

$$X(\lambda\pi) = \lambda \begin{bmatrix} x_1 \\ y_1 \\ z_1 \\ t_1 \end{bmatrix} + (1-\lambda) \begin{bmatrix} x_2 \\ y_2 \\ z_2 \\ t_2 \end{bmatrix}$$

$$\alpha = \frac{-1}{a(x_1 - x_2) + b(y_1 - y_2) + c(z_1 - z_2) + d(t_1 - t_2)}$$

$$= \frac{-1}{a(x_1 - x_2) + b(y_1 - y_2) + c(z_1 - z_2) + d(t_1 - t_2)} \left[(ax_2 + by_2 + cz_2 + dt_2) \begin{bmatrix} x_1 \\ y_1 \\ z_1 \\ t_1 \end{bmatrix} - (ax_1 + by_1 + cz_1 + dt_1) \begin{bmatrix} x_2 \\ y_2 \\ z_2 \\ t_2 \end{bmatrix} \right]$$

$$= \alpha \begin{bmatrix} b(y_2 x_1 - y_1 x_2) + c(z_2 x_1 - z_1 x_2) + d(t_2 x_1 - t_1 x_2) \\ a(x_1 x_2 - x_1 x_2) + c(y_1 z_2 - y_2 z_1) + d(t_1 t_2 - t_2 t_1) \\ a(z_1 x_2 - z_2 x_1) + b(z_1 y_2 - z_2 y_1) + d(z_1 t_2 - z_2 t_1) \\ a(t_1 x_2 - t_2 x_1) + b(t_1 y_2 - t_2 y_1) + c(t_1 z_2 - t_2 z_1) \end{bmatrix} = \alpha X_L$$

$\therefore X_L$ is equal to $X(\lambda\pi)$ up to scale.