Assignment 2 of CISC 2002

ZHANG Huakang/DB92760

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1

```
function y = Assignment_2_1_f(x)

y=816*x^3-3835*x^2+6000*x-3125;

end
```

Listing 1: Function

```
function y = Assignment_2_1_derivative(x)
y=816*3*x^2-3835*2*x+6000;
end
```

Listing 2: Derivative

1.1

```
1 clear
a = 1;
b=2;
_{4} \text{ m}=(a+b)/2;
5 n=1;
 \label{eq:fprintf}  \text{6 } \mathbf{fprintf}(\text{'\%2dth}\,,\ a=\%9.8f\,,\ b=\%9.8f\,,\ error<\%9.8f\,,\ m=\%9.8f\,n\,\text{'},n\,,a\,,b\,,a-b) 
       ,m)
  while (b-a) > 10^{-6}
       if Assignment_2_1_f(m)==0
           break
9
       end
10
       if sign(Assignment_2_1_f(m)) = sign(Assignment_2_1_f(a))
12
       13
           b=m;
14
       end
15
      m=(a+b)/2;
16
17
       fprintf('%2dth, a=%9.8f, b=%9.8f, error<%9.8f, m=%9.8f\n',n,a,b
18
       ,a-b,m)
19 end
```

Listing 3: Bisection

```
1 th \;,\;\; a = 1.00000000 \;,\;\; b = 2.00000000 \;,\;\; error < -1.00000000 \;,\;\; m = 1.500000000 \;
                      2 \, \mathrm{th} \,, \ a \! = \! 1.00000000 \,, \ b \! = \! 1.50000000 \,, \ \mathrm{error} < \! -0.50000000 \,, \ \mathrm{m} \! = \! 1.25000000 \,
                     3th, a=1.25000000, b=1.50000000, error<-0.25000000, m=1.37500000
                    5th, a=1.43750000, b=1.500000000, error < -0.06250000, m=1.46875000
                     6th, a=1.46875000, b=1.500000000, error<-0.03125000, m=1.48437500
                    8 \text{th} \;,\;\; a \!=\! 1.46875000 \;,\;\; b \!=\! 1.47656250 \;,\;\; error <\! -0.00781250 \;,\;\; m \!=\! 1.47265625
                    9th, a=1.46875000, b=1.47265625, error < -0.00390625, m=1.47070313
{\scriptstyle 10\, th \,,\ a=1.46875000 \,,\ b=1.47070313 \,,\ error<-0.00195313 \,,\ m=1.46972656 \,,\ b=1.47070313 \,,\ m=1.46972656 \,,\ m=1.46875000 \,,\ b=1.47070313 \,,\ m=1.46972656 \,,\ m=1.46875000 \,,\ m=1.46972656 \,,\ m=1.469726566 \,,\ m=1.46972666 \,,\ m=1.469726666 \,,\ m=1.46972666 \,,\ m=1.46972666 \,,\ m=1.46972666 \,,\ m=1.469726666 \,,\ m=1.469726666 \,,
 11 11th, a=1.46972656, b=1.47070313, error<-0.00097656, m=1.47021484
 12 \text{ th}, \ a = 1.47021484, \ b = 1.47070313, \ \text{error} < -0.00048828, \ m = 1.47045898
13 13th, a=1.47045898, b=1.47070313, error <-0.00024414, m=1.47058105
_{14} 14 th, a = 1.47058105, b = 1.47070313, error < -0.00012207, m = 1.47064209
15 15th, a=1.47058105, b=1.47064209, error <-0.00006104, m=1.47061157
16\,\mathrm{th}\,,\ a\!=\!1.47058105\,,\ b\!=\!1.47061157\,,\ \mathrm{error}\,<\!-0.00003052\,,\ m\!=\!1.47059631
_{17}\ 17 th \;,\;\; a \!=\! 1.47058105 \;,\;\; b \!=\! 1.47059631 \;,\;\; error < -0.00001526 \;,\;\; m \!=\! 1.47058868 \;,\;\; cross{1} = 1.470588688 \;,\;\; cross{1} = 1.47058868 \;,\;\; cross{1} = 1.470586868 \;,\;\; cross{1} = 1.470586868 \;,\;\; cross{1} = 1.47058688 \;,\;\; cross{1} = 1.470586888 \;,\;\; cross{1} = 1.4
\begin{array}{lll} 18 & 18 th \;, \;\; a = 1.47058105 \;, \;\; b = 1.47058868 \;, \;\; error < -0.00000763 \;, \;\; m = 1.47058487 \\ 19 & th \;, \;\; a = 1.47058487 \;, \;\; b = 1.47058868 \;, \;\; error < -0.00000381 \;, \;\; m = 1.47058678 \end{array}
20\, {\rm th}\,, \ a\!=\!1.47058678\,, \ b\!=\!1.47058868\,, \ {\rm error}\,<\!-0.00000191\,, \ m\!=\!1.47058773\,, \ m\!=\!1.47058773\,, \ m\!=\!1.47058678\,, \ m\!=\!1.
{\tt 21th}\;,\;\;a\!=\!1.47058773\;,\;\;b\!=\!1.47058868\;,\;\;{\tt error}<\!-0.00000095\;,\;\;m\!=\!1.47058821\;
```

Listing 4: Bisection Output

1.2

```
clear
z v0=1.6;
x1=x0-(Assignment_2_1_f(x0)/Assignment_2_1_derivative(x0));
n=0;
fprintf('x(%1d)=%9.8f\n',n,x0)
while abs(x1-x0)>10^(-8)
x0=x1;
x1=x0-(Assignment_2_1_f(x0)/Assignment_2_1_derivative(x0));
n=n+1;
fprintf('x(%1d)=%9.8f\n',n,x0)
end
```

Listing 5: Newton's Method

```
1 \mathbf{x}(0) = 1.60000000

2 \mathbf{x}(1) = 1.54843750

3 \mathbf{x}(2) = 1.56342463

4 \mathbf{x}(3) = 1.56250093

5 \mathbf{x}(4) = 1.56250000
```

Listing 6: Newton's Method Output