

# DYNAMIC PROGRAMMING 4

LINTCODE NO. 92

# BACKPACK

<http://www.lintcode.com/en/problem/backpack/>



# PROBLEM DESCRIPTION

- Given  $n$  items with size  $A_i$ , an integer  $m$  denotes the size of a backpack. How full you can fill this backpack?
- Example
  - If we have 4 items with size  $[2, 3, 5, 7]$ , the backpack size is 11, we can select  $[2, 3, 5]$ , so that the max size we can fill this backpack is 10. If the backpack size is 12. we can select  $[2, 3, 7]$  so that we can fulfill the backpack. Your function should return the max size we can fill in the given backpack.

# IDEA

- Use  $dp[n]$  to denote the max capacity we may obtain if the backpack size is  $n$
- Nested loop structure looks as follows
  - Outer loop goes through the incoming item size
  - Inner loop goes through the backpack size
- DP function
  - $\max(dp[n], dp[n - \text{incoming\_item}] + \text{incoming\_item})$



# SOLUTION

- [https://github.com/Brady31027/lintcode/tree/master/92\\_Backpack](https://github.com/Brady31027/lintcode/tree/master/92_Backpack)

LINTCODE NO. 125

# BACKPACK II

<http://www.lintcode.com/en/problem/backpack-ii/>



# PROBLEM DESCRIPTION

- Given  $n$  items with size  $A_i$  and value  $V_i$ , and a backpack with size  $m$ . What's the maximum value can you put into the backpack?
- Example
  - Given 4 items with size  $[2, 3, 5, 7]$  and value  $[1, 5, 2, 4]$ , and a backpack with size 10. The maximum value is 9.

# IDEA

- Similar to No.92 Backpack except
  - Take value into account
  - DP function

$$dp[space] = \max(dp[space], dp[space - A[item\_idx]] + V[item\_idx])$$



# SOLUTION

- [https://github.com/Brady31027/lintcode/tree/master/125\\_Backpack\\_II](https://github.com/Brady31027/lintcode/tree/master/125_Backpack_II)

LINTCODE NO. 564

# BACKPACK VI

<http://www.lintcode.com/en/problem/backpack-vi/>



# PROBLEM DESCRIPTION

- Given an integer array `nums` with all positive numbers and no duplicates, find the number of possible combinations that add up to a positive integer `target`.
- Example
  - Given `nums = [1, 2, 4]`, `target = 4`
    - `[1, 1, 1, 1]`, `[1, 1, 2]`, `[1, 2, 1]`, `[2, 1, 1]`, `[2, 2]`, `[4]`

# IDEA

- Similar to Leetcode Combination Sum IV
  - <https://leetcode.com/problems/combination-sum-iv/#/description>
  - Refer to [https://github.com/Brady31027/leetcode/blob/master/reports/dynamic\\_programming\\_5.pdf](https://github.com/Brady31027/leetcode/blob/master/reports/dynamic_programming_5.pdf)



# SOLUTION

- [https://github.com/Brady31027/lintcode/tree/master/564\\_Backpack\\_VI](https://github.com/Brady31027/lintcode/tree/master/564_Backpack_VI)

# FOLLOW UP

- There are backpack III, IV, and V
  - Access denied
- <https://segmentfault.com/a/1190000006325321>