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1 Math

1.1 FindPrime

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 //查找[0, 2^15]中的所有質數 共有3515
5
6 const int MAXN = 32768; //2^15=32768
7 bool primes[MAXN];
8 vector<int> p; //3515
9
10 //質數篩法 Sieve of Eratosthenes
11 inline void findPrimes() {
12     for (int i = 0; i < MAXN; i++) {
13         primes[i] = true;
14     }
15     primes[0] = false;
16     primes[1] = false;
17     for (int i = 4; i < MAXN; i += 2) {
18         //將2的倍數全部刪掉(偶數不會是質數)
19         primes[i] = false;
20     }
21     //開始逐個檢查--->小心i*i會有overflow問題--->使用long
22     for (long long i = 3; i < MAXN; i += 2) {
23         if (primes[i]) {
24             //如果之前還未被刪掉 才做篩法
25             for (long long j = i * i; j < MAXN; j += i) {
26                 //從i*i開始(因為i*2, i*3...都被前面處理完了)
27                 primes[j] = false;
28             }
29         }
30     }
31     //搜集所有質數
32     for (int i = 0; i < MAXN; i++) {
33         if (primes[i]) {
34             p.emplace_back(i);
35         }
36     }
37 }

```

2 Graph

2.1 Kruskal

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 //節點從0號開始
5 struct Edge {
6     int v, w, wt;
7     Edge(int a, int b, int c) {
8         v = a;

```

```

9         w = b;
10        wt = c;
11    }
12    bool operator<(const Edge &e) const {
13        return wt < e.wt;
14    }
15 };
16
17 const int maxN = 100000 + 5; //最多maxN個節點
18 int V, E; //有V個節點E條邊
19 int parent[maxN];
20 vector<Edge> edges;
21
22 int do_find(int p) {
23     while (parent[p] >= 0) {
24         p = parent[p];
25     }
26     return p;
27 }
28
29 void do_union(int p, int q) {
30     if (parent[p] > parent[q]) {
31         parent[q] += parent[p];
32         parent[p] = q;
33     } else {
34         parent[p] += parent[q];
35         parent[q] = p;
36     }
37 }
38
39 void init() {
40     edges.clear();
41     for (int i = 0; i < V; i++) {
42         parent[i] = -1;
43     }
44 }
45
46 int kruskal() {
47     sort(edges.begin(), edges.end());
48     int mstWeight = 0;
49     int pRoot, qRoot;
50     for (auto e : edges) {
51         pRoot = do_find(e.v);
52         qRoot = do_find(e.w);
53         if (pRoot != qRoot) {
54             mstWeight += e.wt;
55             do_union(pRoot, qRoot);
56         }
57     }
58     return mstWeight;
59 }
60
61 int main() {
62     int ta, tb, tc;
63     while (~scanf("%d %d", &V, &E)) {
64         init();
65         for (int i = 0; i < E; i++) {
66             scanf("%d %d %d", &ta, &tb, &tc);
67             edges.push_back({ta, tb, tc});
68         }
69         printf("%d\n", kruskal());
70     }
71     return 0;
72 }

```

2.2 Dijkstra

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 //節點從1號開始
5 struct Edge {
6     int v, wt;
7     Edge(int a, int c) {
8         v = a;

```

```

9      wt = c;
10  }
11  Edge() {}
12 };
13 struct Info {
14     int v;
15     int wt;
16     Info(int a, int b) : v(a), wt(b) {}
17     Info() {}
18
19     bool operator<(const Info &i) const {
20         return wt > i.wt;
21     }
22 };
23
24 const int maxN = 100000 + 5; // 最多maxN個節點
25 int V, E; // 有V個節點E條邊
26 vector<Edge> g[maxN];
27 vector<bool> visied(maxN);
28 vector<int> dis(maxN);
29 priority_queue<Info> pq;
30
31 void init() {
32     for (int i = 0; i < V; i++) {
33         g[i].clear();
34         visied[i] = false;
35         dis[i] = 0x3f3f3f;
36     }
37     while (!pq.empty()) {
38         pq.pop();
39     }
40 }
41
42 void dijkstra(int s) {
43     Info info;
44     dis[s] = 0;
45     visied[s] = true;
46     pq.push({s, 0});
47
48     while (!pq.empty()) {
49         info = pq.top();
50         pq.pop();
51         visied[info.v] = true;
52         if (dis[info.v] > info.wt) {
53             dis[info.v] = info.wt;
54         }
55         for (auto e : g[info.v]) {
56             if (!visied[e.v]) {
57                 pq.push({e.v, dis[info.v] + e.wt});
58             }
59         }
60     }
61 }
62
63 int main() {
64     int ta, tb, tc;
65     while (~scanf("%d %d", &V, &E)) {
66         init();
67         while (E--) {
68             scanf("%d %d %d", &ta, &tb, &tc);
69             g[ta].push_back({tb, tc});
70             g[tb].push_back({ta, tc});
71         }
72         dijkstra(1); // 從1號節點開始
73     }
74     return 0;
75 }

```

2.3 BellmanFord

```

1 #include <bits/stdc++.h>
2 using namespace std;
3 //節點從0開始(適用於無向圖)
4 //備註:如果圖為無向圖且包含負權邊 則必定有負權環
5 struct Edge {

```

```

6     int f, t, wt;
7     Edge() {}
8     Edge(int a, int b, int c) {
9         f = a;
10        t = b;
11        wt = c;
12    }
13 };
14
15 const int maxN = 100000; //最多maxN個節點
16 int V, E; //有V個節點E條邊
17 vector<vector<Edge>> G(maxN);
18 vector<int> distTo(maxN); //到節點i的權重
19 bool hasNegativeCycle;
20 Edge e;
21
22 void init() {
23     for (int i = 0; i < V; i++) {
24         G[i].clear();
25         distTo[i] = 0x3f3f3f;
26     }
27 }
28
29 bool detectHasCycle() {
30     for (int i = 0; i < V; i++) {
31         for (int j = 0; j < G[i].size(); j++) {
32             e = G[i][j];
33             if (distTo[e.f] + e.wt < distTo[e.t]) {
34                 return true;
35             }
36         }
37     }
38     return false;
39 }
40
41 void bellmanFord(int s) { //從s點開始
42     distTo[s] = 0;
43     //執行節點-1次鬆弛
44     for (int pass = 1; pass < V; pass++) {
45         for (int i = 0; i < V; i++) {
46             for (int j = 0; j < G[i].size(); j++) {
47                 e = G[i][j];
48                 if (distTo[e.f] + e.wt < distTo[e.t]) {
49                     distTo[e.t] = distTo[e.f] + e.wt;
50                 }
51             }
52         }
53     }
54     //檢測負權環
55     hasNegativeCycle = detectHasCycle();
56 }
57
58 int main() {
59     while (~scanf("%d %d", &V, &E)) {
60         init();
61         for (int i = 0; i < E; i++) { //無向圖
62             scanf("%d %d %d", &e.f, &e.t, &e.wt);
63             G[e.f].push_back(e);
64         }
65         bellmanFord(0); //從節點0開始
66         if (!hasNegativeCycle) {
67             for (int i = 0; i < V; i++) {
68                 printf("%d ", distTo[i]);
69             }
70             printf("\n");
71         } else {
72             printf("Has Negative Cycle.");
73         }
74     }
75     return 0;
76 }

```

2.4 FloydWarshall

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 const int maxN = 100000;
5 int V, E;           //有V個節點E個邊
6 int G[maxN][maxN];  // adjacency matrix
7 int d[maxN][maxN];  // 最短路徑長度
8
9 void floyd_warshall() {
10     for (int i = 0; i < V; i++) {
11         for (int j = 0; j < V; j++) {
12             d[i][j] = G[i][j];
13         }
14     }
15
16     for (int i = 0; i < V; i++) {
17         d[i][i] = 0;
18     }
19
20     for (int k = 0; k < V; k++) {
21         // 嘗試每一個中繼點
22         for (int i = 0; i < V; i++) {
23             // 計算每一個i點與每一個j點
24             for (int j = 0; j < V; j++) {
25                 if (d[i][k] + d[k][j] < d[i][j]) {
26                     d[i][j] = d[i][k] + d[k][j];
27                 }
28             }
29         }
30     }
31 }
32
33 int main() {
34     int ta, tb, tc;
35     while (~scanf("%d %d", &V, &E)) {
36         memset(G, 0, sizeof(G));
37         memset(d, 0, sizeof(d));
38         for (int i = 0; i < E; i++) {
39             scanf("%d %d %d", &ta, &tb, &tc);
40             G[ta][tb] = tc;
41             G[tb][ta] = tc;
42         }
43         floyd_warshall();
44         //輸出所有點對點的權重
45         for (int i = 0; i < V; i++) {
46             for (int j = 0; j < V; j++) {
47                 printf("V[%d] to V[%d] dis=%d\n", i,
48                     j, d[i][j]);
49             }
50         }
51         return 0;
52 }

```

```

16 }
17 //前綴和 [1,x]
18 int query(int x) {
19     int ret = 0;
20     while (x) {
21         ret += bit[x];
22         x -= x & (-x);
23     }
24     return ret;
25 }
26
27 // 區間和 [l,r]
28 int rSum(int l, int r) {
29     return query(r) - query(l - 1);
30 }
31
32 int main() {
33     memset(bit, 0, sizeof(bit));
34     vector<int> v = {0x3f3f3f, 1, 2, 3, 4, 5};
35     dataSize = v.size() - 1; // v[0]不使用
36     for (int i = 1; i < v.size(); i++) { //放入v[1,5]
37         update(i, v[i]);
38     }
39     printf("%d\n", rSum(2, 4)); // v[2,4]=2+3+4=9
40     return 0;
41 }

```

3 DataStructure

3.1 BitIndexTree

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 // bit陣列索引從1開始
5 const int maxN = 100000 + 5; // bit最大容量
6 int bit[maxN];
7 //放入的資料量
8 int dataSize;
9
10 //更新bit[x]的值(加d)
11 void update(int x, int d) {
12     while (x <= dataSize) {
13         bit[x] += d;
14         x += x & (-x);
15     }

```