

Formatted Async 3 Code

Introduction

In this code we're going to work through an extended example that demonstrates how randomization inference works. We hope that at the end of this section you are able to:

1. Understand the sharp null hypothesis
2. Apply randomization inference to produce a sharp null distribution of the focal test-statistic, the *ATE*
3. Produce and evaluate probabilistic statements of belief about the plausibility of the sharp-null hypothesis

Three Inferential Paradigms

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1. Frequentist Inference
2. Bayesian Inference
3. Fisherian Inference

Frequentist Inference

- Theoretically unappealing
 - $P(Data \mid \text{Null Hypothesis}) \neq P(\text{Hypothesis} \mid Data)$
 - Requires assumptions that are frequently implausible
- Analytically challenging

$$\int_{-\infty}^x \frac{e^{\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}}{\sigma\sqrt{2\pi}}, \text{ is hard.}$$

- Computationally solved
 - Look in the back of any book; or,
 - `pnorm`, `pt`, `pf`, `pchisq`

Bayesian Inference

- Theoretically appealing
 - $P(\text{Hypothesis} \mid \text{Data}) \propto P(\text{Data} \mid \text{Hypothesis}) * P(\text{Hypothesis})$
 - Though requires potentially controversial statement of prior beliefs about $P(\text{Hypothesis})$
- Analytically challenging
 - Correctly specifying priors so they are both (a) plausible; and (b) conjugate with Likelihood statement requires skill
- Computationally challenging
 - Sampling likelihood space requires informed, principled samplers (e.g. Metropolis, Gibbs) that require cycles

- Theoretically unappealing
 - $P(Data \mid \text{Sharp Null Hypothesis}) \neq P(\text{Hypothesis} \mid Data)$
- Analytically simple
- Computationally Straightforward