \alpha'_{4,t} D_i + \delta_{i,t}$$

$$\ln y_{i,t} = \beta_{0,t} + \beta_{1,t} \ln T_{i,t} + \beta_{2,t} \ln X_i + \beta'_{3,t} \Gamma_i + \beta'_{4,t} D_i + \varepsilon_{i,t}$$

• $P_{i,t} \equiv$ population density of country i in year t

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- $\Gamma_i \equiv$ vector of geographical controls for country i
- $D_i \equiv$ vector of continental fixed effect in country i

Determinants of Population Density in 1500 CE

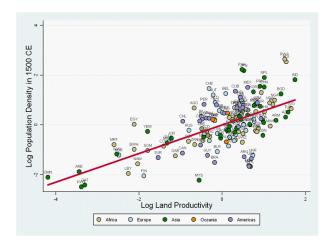
OLS OLS Dependent V 33*** 298) 0.587*** (0.071) -0.425***	OLS ariable: Log p 1.025)*** (0.223 0.641*** (0.059) -0.353***	OLS opulation dens 1.087*** (0.184) 0.576*** (0.052)	1.389*** (0.224) 0.573*** (0.095)	2.077*** (0.391) 0.571*** (0.082)
0.587*** (0.071) 0.425***	1.025)*** (0.223 0.641*** (0.059)	1.087*** (0.184) 0.576*** (0.052)	1.389*** (0.224) 0.573*** (0.095)	2.077*** (0.391) 0.571***
0.587*** (0.071) -0.425***	(0.223 0.641*** (0.059)	(0.184) 0.576*** (0.052)	(0.224) 0.573*** (0.095)	(0.391) 0.571***
(0.071) -0.425***	(0.059)	(0.052)	(0.095)	
	-0.353***			
(0.124)	(0.104)	-0.314*** (0.103)	-0.278** (0.131)	-0.248** (0.117)
		-0.392*** (0.142)	0.220 (0.346)	0.250 (0.333)
		0.899*** (0.282)	1.185*** (0.377)	1.350*** (0.380)
Yes Yes .47 147	Yes 147	Yes 147	Yes 96	Yes 96
.40 0.60	0.66	0.73	0.73	0.70
				14.65
				0.44
	.47 147 .40 0.60	47 147 147 .40 0.60 0.66	(0.142) 0.899*** (0.282) 7es Yes Yes Yes 47 147 147 147 .40 0.60 0.66 0.73	(0.142) (0.346) 0.899*** 1.185*** (0.282) (0.377) Ves Yes Yes Yes Yes 47 147 147 147 96

Effects on Income per Capita versus Population Density

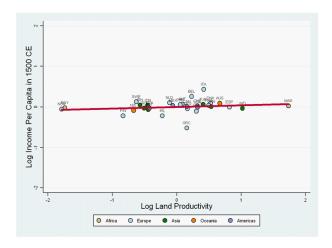
	OLS (1)	OLS (2)	OLS (3)	OLS (4)	OLS (5)	OLS (6)
	Log Income Per Capita in			Log Population Density in		
	1500 CE	1000 CE	1 CE	1500 CE	1000 CE	1 CE
Log years since Neolithic	0.159 (0.136)	0.073 (0.045)	0.109 (0.072)	1.337** (0.594)	0.832** (0.363)	1.006** (0.483)
Log land productivity	0.041 (0.025)	- 0.021 (0.025)	- 0.001 (0.027)	0.584*** (0.159)	0.364*** (0.110)	0.681** (0.255)
Log absolute latitude	-0.041 (0.073)	0.060 (0.147)	-0.175 (0.175)	0.050 (0.463)	-2.140 ** (0.801)	-2.163 ** (0.979)
Distance to nearest coast or river	0.215 (0.198)	-0.111 (0.138)	0.043 (0.159)	-0.429 (1.237)	-0.237 (0.751)	0.118 (0.883)
% land within 100 km of coast or river	0.124 (0.145)	-0.150 (0.121)	0.042 (0.127)	1.855** (0.820)	1.326 ** (0.615)	0.228 (0.919)
Continental dummies	Yes	Yes	Yes	Yes	Yes	Yes
Observations	31	26	29	31	26	29
R ²	0.66	0.68	0.33	0.88	0.95	0.89

Ömer Özak

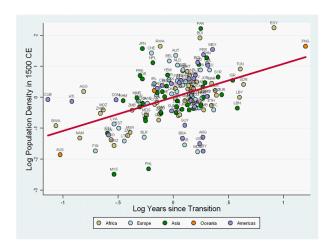
Land Productivity and Population Density in 1500



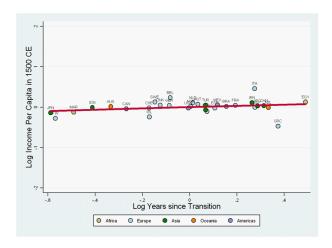
Land Productivity and Income per Capita in 1500



Technology and Population Density in 1500



Technology and Income per Capita in 1500



Robustness to the inclusion of direct measures of technology

- Robustness to the inclusion of direct measures of technology
 - Exploit variation in a direct measure of the technology level

- Robustness to the inclusion of direct measures of technology
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 - Variation in prehistoric biogeographic endowments IV for this direct measure of technology

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- Robustness to the distance from the technological frontier

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 - Exploit variation in a direct measure of the technology level
 - Variation in prehistoric biogeographic endowments IV for this direct measure of technology
- Robustness to the distance from the technological frontier
- Robustness to the exclusion of unobserved time-invariant country fixed effects

- Robustness to the inclusion of direct measures of technology
 - Exploit variation in a direct measure of the technology level
 - Variation in prehistoric biogeographic endowments IV for this direct measure of technology
- Robustness to the distance from the technological frontier
- Robustness to the exclusion of unobserved time-invariant country fixed effects
 - First-difference estimation strategy (with a lagged explanatory variable)

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 - First-difference estimation strategy (with a lagged explanatory variable)
 - The effect of changes in the level of technology in 1000 BCE-1 CE on population density and income per capita in 1-1000CE

Robustness to Direct Measures of Technological Level

	OLS	OLS	OLS	OLS	OLS	OLS		
	(1)	(2)	(3)	(4)	(5)	(6)		
			Dependent					
		pulation	Log Inco		Log Pop			
		Density in:		Capita in:		ty in:		
	1000 CE	1 CE	1000 CE	1 CE	1000 CE	1 CE		
Log Technology Index in Relevant Period	4.315*** (0.850)	4.216*** (0.745)	0.064 (0.230)	0.678 (0.432)	12.762*** (0.918)	7.461** (3.181)		
Log land productivity	0.449*** (0.056)	0.379*** (0.082)	-0.016 (0.030)	0.004 (0.033)	0.429** (0.182)	0.725** (0.303)		
Log absolute latitude	-0.283** (0.120)	-0.051 (0.127)	0.036 (0.161)	-0.198 (0.176)	-1.919*** (0.576)	-2.350*** (0.784)		
Distance to nearest coast or river	-0.638*** (0.188)	-0.782*** (0.198)	-0.092 (0.144)	0.114 (0.164)	0.609 (0.469)	0.886 (0.904)		
% land within 100 km of coast or river	0.385 (0.313)	0.237 (0.329)	-0.156 (0.139)	0.092 (0.136)	1.265** (0.555)	0.788 (0.934)		
Continental dummies	Yes	Yes	Yes	Yes	Yes	Yes		
Observations	140	129	26	29	26	29		
R ²	0.61	0.62	0.64	0.30	0.97	0.88		
Notes: Robus	Notes: Robust standard errors in parentheses; *** p<0.01, ** p<0.05, * p<0.1							

The Causal Effect of Technological Level on Population Density

	OLS	OLS	IV	OLS	OLS	IV
	(1)	(2)	(3)	(4)	(5)	(6)
		Depend	lent Variable:	Population De	ensity in:	
		1000CE			1CE	
Log Technology Index in Relevant Period	4.315*** (0.850)	4.198*** (1.164)	14.530*** (4.437)	4.216*** (0.745)	3.947*** (0.983)	10.798*** (2.857)
Log land productivity	0.449*** (0.056)	0.498*** (0.139)	0.572*** (0.148)	0.379*** (0.082)	0.350** (0.172)	0.464** (0.182)
Log absolute latitude	-0.283** (0.120)	-0.185 (0.151)	-0.209 (0.209)	-0.051 (0.127)	0.083 (0.170)	-0.052 (0.214)
Distance to nearest coast or river	-0.638*** (0.188)	-0.363 (0.426)	-1.155* (0.640)	-0.782*** (0.198)	-0.625 (0.434)	-0.616 (0.834)
% land within 100 km of coast or river	0.385 (0.313)	0.442 (0.422)	0.153 (0.606)	0.237 (0.329)	0.146 (0.424)	-0.172 (0.642)
Continental dummies	Yes	Yes	Yes	Yes	Yes	Yes
Observations	140	92	92	129	83	83
R ²	0.61	0.55	0.13	0.62	0.58	0.32
First-stage F-statistic			12.52			12.00
Overid. p-value			0.941			0.160
Notes: Robus	t standard err	ors in parenth	eses; *** p<0	0.01, ** p<0.0!	5, * p<0.1	

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Robustness to Technology Diffusion and other Geographic Characteristics

	(1)	(2)	(3)	(4)	(5)	(6)
	Log Population Density in 1500		Log Income Per Capita in 1500		Log Population Density in 1500	
Log Technology Index in Relevant Period	0.828*** (0.208)	0.877*** (0.214)	0.117 (0.221)	0.103 (0.214)	1.498** (0.546)	1.478** (0.556)
Log land productivity	0.559*** (0.048)	0.545*** (0.063)	0.036 (0.032)	0.047 (0.037)	0.596*** (0.123)	0.691*** (0.122)
Log Distance to Frontier	-0.186*** (0.035)	-0.191*** (0.036)	-0.005 (0.011)	-0.001 (0.013)	-0.130* (0.066)	-0.108* (0.055)
Small Island Dummy	0.067 (0.582)	0.086 (0.626)	-0.118 (0.216)	-0.046 (0.198)	1.962** (0.709)	2.720*** (0.699)
Landlocked Dummy	0.131 (0.209)	0.119 (0.203)	0.056 (0.084)	0.024 (0.101)	1.490*** (0.293)	1.269*** (0.282)
% Land in Temperate Climate Zones		-0.196 (0.513)		-0.192 (0.180)		-1.624* (0.917)
Continental dummies	Yes	Yes	Yes	Yes	Yes	Yes
Observations	147	147	31	31	31	31
R ²	0.76	0.76	0.67	0.67	0.94	0.96

Malthusian Hypothesis

Population levels positively associated with

- Population levels positively associated with
 - Technology

- Population levels positively associated with
 - Technology
 - Land Productivity

- Population levels positively associated with
 - Technology
 - Land Productivity
- Income per capita levels

- Population levels positively associated with
 - Technology
 - Land Productivity
- Income per capita levels
 - Independent of both

- Population levels positively associated with
 - Technology
 - Land Productivity
- Income per capita levels
 - Independent of both
 - Determined by preferences for children