is a basic reference that discusses light in terms of electromagnetic theory. Electromagnetic energy propagation is covered in some detail by Felsen and Marcuvitz [1994].

The area of image sensing is quite broad and very fast moving. An excellent source of information on optical and other imaging sensors is the International Society for Optical Engineering (SPIE). The following are representative publications by the SPIE in this area: Blouke et al. [2001], Hoover and Doty [1996], and Freeman [1987].

The image model presented in Section 2.3.4 is from Oppenheim, Schafer, and Stockham [1968]. A reference for the illumination and reflectance values used in that section is the *IES Lighting Handbook* [2000]. For additional reading on image sampling and some of its effects, such as aliasing, see Bracewell [1995]. The early experiments mentioned in Section 2.4.3 on perceived image quality as a function of sampling and quantization were reported by Huang [1965]. The issue of reducing the number of samples and gray levels in an image while minimizing the ensuing degradation is still of current interest, as exemplified by Papamarkos and Atsalakis [2000]. For further reading on image shrinking and zooming, see Sid-Ahmed [1995], Unser et al. [1995], Umbaugh [1998], and Lehmann et al. [1999]. For further reading on the topics covered in Section 2.5, see Rosenfeld and Kak [1982], Marchand-Maillet and Sharaiha [2000], and Ritter and Wilson [2001]. Additional reading on linear systems in the context of image processing may be found in Castleman [1996].

Problems

★2.1   Using the background information provided in Section 2.1, and thinking purely in geometric terms, estimate the diameter of the smallest printed dot that the eye can discern if the page on which the dot is printed is 0.2 m away from the eyes. Assume for simplicity that the visual system ceases to detect the dot when the image of the dot on the fovea becomes smaller than the diameter of one receptor (cone) in that area of the retina. Assume further that the fovea can be modeled as a square array of dimensions 1.5 mm × 1.5 mm, and that the cones and spaces between the cones are distributed uniformly throughout this array.

2.2   When you enter a dark theater on a bright day, it takes an appreciable interval of time before you can see well enough to find an empty seat. Which of the visual processes explained in Section 2.1 is at play in this situation?

★2.3   Although it is not shown in Fig. 2 10, alternating current certainly is part of the electromagnetic spectrum. Commercial alternating current in the United States has a frequency of 60 Hz. What is the wavelength in kilometers of this component of the spectrum?

2.4   You are hired to design the front end of an imaging system for studying the boundary shapes of cells, bacteria, viruses, and protein. The front end consists, in this case, of the illumination source(s) and corresponding imaging camera(s). The diameters of circles required to enclose individual specimens in each of these categories are 50, 1, 0.1, and 0.01 μm, respectively.

(a) Can you solve the imaging aspects of this problem with a single sensor and camera? If your answer is yes, specify the illumination wavelength band and the type of camera needed. Identify the camera as being a color camera, far-infrared camera, or whatever appropriate name corresponds to the illumination source.

(b) If your answer in (a) is no, what type of illumination sources and corre-

and cameras as requested in part (a). Use the *minimum* number of illumination sources and cameras needed to solve the problem.

2.5   A CCD camera chip of dimensions 7 × 7 mm, and having 1024 × 1024 elements, is focused on a square, flat area, located 0.5 m away. How many line pairs per mm will this camera be able to resolve? The camera is equipped with a 35-mm lens. (*Hint:* Model the imaging process as in Fig. 2.3, with the focal length of the camera lens substituting for the focal length of the eye.)

★**2.6**   An automobile manufacturer is automating the placement of certain components on the bumpers of a limited-edition line of sports cars. The components are color coordinated, so the robots need to know the color of each car in order to select the appropriate bumper component. Models come in only four colors: blue, green, red, and white. You are hired to propose a solution based on imaging. How would you solve the problem of automatically determining the color of each car, keeping in mind that *cost* is the most important consideration in your choice of components?

2.7   Suppose that a flat area with center at (x_0, y_0) is illuminated by a light source with intensity distribution

$$i(x, y) = Ke^{-[(x-x_0)^2+(y-y_0)^2]}.$$

Assume for simplicity that the reflectance of the area is constant and equal to 1.0, and let $K = 255$. If the resulting image is digitized with k bits of intensity resolution, and the eye can detect an abrupt change of eight shades of intensity between adjacent pixels, what value of k will cause visible false contouring?

2.8   Sketch the image in Problem 2.7 for $k = 2$.

★**2.9**   A common measure of transmission for digital data is the *baud rate*, defined as the number of bits transmitted per second. Generally, transmission is accomplished in packets consisting of a start bit, a byte (8 bits) of information, and a stop bit. Using these facts, answer the following:

(a) How many minutes would it take to transmit a 1024 × 1024 image with 256 gray levels using a 56K baud modem?

(b) What would the time be at 750K baud, a representative speed of a phone DSL (digital subscriber line) connection?

2.10   High-definition television (HDTV) generates images with a resolution of 1125 horizontal TV lines interlaced (where every other line is painted on the tube face in each of two fields, each field being 1/60th of a second in duration). The width-to-height aspect ratio of the images is 16:9. The fact that the horizontal lines are distinct fixes the vertical resolution of the images. A company has designed an image capture system that generates digital images from HDTV images. The resolution of each TV (horizontal) line in their system is in proportion to vertical resolution, with the proportion being the width-to-height ratio of the images. Each pixel in the color image has 24 bits of intensity resolution, 8 bits each of a red, a green, and a blue image. These three "primary" images form a color image. How many bits would it take to store a 2-hour HDTV program?

★**2.11**   Consider the two image subsets, S_1 and S_2, shown in the following figure. For $V = \{1\}$, determine whether these two subsets are (a) 4-adjacent, (b) 8-adjacent, or (c) m-adjacent.

	S_1				S_2				
0	0	0	0	0	0	0	1	1	0
1	0	0	1	0	0	1	0	0	1
1	0	0	1	0	1ʹ	1	0	0	0
0	0	1	1	1	0	0	0	0	0
0	0	1	1	1	0	0	1	1	1

★2.12   Develop an algorithm for converting a one-pixel-thick 8-path to a 4-path.

2.13   Develop an algorithm for converting a one-pixel-thick m-path to a 4-path.

2.14   Show that the boundary of the region, as defined in Section 2.5.2, is a closed path.

★2.15   Consider the image segment shown.

(a) Let $V = \{0, 1\}$ and compute the lengths of the shortest 4-, 8-, and m-path between p and q. If a particular path does not exist between these two points, explain why.

(b) Repeat for $V = \{1, 2\}$.

$$
\begin{array}{cccc}
3 & 1 & 2 & 1\,(q) \\
2 & 2 & 0 & 2 \\
1 & 2 & 1 & 1 \\
(p)\,1 & 0 & 1 & 2
\end{array}
$$

★2.16   (a) Give the condition(s) under which the D_4 distance between two points p and q is equal to the shortest 4-path between these points.

(b) Is this path unique?

2.17   Repeat Problem 2.16 for the D_8 distance.

★2.18   In the following chapter, we will deal with operators whose function is to compute the sum of pixel values in a small subimage area, S. Show that these are linear operators.

2.19   The median, ζ, of a set of numbers is such that half the values in the set are below ζ and the other half are above it. For example, the median of the set of values $\{2, 3, 8, 20, 21, 25, 31\}$ is 20. Show that an operator that computes the median of a subimage area, S, is nonlinear.

2.20   A plant produces a line of translucent miniature polymer squares. Stringent quality requirements dictate 100% visual inspection, and the plant manager finds the use of human inspectors increasingly expensive. Inspection is semiautomated. At each inspection station, a robotic mechanism places each polymer square over a light located under an optical system that produces a magnified image of the square. The image completely fills a viewing screen measuring 80 × 80 mm. Defects appear as dark circular blobs, and the inspector's job is to look at the screen and reject any sample that has one or more such dark blobs with a diameter of 0.8 mm or larger, as measured on the scale of the screen. The manager believes that, if she can find a way to automate the process completely, she will increase profits by 50%. She also believes that success in this project will aid her climb up the corporate ladder. After much investigation, the manager decides that the way to solve the problem is to view each inspection screen with a CCD TV camera and feed the output of the

camera into an image processing system capable of detecting the blobs, measuring their diameter, and activating the accept/reject buttons previously operated by an inspector. She is able to find a system that can do the job, as long as the smallest defect occupies an area of at least 2 × 2 pixels in the digital image. The manager hires you to help her specify the camera and lens system, but requires that you use off-the-shelf components. For the lenses, assume that this constraint means any integer multiple of 25 mm or 35 mm, up to 200 mm. For the cameras, it means resolutions of 512 × 512, 1024 × 1024, or 2048 × 2048 pixels. The *individual* imaging elements in these cameras are squares measuring 8 × 8 μm, and the spaces between imaging elements are 2 μm. For this application, the cameras cost much more than the lenses, so the problem should be solved with the lowest-resolution camera possible, based on the choice of lenses. As a consultant, you are to provide a written recommendation, showing in reasonable detail the analysis that led to your conclusion. Use the same imaging geometry suggested in Problem 2.5.