

MPSS mid recursion

Step	Size	Tree	
0	n	$n \log n$	n ↑ Filling left and right
1	$n/2$	$\frac{n}{2} \log(\frac{n}{2})$	$n \log n$ ↑ sorting
2	$n/4$	$\frac{n}{4} \log(\frac{n}{4})$	n ↑ determining mpssMid
⋮	⋮	⋮	
k	1	$\Theta(1)$	

$$1 = \frac{n}{2^k}$$

$$k = \log n$$

$$\sum_{i=0}^{k-1} \frac{n}{2^i} (\log(\frac{n}{2^i})) + \cancel{X}$$

$$\hookrightarrow \log n - \log 2^i$$

$$n \sum_{i=0}^{k-1} \frac{1}{2^i} (\log n - i)$$

$$n \left[\sum_{i=0}^{k-1} \frac{1}{2^i} \right] \left[\sum_{i=0}^{k-1} (\log n - i) \right]$$

$$n \left[\frac{2-1}{2^k-1} \right] \left[\log n - \frac{(k-1)(k)}{2} \right]$$

$$\cancel{n \left[\frac{1}{2^{\log n} - 1} \right]}_{\text{constant}} \left[\log n - \frac{(\log n)(\log n)}{2} \right]$$

$$O(n \log^2 n)$$