- (c) Finally use the above results to show the following two statements.

 which help interpretting the covariance metrix and its inverse (the precision matrix.
 - (a) A zero entry in the i, ith position of the covariance motion Z implies that n; and n; are mariginally independent
 - (1) A zero-entry in the i, it position of the precision matrix $\Delta = \Xi^{-1}$ implies that α_i and n_j are conditionally independentagiven all other variables n_k for $k \neq i,j$.
- (i) Without loss of generality, we can assume that

 (i,i) = (1,2), as we can permute the variables without changing

 the distribution:

we have been given that $Z_{12} = 0$ and from the symmetry of covariance matrix we know $Z_{2i} = 0$ $P(x; u, Z) = \frac{1}{(2\pi)^{p/2}} \exp \left\{ -\frac{1}{2} (x-u)^T Z(x-u)^T Z$

consider the matrix $A = \begin{bmatrix} I_2 & O_2 \\ O_2 & O_{D+2} \end{bmatrix}$; $A = A^T$

As we know the affine projection $p(2:=An) = N(x; Au, A = A^T)$ thus are have $Z = A \begin{pmatrix} n_1 \\ n_2 \\ \vdots \\ n_n \end{pmatrix} = \begin{pmatrix} n_1 \\ n_2 \\ \vdots \\ n_n \end{pmatrix}$

The new means
$$\mathcal{A}' = A \mathcal{A} = \begin{bmatrix} u_x \\ u_y \\ \vdots \\ u_y \end{bmatrix}_{DN}$$

The new covariance $Z' = \begin{bmatrix} I_L & O_L \\ O_L & O_{PNL} \end{bmatrix} \begin{bmatrix} \Sigma_{11} & \Sigma_{12} & \vdots & \Sigma_{1D} \\ O_L & O_{PNL} \end{bmatrix} \begin{bmatrix} I_2 & O_L \\ O_L & O_{PNL} \end{bmatrix} \begin{bmatrix} \Sigma_{21} & \Sigma_{22} & \vdots & \Sigma_{2D} \\ \vdots & \vdots & \Sigma_{2L} & \vdots & \vdots \\ O_L & O_L & O_L \end{bmatrix}$

$$= \begin{bmatrix} \Sigma_{21} & \Sigma_{22} & 0 & 0 \\ \Sigma_{21} & \Sigma_{22} & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots \\ O_L & O_L & O_L \end{bmatrix}$$

$$= \begin{bmatrix} \Sigma_{21} & \Sigma_{22} & 0 & 0 \\ O_L & O_L & O_L \end{bmatrix}$$

$$= \begin{bmatrix} \Sigma_{21} & \Sigma_{22} & 0 & 0 \\ \vdots & \ddots & \ddots & \vdots \\ \Sigma_{21} & \Sigma_{21} \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} \\ \Sigma_{21} & \Sigma_{21} &$$