Homework 7

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R Markdown

1. Create a new column in the dataset, high_mileage that is true if mpg > mean(mpg). Else its false. You will try to predict these variables as a function of the predictors. DO NOT USE name and origin is a categorical as before.

```
library(ISLR)
library(glmnet)
## Warning: package 'glmnet' was built under R version 3.4.2
## Loading required package: Matrix
## Loading required package: foreach
## Loaded glmnet 2.0-13
library(tree)
library(gbm)
## Loading required package: survival
## Loading required package: lattice
## Loading required package: splines
## Loading required package: parallel
## Loaded gbm 2.1.3
library(e1071)
data(Auto)
table = Auto[1:7]
meanOfmpg = mean(Auto$mpg)
high mileage=ifelse(Auto$mpg<meanOfmpg,"false","true")
newTable = data.frame(table,high_mileage)
summary(newTable)
##
                      cylinders
                                      displacement
                                                       horsepower
         mpg
##
   Min. : 9.00
                    Min.
                           :3.000
                                    Min. : 68.0
                                                     Min.
                                                            : 46.0
                                                     1st Qu.: 75.0
   1st Qu.:17.00
                    1st Qu.:4.000
                                     1st Qu.:105.0
##
   Median :22.75
                    Median :4.000
                                    Median :151.0
                                                     Median: 93.5
##
  Mean
           :23.45
                    Mean
                           :5.472
                                    Mean
                                            :194.4
                                                     Mean
                                                            :104.5
##
   3rd Qu.:29.00
                    3rd Qu.:8.000
                                     3rd Qu.:275.8
                                                     3rd Qu.:126.0
##
   Max.
           :46.60
                    Max.
                           :8.000
                                    Max.
                                            :455.0
                                                     Max.
                                                            :230.0
##
        weight
                    acceleration
                                                    high_mileage
                                         year
##
                          : 8.00
                                                    false:206
  Min.
           :1613
                   Min.
                                   Min.
                                           :70.00
  1st Qu.:2225
                   1st Qu.:13.78
                                    1st Qu.:73.00
                                                    true :186
##
## Median :2804
                   Median :15.50
                                   Median :76.00
## Mean
                                   Mean
           :2978
                   Mean
                          :15.54
                                           :75.98
## 3rd Qu.:3615
                   3rd Qu.:17.02
                                    3rd Qu.:79.00
## Max.
           :5140
                   Max.
                          :24.80
                                   Max.
                                           :82.00
```

2. Set the seed to one and set up the data for 3-fold cross validation

```
k=3
set.seed(1)
folds=sample(1:k,nrow(newTable),replace = TRUE)
tableSet = data.frame(newTable,folds)
Auto$origin=factor(Auto$origin)
```

3. Guess which classifier will do best.

Answer:Boosting is best

- 4. Predict high mpg with these classifiers:
- a. Logistic regression tuning (i.e., with ridge regularization)

```
high_mileage <- Auto$mpg > mean(Auto$mpg)
Auto$origin <- as.factor(Auto$origin)</pre>
Auto = data.frame(Auto,high_mileage)[,c(-1,-9)]
set.seed(1)
k = 3
folds = sample(1:k, nrow(Auto), rep = TRUE)
x = model.matrix(high_mileage ~ ., Auto)[,-1]
y = Auto$high_mileage
expo = seq(-10, 10, length = 200)
lmd = sort(c(0, 100, 10 ^ expo))
MSErg = c()
for (i in 1:k){
        train = c(1:nrow(x))[folds != i]
        test = (-train)
        y.test = y[test]
      glm.fit = glmnet(x[train,], y[train], alpha = 0, lambda = lmd, thresh = 1e-12)
        glm.row = nrow(x[test,])
        glm.probs = predict(glm.fit, s = lmd, newx = x[test,])
        if (!length(MSErg)){
          MSErg = rep(0, ncol(glm.probs))
        MSErg = MSErg + colMeans((glm.probs - y.test) ^ 2)
MSErg = unname(MSErg) / k
plot(x = log(lmd), y = MSErg, xlab = 'log(lambda)', ylab = 'MSE')
```

```
0.20
     0.15
               -20
                             -10
                                                         10
                                                                       20
                                            0
                                      log(lambda)
print("The Lowest MSE:")
## [1] "The Lowest MSE:"
print(min(MSErg))
## [1] 0.09625485
optirg = lmd[which(MSErg == min(MSErg))]
print("The Best Lambda:")
## [1] "The Best Lambda:"
print(optirg)
## [1] 0.001366716
Mrate = 0
for (i in 1:k){
       train = c(1:nrow(x)) [folds != i]
       test = (-train)
       y.test = y[test]
     glm.fit = glmnet(x[train,], y[train], alpha = 0, lambda = lmd, thresh = 1e-12)
       glm.row = nrow(x[test,])
       glm.probs = predict(glm.fit, s = optirg, newx = x[test,])
     glm.pred = rep(FALSE,glm.row)
       glm.pred[glm.probs > 0.5] = TRUE
     print(table(glm.pred, y.test))
       print(mean(glm.pred == y.test))
       Mrate = Mrate + mean(glm.pred == y.test)
```

```
y.test
##
## glm.pred FALSE TRUE
##
      FALSE
               59
                      1
      TRUE
                10
                     61
##
##
   [1] 0.9160305
           y.test
##
  glm.pred FALSE TRUE
##
##
      FALSE
               57
                      2
##
      TRUE
                15
                     65
##
  [1] 0.8776978
           y.test
   glm.pred FALSE TRUE
##
##
      FALSE
               51
                      2
##
      TRUE
                14
                     55
## [1] 0.8688525
print("The mean accuracy:")
## [1] "The mean accuracy:"
print(Mrate/k)
## [1] 0.8875269
  b. Decision trees with tuning (e.g., you will set the splitting criterion)
library(ISLR)
library(glmnet)
library(tree)
library(gbm)
library(e1071)
data(Auto)
table = Auto[1:7]
meanOfmpg = mean(Auto$mpg)
high mileage=ifelse(Auto$mpg<meanOfmpg,"false","true")
newTable = data.frame(table,high_mileage)
summary(newTable)
##
                       cylinders
                                       displacement
                                                         horsepower
         mpg
                            :3.000
##
    Min.
           : 9.00
                     Min.
                                      Min.
                                             : 68.0
                                                       Min.
                                                              : 46.0
                     1st Qu.:4.000
##
    1st Qu.:17.00
                                      1st Qu.:105.0
                                                       1st Qu.: 75.0
   Median :22.75
                     Median :4.000
                                      Median :151.0
                                                       Median: 93.5
##
    Mean
           :23.45
                     Mean
                            :5.472
                                      Mean
                                            :194.4
                                                       Mean
                                                              :104.5
##
    3rd Qu.:29.00
                     3rd Qu.:8.000
                                      3rd Qu.:275.8
                                                       3rd Qu.:126.0
##
    Max.
           :46.60
                     Max.
                            :8.000
                                      Max.
                                             :455.0
                                                       Max.
                                                              :230.0
##
        weight
                     acceleration
                                                      high_mileage
                                          year
##
   Min.
           :1613
                    Min.
                          : 8.00
                                     Min.
                                            :70.00
                                                      false:206
                    1st Qu.:13.78
                                                      true :186
##
    1st Qu.:2225
                                     1st Qu.:73.00
   Median:2804
                    Median :15.50
                                     Median :76.00
## Mean
           :2978
                           :15.54
                                     Mean
                                            :75.98
                    Mean
    3rd Qu.:3615
                    3rd Qu.:17.02
                                     3rd Qu.:79.00
##
           :5140
                           :24.80
                                            :82.00
   {\tt Max.}
                    Max.
                                     Max.
Auto$origin=factor(Auto$origin)
table = Auto[1:8]
meanOfmpg = mean(Auto$mpg)
k=3
```

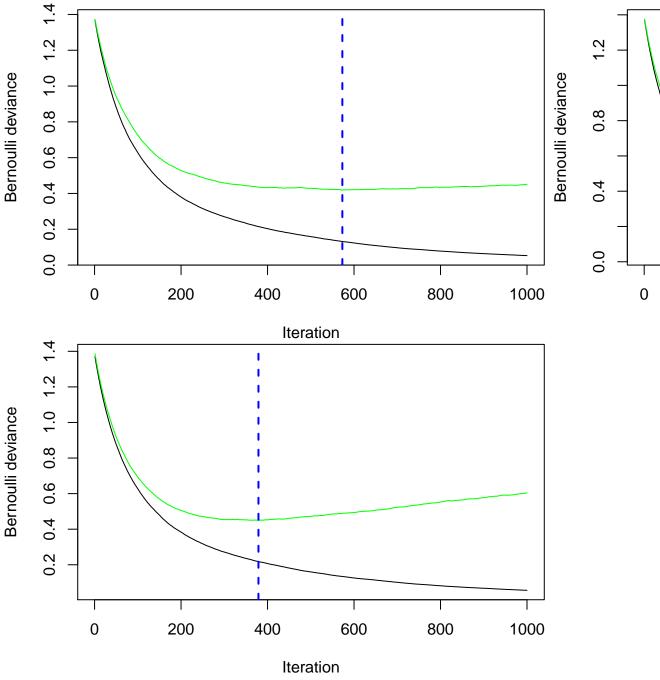
```
set.seed(1)
folds=sample(1:k,nrow(table),replace = TRUE)
high_mileage =ifelse(Auto$mpg<meanOfmpg,"false","true")
newTable = data.frame(table[2:7],high_mileage)
tableSet = data.frame(newTable,folds)
accuracy = rep(0,3)
for(i in 1:3){
  train = tableSet[which(tableSet$folds != i),]
  test = tableSet[which(tableSet$folds == i),]
 tree.mpg = tree(high_mileage~.,data = train)
  cv.mpg =cv.tree(tree.mpg ,FUN=prune.misclass )
  prune.mpg=prune.misclass(tree.mpg,best=4)
 tree.pred=predict(prune.mpg,test,type="class")
  a=table(tree.pred,test$high_mileage)
  accuracy[i] = (a[1,1] + a[2,2])/(a[1,1]+a[1,2]+a[2,1]+a[2,2])
}
meanAccuracy = (accuracy[1] + accuracy[2] +accuracy[3])/3
meanAccuracy
## [1] 0.9057141
  c. Bagging with tuning
Auto$origin=factor(Auto$origin)
library(randomForest)
## randomForest 4.6-12
## Type rfNews() to see new features/changes/bug fixes.
accuracy = rep(0,3)
for(i in 1:k){
 train = tableSet[which(tableSet$folds != i),]
  test = tableSet[which(tableSet$folds == i),]
  bag.mpg = randomForest(high_mileage ~. , data= train,mtry=dim(newTable)[2],importance = TRUE)
  bag.predict.mpg = predict(bag.mpg , test, type = "class")
  table(bag.predict.mpg,test$high_mileage)
  a=table(bag.predict.mpg,test$high_mileage)[1,1]
  b=table(bag.predict.mpg,test$high_mileage)[2,2]
  total = table(bag.predict.mpg,test$high_mileage)[1,1] +table(bag.predict.mpg,test$high_mileage)[1,2]+
  accuracy[i] = (a + b)/total
}
meanAccuracy =(accuracy[1]+accuracy[2]+accuracy[3]) /3
meanAccuracy
## [1] 0.9021671
  d. Random forest with tuning
library(randomForest)
Auto$origin=factor(Auto$origin)
```

```
accuracy = rep(0,3)
for(i in 1:k){
  train = tableSet[which(tableSet$folds != i),]
  test = tableSet[which(tableSet$folds == i),]
  random.mpg = randomForest(high_mileage ~. , data= train,mtry=dim(newTable)[2]/3,importance = TRUE)
  random.predict.mpg = predict(random.mpg , test, type = "class")
  table(random.predict.mpg,test$high_mileage)
  a=table(random.predict.mpg,test$high_mileage)[1,1]
  b=table(random.predict.mpg,test$high_mileage)[2,2]
  total = table(random.predict.mpg,test$high_mileage)[1,1] +table(random.predict.mpg,test$high_mileage)
  accuracy[i] = (a + b)/total
}
meanAccuracy =(accuracy[1]+accuracy[2]+accuracy[3]) /3
meanAccuracy
## [1] 0.9125742
  e. Boosting with tuning
Auto$origin=factor(Auto$origin)
newTable$high_mileage =as.integer(as.logical(newTable$high_mileage))
tableSet = data.frame(newTable,folds)
  train = tableSet[which(tableSet$folds != 1),]
  test = tableSet[which(tableSet$folds == 1),]
boost.mpg = gbm(high_mileage~.,data = train,distribution = "bernoulli",n.trees=1000, interaction.depth=
summary(boost.mpg)
cylinders
folds
                                                                 25
                 5
                             10
                                         15
                                                     20
     0
                                                                              30
                                 Relative influence
                                rel.inf
                         var
## displacement displacement 30.1604563
## weight
                      weight 24.2112762
```

year 17.4935990

year

```
## horsepower
                  horsepower 13.4060714
                  cylinders 10.2009440
## cylinders
## acceleration acceleration 4.1126235
## folds
                       folds 0.4150296
library(ISLR)
library(glmnet)
library(tree)
library(gbm)
library(e1071)
library(survival)
library(pROC)
## Type 'citation("pROC")' for a citation.
## Attaching package: 'pROC'
## The following object is masked from 'package:glmnet':
##
       auc
## The following objects are masked from 'package:stats':
##
       cov, smooth, var
data(Auto)
Auto$origin=factor(Auto$origin)
table = Auto[1:8]
meanOfmpg = mean(Auto$mpg)
k=3
set.seed(1)
folds=sample(1:k,nrow(table),replace = TRUE)
high_mileage =ifelse(Auto$mpg<meanOfmpg,"false","true")
newTable = data.frame(table[2:7],high_mileage)
tableSet = data.frame(newTable,folds)
tableSet$high_mileage =as.integer(as.logical(tableSet$high_mileage))
library(randomForest)
accuracy = rep(0,3)
for(i in 1:k){
  train = tableSet[which(tableSet$folds != i),]
  test = tableSet[which(tableSet$folds == i),]
  boost.mpg = gbm(high_mileage~.,data = train,distribution = "bernoulli",n.trees=1000, interaction.dept
  boost.iter=gbm.perf(boost.mpg,method = "cv")
  boost.predict = predict(boost.mpg,test,n.trees = boost.iter )
  boost.roc = roc(test$high_mileage,boost.predict)
  coords(boost.roc, "best")
  boost.predict.class = ifelse(boost.predict > coords(boost.roc, "best")["threshold"], "TURE", "FALSE")
  a = table(boost.predict.class,test$high mileage)
  accuracy[i] = (a[1,1] + a[2,2])/(a[1,1]+a[1,2]+a[2,1]+a[2,2])
}
```



```
meanAccuracy = (accuracy[1] + accuracy[2] +accuracy[3])/3
meanAccuracy
```

```
## [1] 0.9209586
```

f. SVM with linear kernel tuning

```
library(ISLR)
library(e1071)
Auto$origin=factor(Auto$origin)
table = Auto[1:8]
meanOfmpg = mean(Auto$mpg)
```

```
set.seed(1)
folds=sample(1:k,nrow(table),replace = TRUE)
high mileage =ifelse(Auto$mpg<meanOfmpg,"false","true")
newTable = data.frame(table[2:7],high_mileage)
tableSet = data.frame(newTable,folds)
accuracy = rep(0,3)
for(i in 1:k){
  train = tableSet[which(tableSet$folds != i),]
  test = tableSet[which(tableSet$folds == i),]
  tune.out=tune(svm,high_mileage~.,data=train,kernel="linear",
                ranges=list(cost=c(0.001, 0.01, 0.1, 1,5,10,100)))
  bestmod = tune.out$best.model
  mpg.pred = predict(bestmod,test)
  a = table(predict=mpg.pred,truth = test$high_mileage)
  accuracy[i] = (a[1,1] + a[2,2])/(a[1,1]+a[1,2]+a[2,1]+a[2,2])
meanAccuracy = (accuracy[1] + accuracy[2] +accuracy[3])/3
meanAccuracy
## [1] 0.8922818
  g. SVM with polynomial kernel and tuning
library(ISLR)
library(e1071)
Auto$origin=factor(Auto$origin)
table = Auto[1:8]
meanOfmpg = mean(Auto$mpg)
k=3
set.seed(1)
folds=sample(1:k,nrow(table),replace = TRUE)
high_mileage =ifelse(Auto$mpg<meanOfmpg,"false","true")
```

[1] 0.8846483

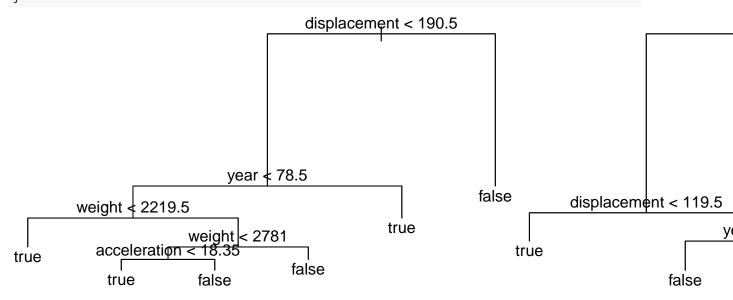
Report a. Report the accuracy if you predicted the most frequent class for all observations. This is your baseline.

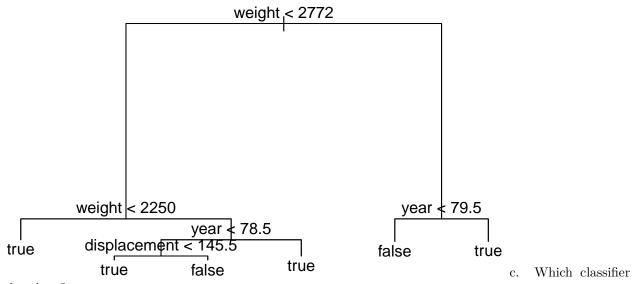
Logistic regression tuning:0.8875269 Decision trees with tuning:0.9057141 Bagging with tuning:0.9048993 Random forest with tuning:0.9180386 Boosting with tuning:0.9209586 SVM with linear kernel tuning:0.8922818 SVM with polynomial kernel and tuning:0.8846483

b. Plot of cross validation accuracy as a function of the tuning parameter for each classifier.

b.1 For the decision tree, plot the tree.

```
library(ISLR)
library(tree)
Auto$origin=factor(Auto$origin)
table = Auto[1:8]
meanOfmpg = mean(Auto$mpg)
k=3
set.seed(1)
folds=sample(1:k,nrow(table),replace = TRUE)
high_mileage =ifelse(Auto$mpg<meanOfmpg,"false","true")
newTable = data.frame(table[2:7],high_mileage)
tableSet = data.frame(newTable,folds)
accuracy = rep(0,3)
for(i in 1:3){
  train = tableSet[which(tableSet$folds != i),]
  test = tableSet[which(tableSet$folds == i),]
  tree.mpg = tree(high_mileage~.,data = train)
  cv.mpg =cv.tree(tree.mpg ,FUN=prune.misclass )
  prune.mpg=prune.misclass(tree.mpg,best=4)
  plot(prune.mpg)
  text(prune.mpg ,pretty=0)
}
```





does best?

Answer???Boosting with tuning does best since the accuracy 0.9209586 is the highest.

d. Which one would you use? And does this classifier match your initial guess?

Answer: We would use Boosting with tuning. This classifier match our initial guess.