



ClusterFL: A Similarity-Aware Federated Learning System for Human Activity Recognition

ClusterFL

- A similarity-aware federated learning system.
 - High system accuracy
 - Low communication overhead
- Motivation
 - Despite the heterogeneity, data distributions of different users' activities may share significant spatial-temporal similarity which can be captured by cluster structures.
 - Subjects' biological features
 - Physical environment
 - Sensor biases
- *Clustered multi-task federated learning*
 - Cluster indicator matrix indicating the similarity of users
- *Cluster-wise straggler dropout*
- *Correlation-based node selection*

Impact of Clusterability

Centralized-cluster:

- K-means clustering → Training a model for each cluster using data of all subjects who belong to the cluster.

Compare with:

- Local learning
 - Overfitting
- Centralized single model learning
 - Privacy concern
- Federated average
- Federated transfer learning

Method	Local	FedAvg	FTL	Centralized-single	Centralized-cluster
Mean Accuracy (%)	53.67	33.61	54.61	72.22	73.17
STD (%)	9.74	12.812	10.19	6.06	3.40

Table 2: Accuracy comparison of different paradigms.

System Architecture

Cluster-wise straggler dropout

- The server will drop stragglers who converge slower than other nodes within each cluster

Correlation-based node selection

- The server will drop nodes that are less related to others in the same cluster

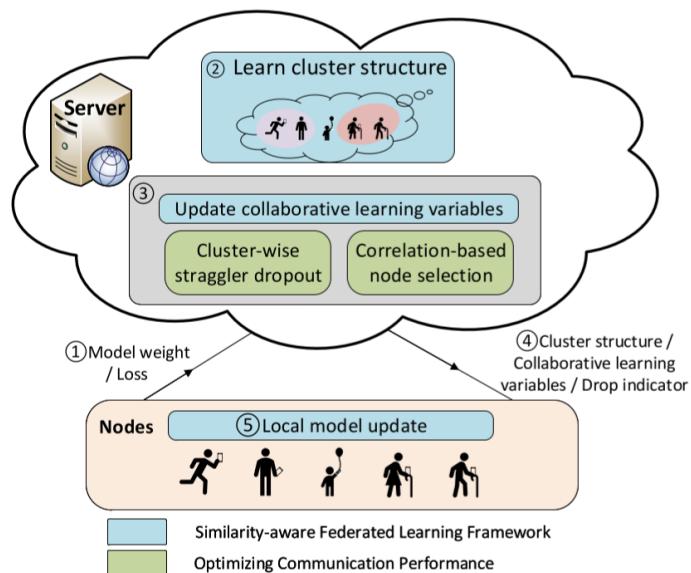


Figure 2: System Architecture of ClusterFL

Cluster Indicator Matrix

Problem Formulation

$$\min_{\mathbf{W}, \mathbf{F}} \sum_{i=1}^M \frac{1}{N_i} \sum_{r=1}^{N_i} l(\mathbf{w}_i^T \mathbf{x}_i^r, y_i^r) + \alpha \text{tr}(\mathbf{W}\mathbf{W}^T) - \beta \text{tr}(\mathbf{F}^T \mathbf{W}\mathbf{W}^T \mathbf{F}) \quad (1)$$

- M is the number of total involved nodes, N_i is number of training data samples in node i . α and β are the hyperparameters and $\alpha \geq \beta > 0$.
- $(\mathbf{x}_i^r, y_i^r) \in \mathbb{R}^D \times \mathbb{R}$ is the r -th training pair of i -th node; $\mathbf{W} = [\mathbf{w}_1, \mathbf{w}_2, \dots, \mathbf{w}_M]^T \in \mathbb{R}^{M \times D}$ is the weight matrix to be estimated where each local model is an activity classifier; l is the loss function of local model.
- $\mathbf{F} \in \mathbb{R}^{M \times D}$ is an orthogonal cluster indicator matrix, with $F_{i,j} = \frac{1}{\sqrt{N_j}}$ if node i belongs to j -th cluster and $F_{i,j} = 0$ otherwise. Here K is the number of clusters and N_j denotes the number of nodes in j -th cluster.

Cluster Indicator Matrix

Problem Formulation

$$\min_{\mathbf{W}, \mathbf{F}} \sum_{i=1}^M \frac{1}{N_i} \sum_{r=1}^{N_i} l(\mathbf{w}_i^T \mathbf{x}_i^r, y_i^r) + \boxed{\alpha tr(\mathbf{W}\mathbf{W}^T) - \beta tr(\mathbf{F}^T \mathbf{W}\mathbf{W}^T \mathbf{F})}$$
$$(\alpha - \beta) \sum_{i=1}^M \|\mathbf{w}_i\|_2^2 + \beta \sum_{j=1}^K \sum_{v \in \mathcal{S}_j} \|\mathbf{w}_v - \bar{\mathbf{w}}_j\|_2^2$$

- L_2 -norm regularization of model weights
 - Prevent overfitting
- K -means clustering
 - Minimize the overall intra-cluster distances of model weights

Alternating Optimization

Alternating Direction Method of Multipliers (ADMM)

Algorithm 1: Alternating Optimization of ClusterFL

Initialization : set $\mathbf{W} = \mathbf{0}^{M \times D}$, $\mathbf{F} = \mathbf{0}^{M \times M}$

1 **for** $h = 0$ **to** H **do**

2 1. Optimization of \mathbf{W} with \mathbf{F} fixed.

3 **for** $t = 0$ **to** T **do**

4 **node update:** parallelly update \mathbf{w}_i ($i = 1, \dots, M$)
5 $\mathbf{w}_i^{t+1} \leftarrow \text{Local SGD}(\mathbf{w}_i^t, (\mathbf{x}_i^r, y_i^r), \mathbf{F}, \Omega, \mathbf{U})$

6 **server update:** update Ω and \mathbf{U}

7 **for** $j = 1$ **to** K **do**

8 $\Omega_j^{t+1} \leftarrow \arg \min_{\Omega_j} L_\rho(\Omega_j, \mathbf{U}_j^t, \mathbf{F}_j^t, \mathbf{W}^{t+1})$

9 $\mathbf{U}_j^{t+1} \leftarrow \mathbf{U}_j^t + \rho(\mathbf{F}_j \mathbf{W}^{t+1} - \Omega_j^{t+1})$

10 **end**

11 **end**

12 2. Optimization of \mathbf{F} with \mathbf{W} fixed.

13 **server update:** Update \mathbf{F} based on Section 5.3

14 **end**

Optimize Model Weights

Let $\mathbf{C}\Omega = \mathbf{F}^T \mathbf{W} \in \mathbb{R}^{K \times D}$

$$\min_{\mathbf{W}, \Omega} f(\mathbf{W}) + g(\Omega)$$

$$s.t. \mathbf{F}^T \mathbf{W} - \Omega = 0$$

$$\text{where: } f(\mathbf{W}) = \sum_{i=1}^M \frac{1}{N_i} \sum_{r=1}^{N_i} l_t(\mathbf{w}_i^T \mathbf{x}_i^r, y_i^r) + \alpha tr(\mathbf{W} \mathbf{W}^T)$$

$$g(\Omega) = -\beta tr(\Omega \Omega^T)$$

Node Update

```
2 | 1. Optimization of W with F fixed.  
3 | for  $t = 0$  to  $T$  do  
4 |   node update: parallelly update  $\mathbf{w}_i$  ( $i = 1, \dots, M$ )  
5 |    $\mathbf{w}_i^{t+1} \leftarrow \text{Local SGD}(\mathbf{w}_i^t, (\mathbf{x}_i^r, y_i^r), \mathbf{F}, \Omega, \mathbf{U})$   
6 |   server update: update  $\Omega$  and  $\mathbf{U}$   
7 |   for  $j = 1$  to  $K$  do  
8 |      $\Omega_j^{t+1} \leftarrow \arg \min_{\Omega_j} L_\rho(\Omega_j, \mathbf{U}_j^t, \mathbf{F}_j^t, \mathbf{W}^{t+1})$   
9 |      $\mathbf{U}_j^{t+1} \leftarrow \mathbf{U}_j^t + \rho(\mathbf{F}_j \mathbf{W}^{t+1} - \Omega_j^{t+1})$   
10 |   end  
11 | end
```

Node Update (line 4-5 in Algorithm 1): Each node will parallelly optimize (e.g., using gradient descent methods) its model weight \mathbf{w}_i based on its local data (\mathbf{x}_i, y_i) , the cluster structure \mathbf{F} and the collaborative learning variables Ω, \mathbf{U} from the server.

$$\mathbf{w}_i^{t+1} = \arg \min_{\mathbf{w}_i} \frac{1}{N_i} \sum_{r=1}^{N_i} l_t(\mathbf{w}_i^T \mathbf{x}_i^r, y_i^r) + (\alpha + \frac{\rho}{2} \sum_{j=1}^K F_{ij}^2) \|\mathbf{w}_i\|_2^2$$

$$+ \sum_{j=1}^K F_{ij} (\mathbf{U}_j^t - \rho \Omega_j^t)^T \cdot \mathbf{w}_i$$

Server Update

```
2 | 1. Optimization of W with F fixed.  
3 | for  $t = 0$  to  $T$  do  
4 |   node update: parallelly update  $\mathbf{w}_i$  ( $i = 1, \dots, M$ )  
5 |    $\mathbf{w}_i^{t+1} \leftarrow \text{Local SGD}(\mathbf{w}_i^t, (\mathbf{x}_i^r, y_i^r), \mathbf{F}, \Omega, \mathbf{U})$   
6 |   server update: update  $\Omega$  and  $\mathbf{U}$   
7 |   for  $j = 1$  to  $K$  do  
8 |      $\Omega_j^{t+1} \leftarrow \arg \min_{\Omega_j} L_\rho(\Omega_j, \mathbf{U}_j^t, \mathbf{F}_j^t, \mathbf{W}^{t+1})$   
9 |      $\mathbf{U}_j^{t+1} \leftarrow \mathbf{U}_j^t + \rho(\mathbf{F}_j \mathbf{W}^{t+1} - \Omega_j^{t+1})$   
10 |   end  
11 | end
```

Server Update (line 6-10 in Algorithm 1): The server will further utilize the newly-updated model weights from nodes **W** and the cluster structure **F** (optimized in Section 5.3) to update the collaborative learning variables Ω, \mathbf{U} . For $j = 1, \dots, K$:

$$\Omega_j^{t+1} = \arg \min_{\Omega_j} -\beta \|\Omega_j\|_2^2 - \Omega_j \cdot (\mathbf{U}_j^t)^T + \frac{\rho}{2} \|\Omega_j - \mathbf{F}_j^T \mathbf{W}^{t+1}\|_2^2$$
$$\mathbf{U}_j^{t+1} = \mathbf{U}_j^t + \rho(\mathbf{F}_j^T \mathbf{W}^{t+1} - \Omega_j^{t+1})$$

Learn Cluster Structure

With W is fixed, problem (1) w.r.t F can be seen as a K -means clustering problem on the nodes' model weights W .

- Quantify the similarity of model weights
- Optimize cluster structure dynamically without knowing the number of cluster K .

Similarity of Model Weights.

Kullback–Leibler divergence(KLD)

$$D_{KL}(\mathbf{w}_i, \mathbf{w}_j) = \frac{1}{N_O} \sum_{r=1}^{N_O} \delta(\mathbf{w}_i, \mathbf{x}_o^r) \log \frac{\delta(\mathbf{w}_i, \mathbf{x}_o^r)}{\delta(\mathbf{w}_j, \mathbf{x}_o^r)}$$

$$\delta(\mathbf{w}_i, \mathbf{x}_o^r) = \text{softmax}\left(\frac{\Phi(\mathbf{w}_i, \mathbf{x}_o^r)}{\tau}\right)$$

where $\Phi(\mathbf{w}_i, \mathbf{x}_o^r)$ denotes the pre-softmax output of model \mathbf{w}_i on the input data \mathbf{x}_o^r . Smaller KL divergence denotes closer relationship of models for node i and j. Then we calculate the KL divergence between any two models and therefore obtain a KL divergence matrix $\mathbf{D} \in \mathbb{R}^{M \times M}$, with $D_{i,j} = D_{KL}(\mathbf{w}_i, \mathbf{w}_j)$.

Gibbs' inequality:

$$-\sum_{i \in I} p_i \ln q_i \geq -\sum_{i \in I} p_i \ln p_i.$$

Optimize Cluster Relationship

*Principal Components Analysis
(PCA) → K-means clustering*

$\mathbf{F} \in \mathbb{R}^{M \times D}$ is an orthogonal cluster indicator matrix, with $F_{i,j} = \frac{1}{\sqrt{N_j}}$ if node i belongs to j -th cluster and $F_{i,j} = 0$ otherwise. Here K is the number of clusters and N_j denotes the number of nodes in j -th cluster.

According to [14], principal components are the continuous solutions to the discrete cluster membership indicators for K -means clustering. Suppose there are total M clusters among nodes, then $\mathbf{P} = \mathbf{Q}_{M-1}\mathbf{Q}_{M-1}^T \in \mathbb{R}^{M \times M}$ will be the continuous solution of \mathbf{F} , where $\mathbf{Q}_{M-1} = (\mathbf{v}_1, \dots, \mathbf{v}_{M-1})$ collects the $M - 1$ principal components of \mathbf{D} using principal components analysis (PCA).

If the data of nodes has a cluster structure, \mathbf{P} is expected to yield a similar diagonal block structure after permutation clusters together. However, as \mathbf{P} is an approximation of the discrete valued indicators, there may be outliers in \mathbf{P} . We recover \mathbf{F} more accurately as follows:

- 1) we set $P_{ij} = 0$ if $P_{ij} < 0$ as \mathbf{P} could contain negative elements;
- 2) we scale each element of \mathbf{P} as $F_{ij} = \frac{P_{ij}}{\sqrt{\sum_{i=1}^M P_{ij}}}$ to obtain the final normalized cluster indicator matrix \mathbf{F} .

Note that here we obtain a continuous approximation of \mathbf{F} for the optimization steps in line 12-13 of Algorithm 1 without requiring to know the number of cluster K in the optimiztion process.

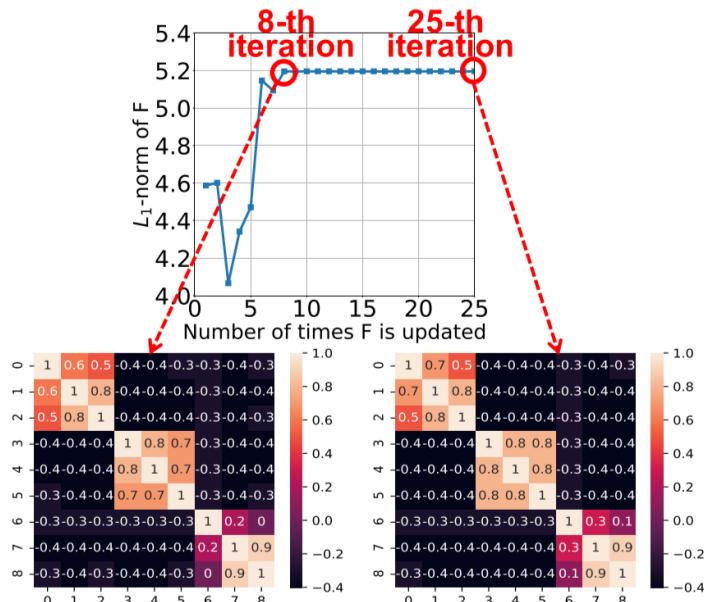
- [14] Chris Ding and Xiaofeng He. 2004. K-means clustering via principal component analysis. In *Proceedings of the twenty-first international conference on Machine learning*. 29.

Optimizing Communication Performance

In traditional FL systems:

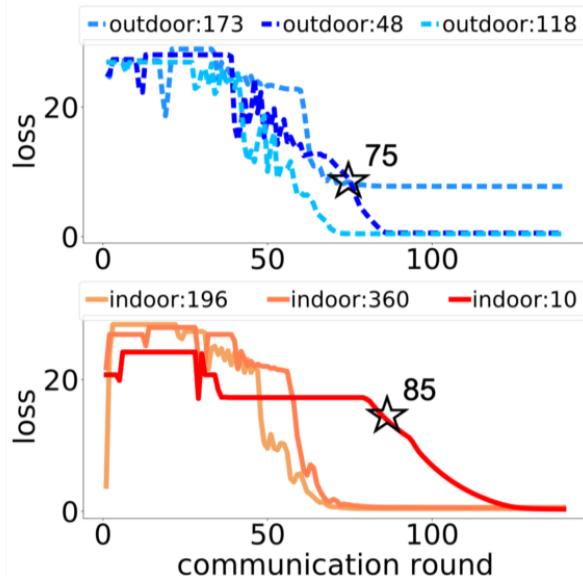
- Some focuses on the model compression and quantization techniques
- Other approaches chooses stragglers (the nodes who converge slower) from all nodes and drop them simultaneously, which does not consider the differences among the stragglers.

Leverage the inherent cluster relationship learned by ClusterFL to dynamically drop nodes during the FL process.

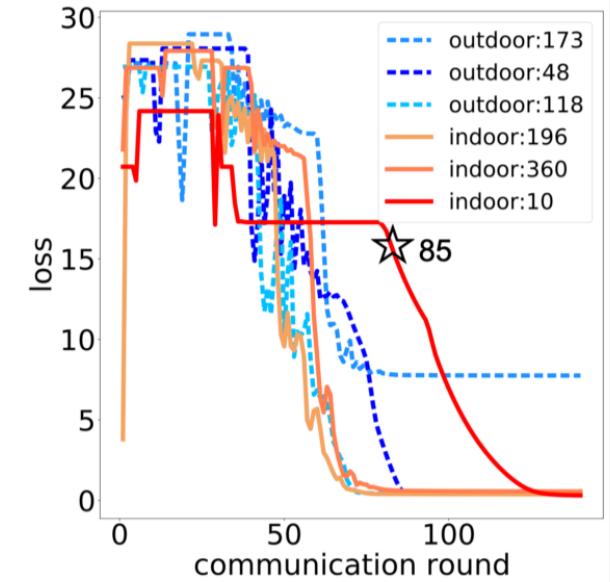


Cluster-wise Straggler Dropout

This example suggests that it's more flexible and efficient to identify stragglers within clusters.



(a) Within clusters



(b) Among all nodes

Figure 4: Identifying stragglers within clusters (a) and among all nodes (b). Our cluster-wise straggler dropout can dynamically identify and drop stragglers within each cluster. “indoor:196” means the node has 196 data samples from the environment “indoor”.

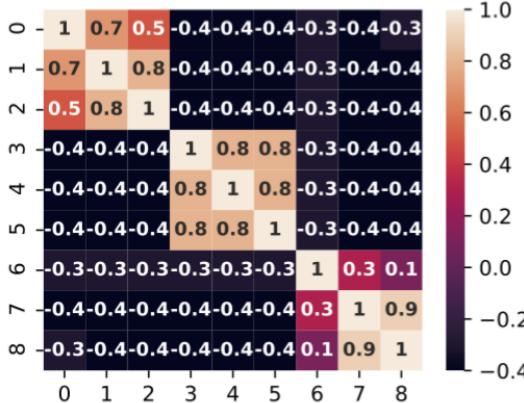
Measure the Convergence

For cluster j ($j = 1, \dots, K$) which contains N_j nodes, we define the averaged convergence rate γ_q for node q ($q = 1, \dots, N_j$) in the cluster during the latest T_c iterations as follows:

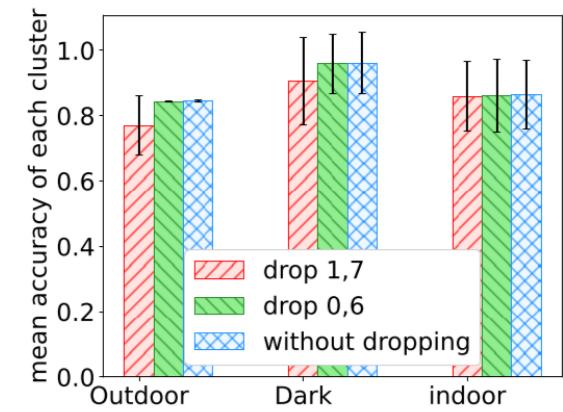
$$\gamma_q = \frac{1}{T_c} \sum_{t=1}^{T_c} \varepsilon_q^t \quad \text{for } q = 1, 2, \dots, N_j$$
$$\varepsilon_q^t = \frac{|loss_q(t) - loss_q(t-1)|}{\sum_{q=1}^{N_j} |loss_q(t) - loss_q(t-1)|}$$

Here ε_q^t is the normalized loss update for node q compared to other nodes in cluster j at t -th iteration; γ_q is the mean value of ε_q^t in the latest T_c iterations; T_c is the threshold of iteration for determining stragglers, where a larger T_c means obtaining a more smooth loss update to filter out interference while also putting off the iteration to recognize stragglers.

Correlation-based Node Selection



(a) Correlation matrix of nodes



(b) Mean accuracy of each cluster

Figure 5: Effectiveness of correlation-based dropout. Left: The three block denotes the cluster “outdoor”, “dark”, “indoor”, respectively. Compared to node 1 and node 7, node 0 and node 6 are less related to other nodes in the clusters. Right: The accuracy performance after dropping the less related nodes suffers minor degradation.

Specifically, the server will compute an importance vector σ for all nodes using the correlation matrix of \mathbf{F} to measure their degree of correlation with other nodes in each cluster. Suppose node q is in the cluster j which contains N_j nodes, we define the importance metric σ_q for node q as follows:

$$\sigma_q = \frac{1}{N_j} \sum_{p=1}^{N_j} \mathbf{R}_{pq} \quad \text{for node } q \text{ in cluster } j$$

Correlation-based Node Selection

As shown in Figure 5, a node with a larger σ_q (e.g., node 1 with $\sigma_1 = 0.833$ while node 0 with $\sigma_0 = 0.733$) means it has a higher level of correlation with other nodes in the same cluster. The server will then order σ_q of all clusters from large to small and drop the last M_d nodes at iteration T_{thresh} . In this way, the total number of nodes communicating with the server will be reduced to $M - M_d$. The dropped-out nodes will then locally train their models based on the last update and do not communicate with the server. Finally, the total communication time will be reduced since the number of nodes interacting with the server is smaller, while relatively more important nodes are kept in the learning process to improve the overall performance.

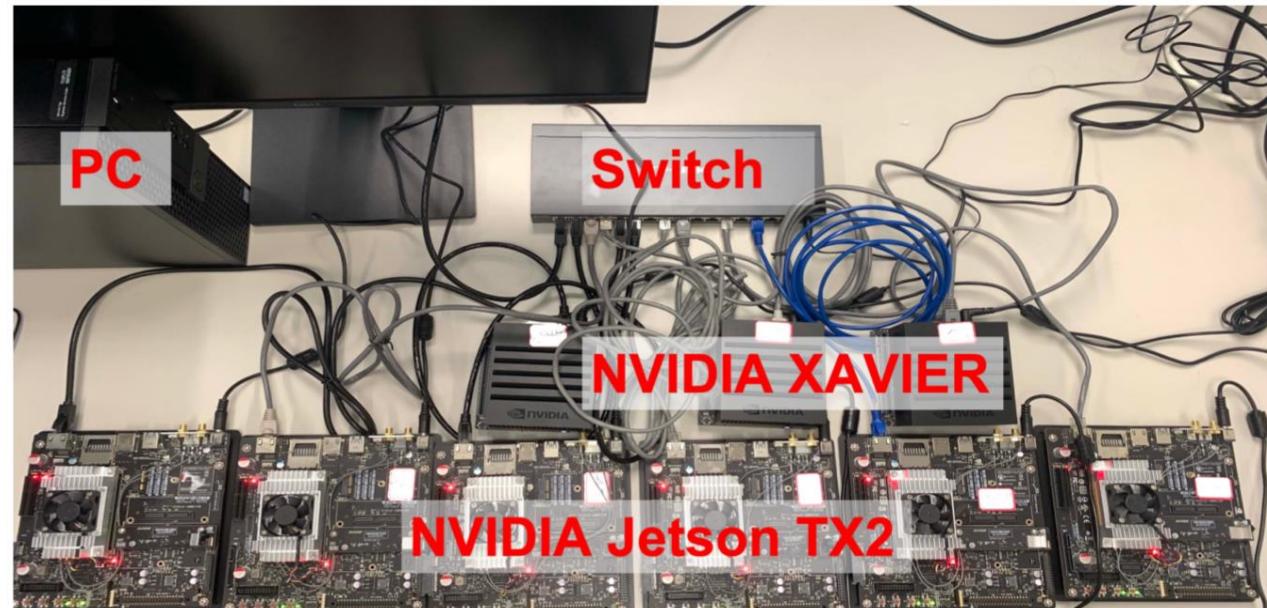
Data Collection

Application	Task	Data Dimension	Number of Subjects	Number of Data Records	Sensor	Environment
Human Movement Detection using UWB	with/without Human Movement	55	8	663	Decawave DWM1000 UWB	node 0,1 from parking lot node 2,3,4 from corridor node 5,6,7 from room
Walking Activity Recognition using IMU	walking on corridors/upstairs/downstairs	900	7	1369	LPMS-B2 IMU	node 0,1,2,3 from building 1 node 4,5,6 from building 2
Gesture Recognition using Depth Camera	good/ok/victory/stop/fist	1296	9	7422	PicoZense DCAM710	node 0,1,2 from "outdoor" node 3,4,5 from "dark" node 6,7,8 from "indoor"
HARBox: ADL Recognition using Smartphones	walking/hopping/phone calls/waving/typing	900	121	32935	77 different smartphone models	121 subjects (17-55 years old) Sampling rate: 43.5-57.5Hz

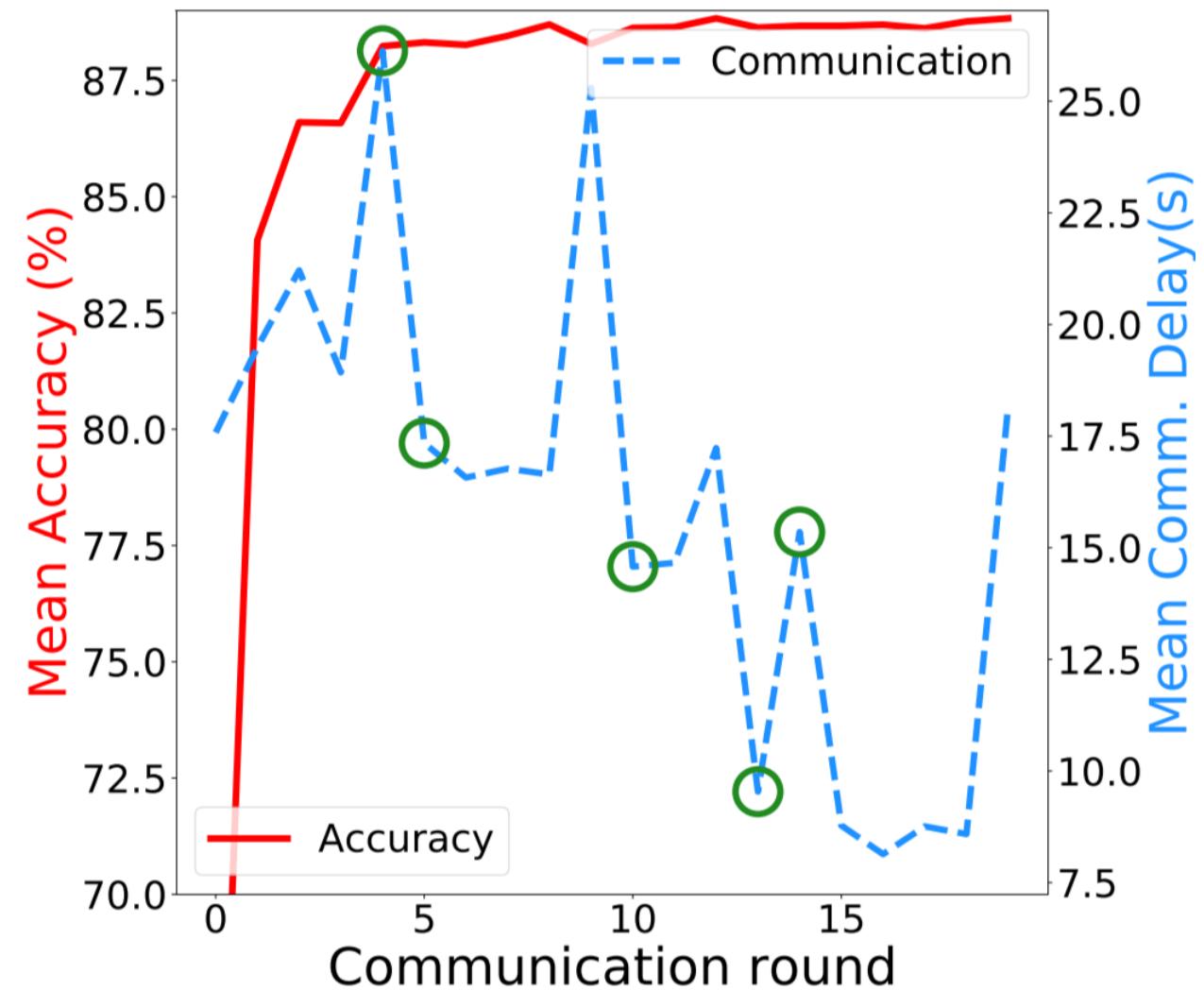
Table 3: Four new HAR datasets (UWB, IMU, Depth, HARBox) collected in real-world experiments

Implementation and Evaluation

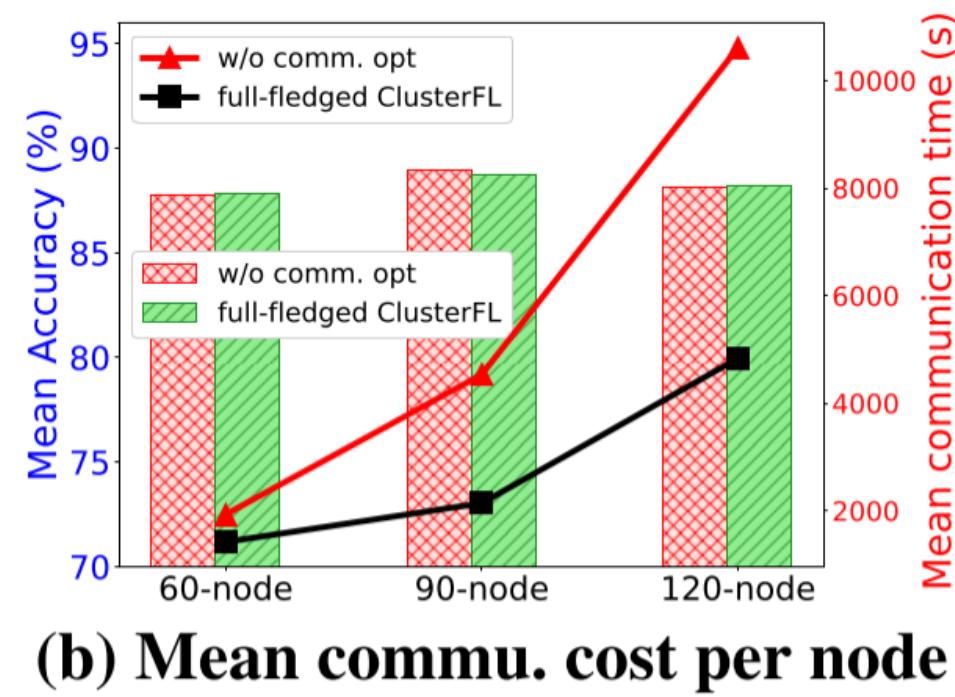
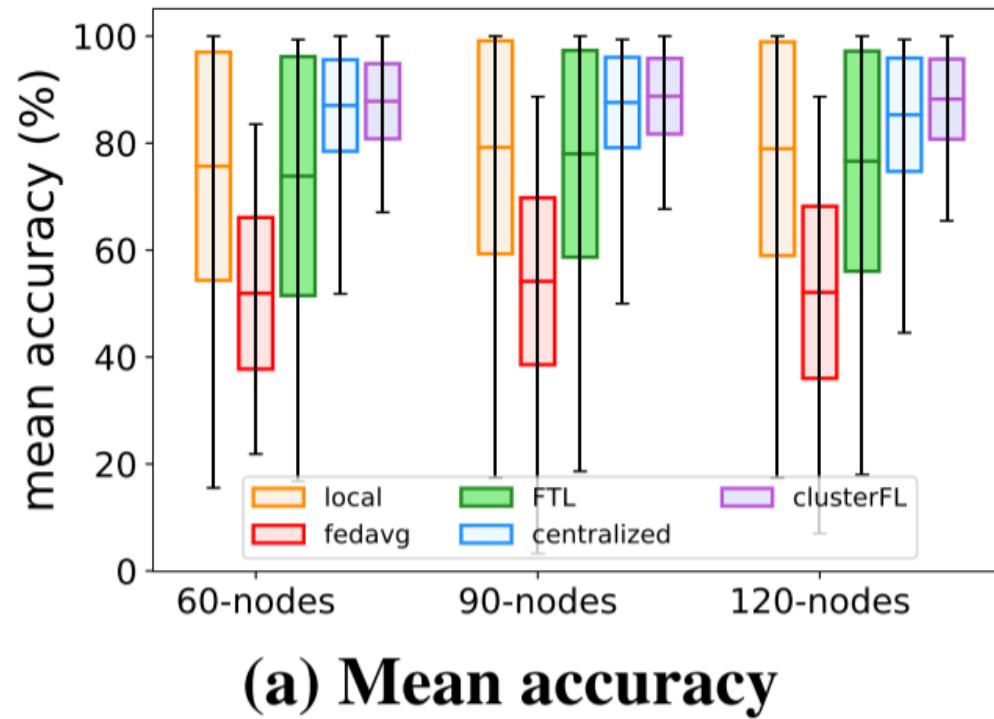
- Server
 - PC
 - Intel Core i7-9700 CPU 3.0GHz x 8
 - Ubuntu 18.04.5
- Node
 - NVIDIA Jetson TX2 x 7
 - 6 core ARM CPU
 - Ubuntu 18.04.5
 - NVIDIA Jetson AGX Xavier x 3
 - 8 core ARM CPU
 - Ubuntu 18.04.5
- TP-link TL-SG2016k
- Python3



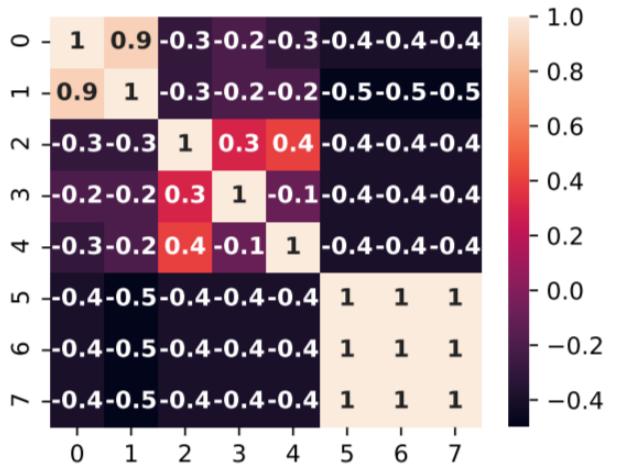
Impact of Dynamic Network Conditions



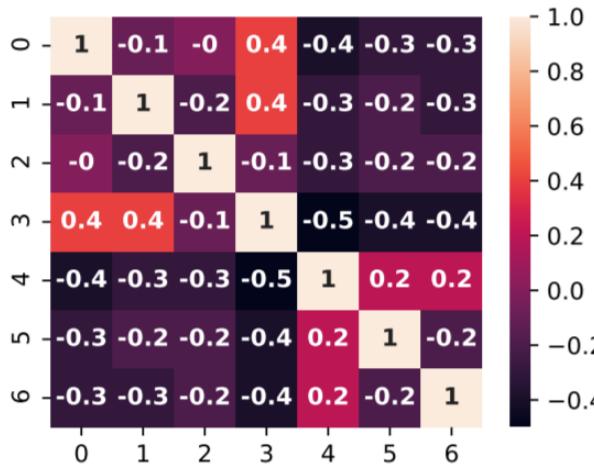
Scalability



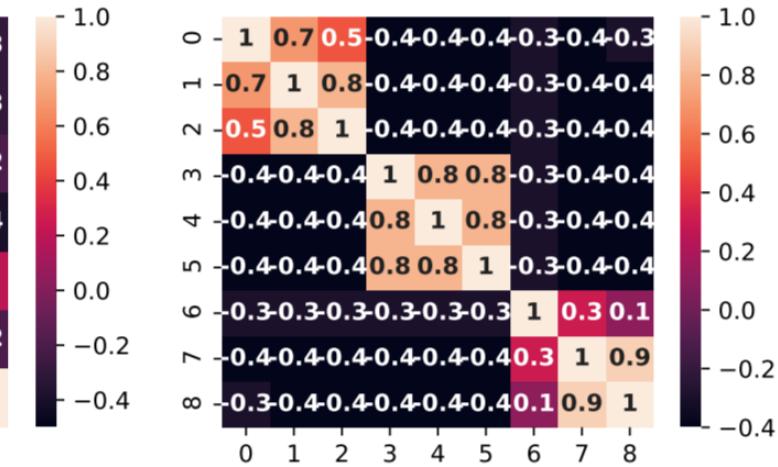
Performance on Different Datasets



(a) UWB structure



(b) IMU structure



(c) Depth structure

Figure 14: Learned relationship among nodes for UWB, IMU, Depth dataset, respectively.

Comparison of Different Methods

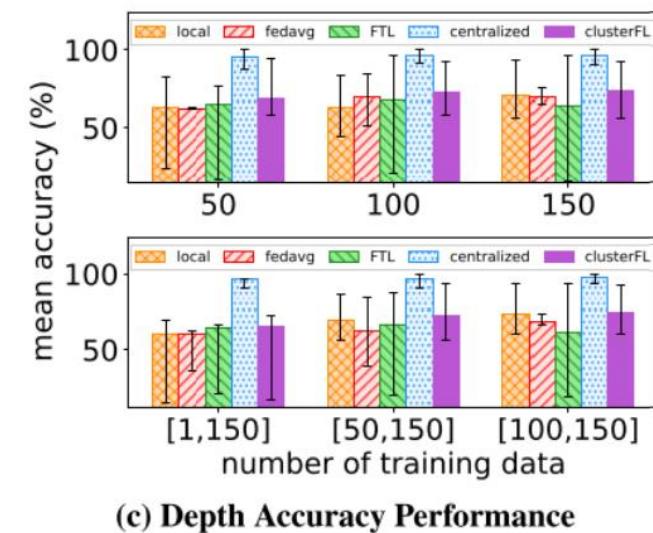
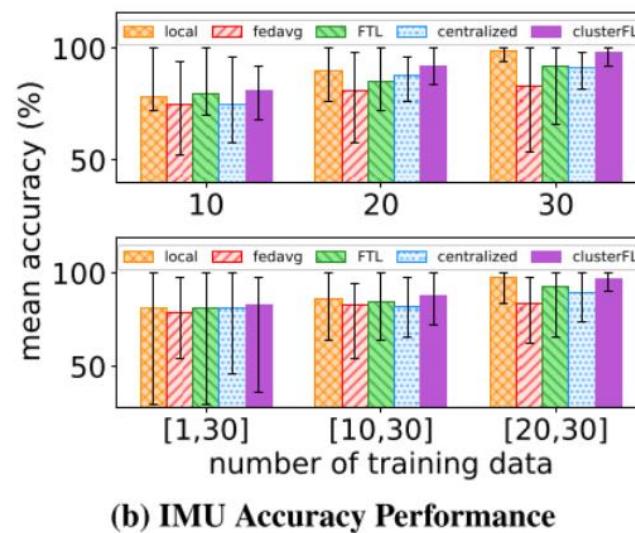
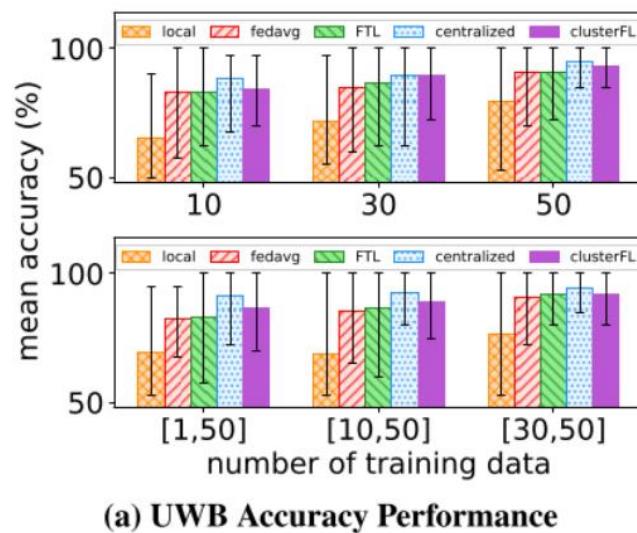


Figure 12: Comparison of Accuracy Performance for UWB, IMU, Depth dataset, respectively. ClusterFL outperforms local/FedAvg/FTL in various settings and even performs better than centralized learning for IMU dataset.

Comparison of Different Methods

	Local	FedAvg	FTL	Centralized	ClusterFL
UWB	72.19%	86.25%	86.98%	90.83 %	89.06%
IMU	88.86%	79.52%	85.42%	84.48%	90.47%
Depth	65.81%	67.52%	65.69%	96.29 %	71.82%

Table 4: Mean accuracy in balanced data settings

	Local	FedAvg	FTL	Centralized	ClusterFL
UWB	71.67%	86.25%	87.30%	92.71%	92.71%
IMU	88.29%	82.00%	86.20%	84.19%	89.05%
Depth	67.91 %	63.75%	63.86%	96.82%	70.68%

Table 5: Mean accuracy in unbalanced data settings

System Overhead

Dataset	number of nodes	number of data records in nodes	configuration of nodes	dropped nodes
UWB	8	[22, 25, 10, 13, 13, 17, 19, 29]	node 0,1,2 on Xavier node 3,4,5,6,7 on Tx2	node 3 and 4
IMU	7	[10, 13, 13, 49, 19, 29, 31]	node 0,1,2 on Xavier node 3,4,5,6 on Tx2	node 3 and 6
Depth	9	[94, 97, 114, 117, 117, 59, 133, 71, 86]	node 0,1,2 on Xavier node 3,4,5,6,7,8 on Tx2	node 5,7,8

Table 6: Setup of nodes for three datasets

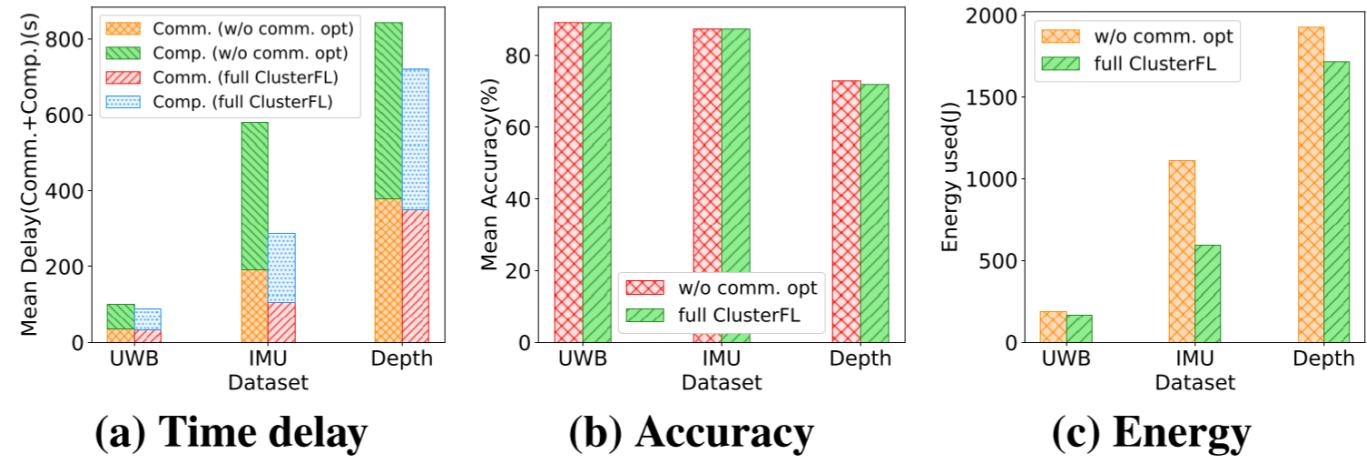


Figure 15: Performance with or without communication optimization of ClusterFL for UWB, IMU, Depth dataset. w/o comm. opt means without communication optimization.

Performance with Different Model Depths

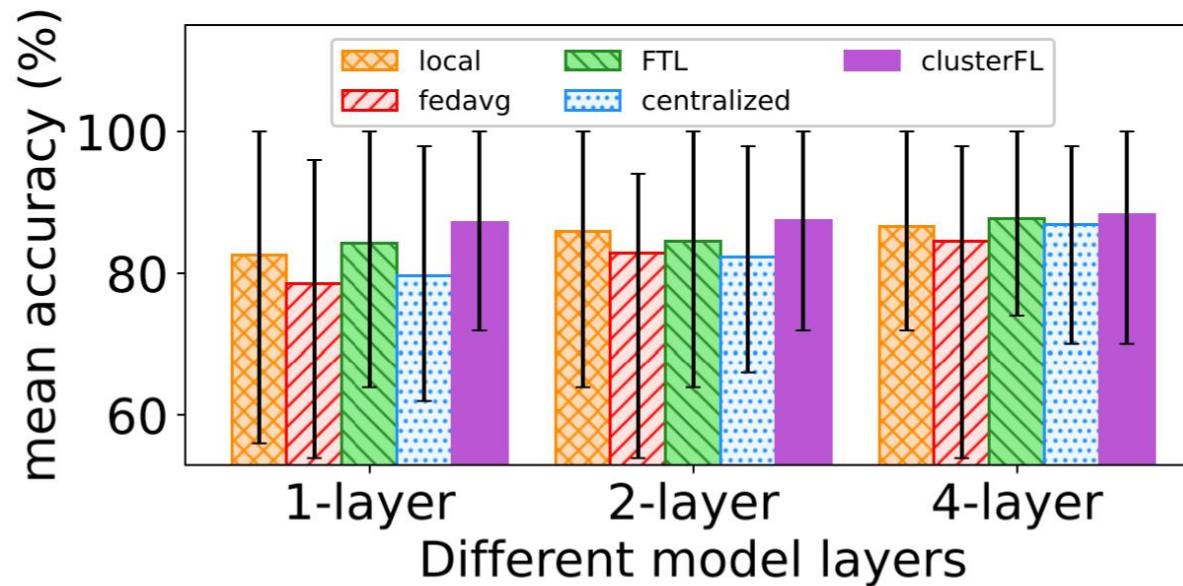


Figure 16: The accuracy of IMU dataset for models with different depths.