

3.1

a)  $6^4 6^3 6^2 6^1 6^0$

$1296 \quad 216 \quad 36 \quad 6 \quad 1$

$6^4 = 1296$

$6^3 = 216$

$6^2 = 36$

$6^1 = 6$

$6^0 = 1$

b)  $24531_6 = 2 \times 6^4 + 4 \times 6^3 + 5 \times 6^2 + 3 \times 6^1 + 1 \times 6^0$

$2 \times 1296 + 4 \times 216 + 5 \times 36 + 3 \times 6 + 1 \times 1$

$2592 + 864 + 180 + 18 + 1 = \boxed{3655}$

3.2

$16^3 \quad 16^2 \quad 16^1 \quad 16^0$

$4096 \quad 256 \quad 16 \quad 1$

$2^{12} \quad 2^8 \quad 2^4 \quad 2^0$

$16^3 = 4096 \quad 2^8$

$16^2 = 256 \quad 2^4$

$16^1 = 16 \quad 2^1$

$16^0 = 1 \quad 2^0$

3.3 a)  $4E \rightarrow 4 \mid 184$

$= 78$

$16 \times 4 \quad 16^1 \times 18 \quad 16^0$

$15 + 40$

$(4 \times 16^1) + (18 \times 16^0)$

$64 + 14 = 78$

$+ 256$

$75$

$768$

b)  $307$

$3 \mid 13 \mid 7$

$(3 \times 16^2) + (13 \times 16^1) + (7 \times 16^0)$

$768 + 208 + 7$

$= 983$

$3 \times 4096$

c)  $3070$

$3 \mid 13 \mid 7 \mid 0$

$(3 \times 16^3) + (13 \times 16^2) + (7 \times 16^1) + (0 \times 16^0)$

$(3 \times 4096) + (13 \times 256) + (7 \times 16) + (0 \times 1)$

$12288 + 3328 + 112 + 0 = \boxed{15,728}$

$\times 13$

$18$

$+ 78$

$130$

$208$

$47$

$112$

$0$

$\times 256$

$18$

$+ 768$

$2560$

$3328$

											10	11	12	13	14	15	16
3.7	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F	10
0	0	C	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F	10
2	0	2	4	6	8	A	C	E	10	12	14	16	18	1A	1C	1E	20
3	0	3	6	9	C	F	12	15	18	1B	1E	21	24	27	2A	2D	30
4	0	4	8	C	10	14	18	1C	20	24	28	2C	30	34	38	3C	40
5	0	5	A	F	14	19	1E	23	28	2D	32	37	3C	41	46	4B	50
6	0	6	C	12	18	1E	24	2A	30	36	3C	42	48	4E	54	5A	60
7	0	7	E	15	1C	23	2A	31	38	3F	4C	4D	54	5B	62	69	70
8	0	8	10	18	20	28	30	38	40	48	50	58	60	68	70	78	80
9	0	9	12	1B	24	2D	36	3F	48	51	5A	61	6C	75	7E	87	90
10	A	0	A	14	1E	28	32	3C	46	50	5A	64	6E	78	82	8C	96
11	B	0	B	16	21	2C	37	42	4D	58	63	6E	79	84	8F	9A	A5
12	C	0	C	18	24	30	3C	48	54	60	6C	78	84	90	9C	A8	B4
13	D	0	D	1A	27	34	41	4E	5B	68	75	82	8F	9C	A9	B6	C3
14	E	0	E	1C	2A	38	46	54	62	70	7E	8C	9A	A8	B6	CA	D2
15	F	0	F	1E	2D	3C	4B	5A	69	78	87	96	A5	B4	C3	D2	E1
16	10	0	10	20	30	40	50	60	70	80	90	A0	B0	C0	D0	E0	100

$$27 = 16 + 11$$

$$28 = 16 + 12 \quad 32 \quad 35 \quad \frac{32}{32, 3}$$

$$70 = 16 + 14$$

49 31

$$\begin{array}{r} \text{3.7 b) } \cancel{2AB3} \\ + \cancel{35DC} \\ \hline \cancel{5F8F} \end{array}$$

$$\begin{array}{r} 2AB3 \\ + 35DC \\ \hline 501F \checkmark \end{array}$$

$$\begin{array}{r} \text{c) } \overset{111}{1FF9} \\ + \quad F7 \\ \hline 20F0 \checkmark \end{array}$$

$$\begin{array}{r} \text{d) } \overset{3}{2E26} \\ \times \quad 4X \\ \hline 1607C \\ + 38980 \\ \hline 0F6EC \end{array}$$

$$\begin{array}{r} \text{3.8 a) } \overset{111111}{101101101} \\ + \quad 10011011 \\ \hline 1000001000 \end{array}$$

$$\begin{array}{r} \text{b) } \overset{1111111}{11011111} \\ + \quad 11011111 \\ \hline 1101111110 \end{array}$$

$$\begin{array}{r} \text{c) } \overset{1}{11010011} \\ + \quad 10001010 \\ \hline 101011101 \end{array}$$

$$\begin{array}{r} \text{d) } \overset{11}{1101} \quad \text{7} \quad \overset{1}{10111} \\ 1010 \\ \hline 111 \quad \text{7} \quad + \quad \overset{1100}{100011} \\ + \quad 101 \end{array}$$

$$\begin{array}{r} \text{e) a) } \overset{0001}{0001} \overset{0110}{0110} \overset{1101}{1101} \rightarrow \\ + \quad (0000)(0001)(0011) \end{array}$$

$$\begin{array}{r} \overset{11}{1600} \\ 09B \\ \hline 008 \rightarrow (0010)(0000)(1000) \end{array}$$

$$\begin{array}{r} \text{b) } (0001)(1011)(1111) \rightarrow 1BF \\ (0001)(1011)(1111) \rightarrow 1BF \end{array}$$

$$\begin{array}{r} 37E \rightarrow (0011)(0111)(1110) \end{array}$$



✱

3.8 | c)  $(11010011) \rightarrow D3$   
 $(1000010) \rightarrow 8A$   
 $\underline{\hspace{1cm}} \quad \quad \quad 150 \rightarrow (0001)(0101)(1101)$

d)  $(1101) \rightarrow 0 \geq 17$   
 $(1010) \rightarrow A \geq$   
 $(0111) \rightarrow 7 \geq C$   
 $(0101) \rightarrow 5$   
 $\underline{\hspace{1cm}} \quad \quad \quad (2)(3) \rightarrow (0010)(0011)$

3.9 | a)  $\begin{array}{r} 1101 \\ \times 10.1 \\ \hline 000101 \\ + 010100 \\ + 101000 \\ \hline 1000001 \end{array}$

b)  $\begin{array}{r} 11011 \\ \times 1011 \\ \hline 1011 \\ + 10110 \\ + 11011000 \\ + 10110000 \\ \hline 100101001 \end{array}$

3.10 | a)  $\begin{array}{r} 0001101100.000 \\ 110 \overline{) 11010001001000} \\ \underline{- 0110} \phantom{0000000000} \\ 01000 \phantom{0000000000} \\ \underline{- 0110} \phantom{0000000000} \\ 001001 \phantom{0000000000} \\ \underline{- 0110} \phantom{0000000000} \\ 0110 \phantom{0000000000} \\ \underline{- 110} \phantom{0000000000} \\ 0000000000 \end{array}$  remainder 1. (I don't think you can have a <sup>fraction</sup> remainder of a bit)

★

3.10)  $00010001011$  Remainder: 111

(11)  $1011 \sqrt{11000000000}$

$-1011$

$00010000$

$-01011$

$0010100$

$-1011$

$1001018$

$-101111$

$0000$

00P5  $\rightarrow 3.11 \sqrt{6026}$

$8^1 = 8$   $6 \times 8^3 + 0 \times 8^2 + 2 \times 8^1 + 6 \times 8^0$

$8^2 = 64$   $6 \times 512 + 0 + 2 \times 8 + 6 \times 1$

$8^3 = 512$   $3072 + 0 + 16 + 6$

$8^4 = 4096$   $3072 + 22$

3094

3.16)  $(0101010101010101)$

5 ABBA  $\rightarrow$  5BBA

b)  $(1111111111110001)$

F F F 1  $\rightarrow$  FFFI

c)  $(000111111101111)$

1 F E F  $\rightarrow$  1FEF

d)  $(011000110001001)$

6 3 1 9  $\rightarrow$  6319

3.17) a)  $(4FGA)$  b)  $9902$

$0100 \quad 1111 \quad 0110 \quad 1010$   $1001 \quad 1001 \quad 0000 \quad 0010$

c)  $A3AB$  d)  $1000$

$1010 \quad 0011 \quad 1010 \quad 1011$   $0001 \quad 0000 \quad 0000 \quad 0000$



3.25/a)

6640625

6640625 \* 16

16

3'984'3'750

+ 6.6406250

10.6250000 → 10 = A

3.62500 \* 16 =

x 16

3.75000

+ 0.25000

10.00000

→ 10 = A

→ .AA

b) .3333

x 16

1.9998

+ 3.3330

5.3328

→ 5

2.3328

16

1.9998

+ 33280

5.3148

→ 5

3148

16

18858

+ 31480

5.0338

→ 5

224

.0338

x 16

2028

+ 3380

.5408 → 0

10 16  
16 609  
48  
129

$$\begin{array}{r}
 \star \\
 \begin{array}{r}
 24 \\
 .5408 \\
 \times 16 \\
 \hline
 3.2448 \\
 + 54080 \\
 \hline
 8.6528 \rightarrow 8 \\
 \hline
 314 \\
 .6528
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{r}
 16 \\
 3.9168 \\
 + 65280 \\
 \hline
 10.4448 \rightarrow A \\
 \hline
 .9948
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{r}
 \times 1116 \\
 2.6688 \\
 + 44480 \\
 \hline
 7.1168 \rightarrow 7 \\
 \hline
 1168 \\
 \times 16
 \end{array}
 \end{array}$$

.5550 determined to be irrational,  
Because You can never get rid of the 8

$$\begin{array}{r}
 C. \quad 69 \quad \cancel{116} \quad 00.26953125 \\
 \hline
 256 \quad 256 \sqrt{69.00000000} \\
 \begin{array}{r}
 - 576 \\
 \hline
 1780 \\
 \downarrow 1536 \\
 \hline
 2440 \\
 - 2304 \\
 \hline
 1360 \\
 - 1280 \\
 \hline
 800 \\
 - 768 \\
 \hline
 320 \\
 - 256 \\
 \hline
 640 \\
 - 512 \\
 \hline
 1280 \\
 - 1280 \\
 \hline
 0000
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 29 \\
 256 \\
 \times 5 \\
 \hline
 1280
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{r}
 1453113 \\
 .26953125 \\
 \times 16 \\
 \hline
 4.31250000 \rightarrow 4 \\
 \hline
 1.61718750 \\
 + 2.69531250 \\
 \hline
 4.31250000 \\
 \times 3125 \\
 \hline
 1.8750 \\
 + 3.1250 \\
 \hline
 5.0000 \rightarrow 5
 \end{array}
 \end{array}$$

1451



3.26

a)  $.1001001 = 73 = .73 / 128_{or} 2^7 = .5703125$

b) 0.3A2<sub>16</sub>

$(0011010101010) + .1110100010 =$   
 $512 + 256 + 128 + 32 + 2 = 930 / 16^3_{or} 930 / 4096 = .2270507813$

c) .2A1

$00101010001$   
 $512 + 128 + 32 + 1 = 673 / 1728_{or} 1728 = .3894675926$

3.27

a)  $27.625 = 27$

$\begin{array}{r} 625 \\ - 512 \\ \hline 113 \\ - 64 \\ \hline 49 \end{array}$

512	256	128	64	32	16	8	4	2	1
0	0	0	0	0	1	1	0	1	1
1	0	0	1	1	1	0	0	0	1

$27.625 \cdot 2^3_{or} 8 = 221_{or} 1101110$

~~1101110001~~

b)  $4192.37761 \cdot 4192$

$37761$

131072	65536	32768	16384	8192	4096	2048	1024	512	256	128	64	32	16	8	4	2	1
0	0	0	0	1	1	0	0	0	0	0	0	0	0	1	1	0	0
				1	0	0	0	0	0	1	0	1	0	0	0	0	0

$4192.37761 \cdot 2^5_{or} 32 = 134156.08352$

$100000110000001100.000000101000001$