CS202 - Algorithm Analysis

Graph Algorithms - Module2

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Graph Traversal

- **Graph traversal** is a process used to visit each node or vertex in a connected graph.
- Two popular algorithms are generally used for the traversal of a graph, namely, Depth First Search (DFS) and Breadth First Search (BFS).

An important: application of graph traversal is to detect cycles in a Graph.

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- **Graph traversal** is a process used to visit each node or vertex in a connected graph.
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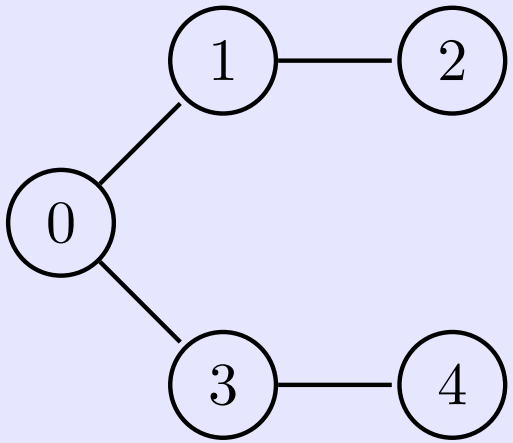
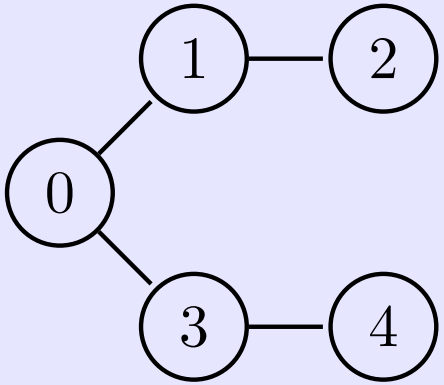
An important: application of graph traversal is to detect cycles in a Graph.

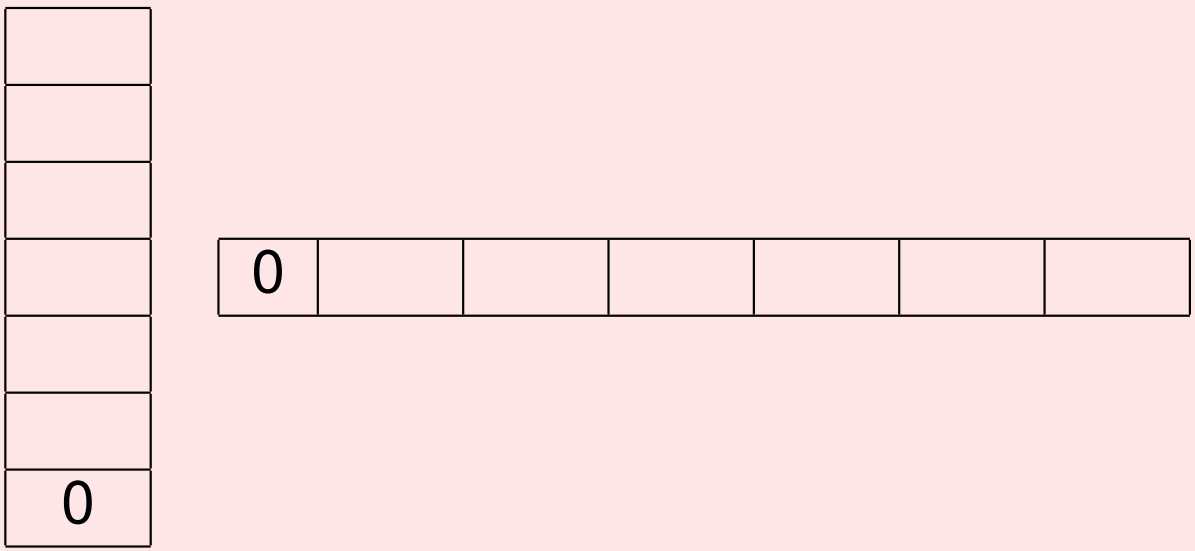
DFS example



Traverse graph by starting from 0

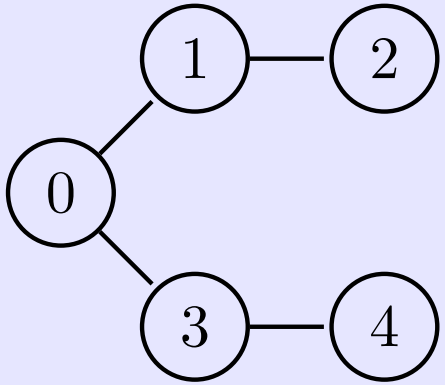
DFS example

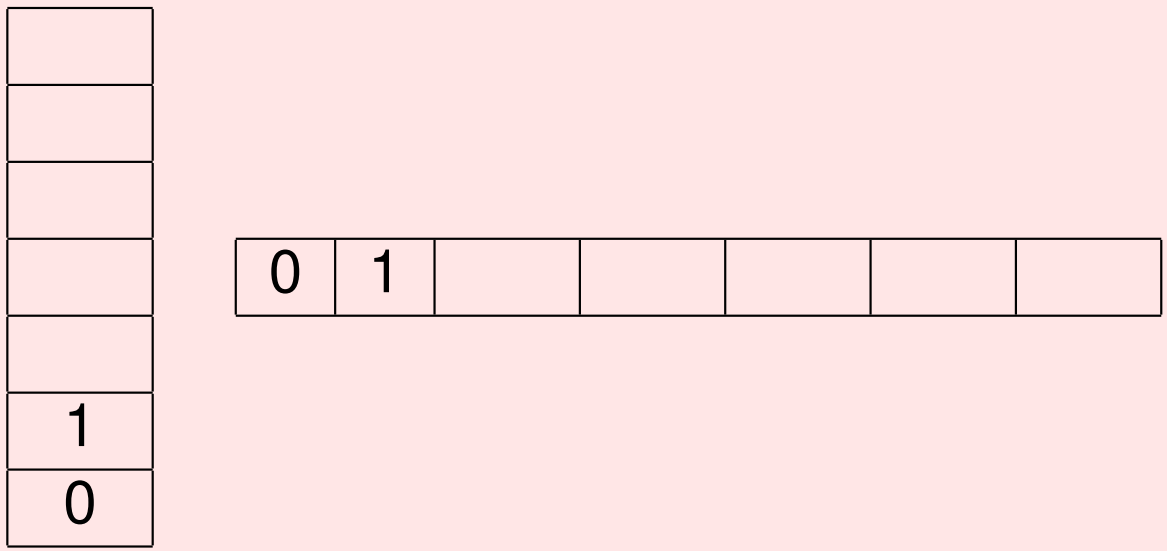




Stack

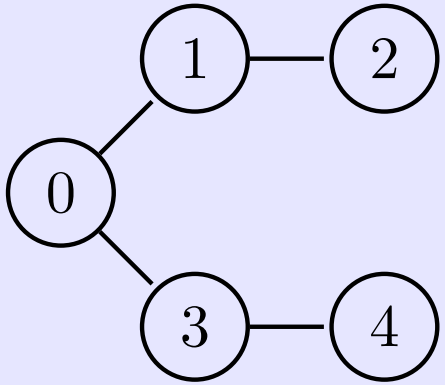
DFS example

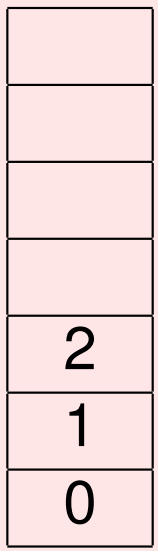


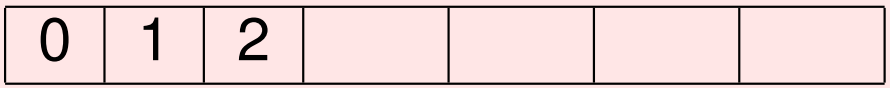


Stack

DFS example

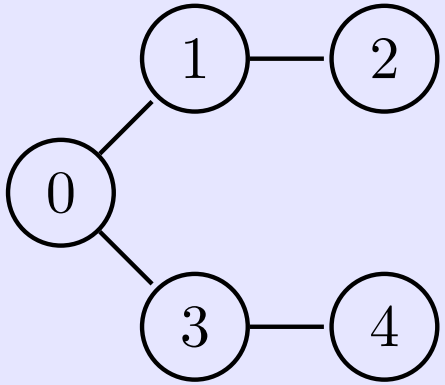


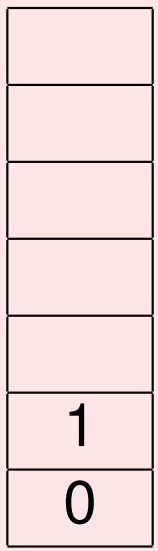




Stack

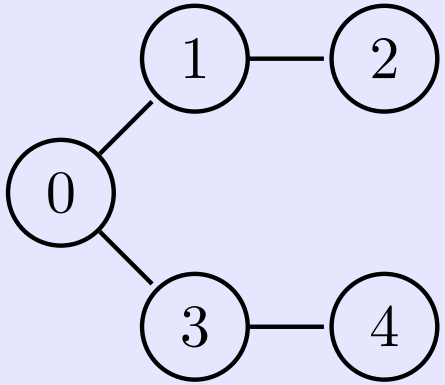
DFS example

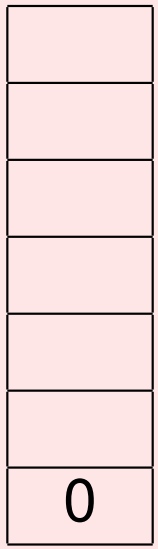




Stack

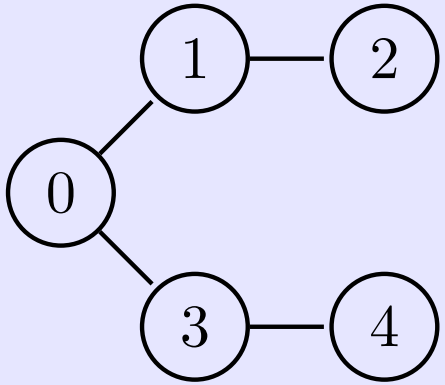
DFS example

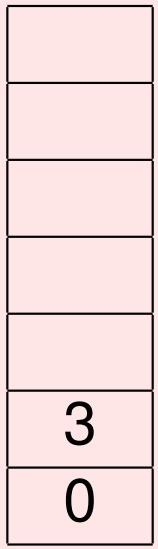




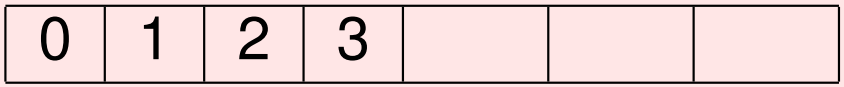
Stack

DFS example

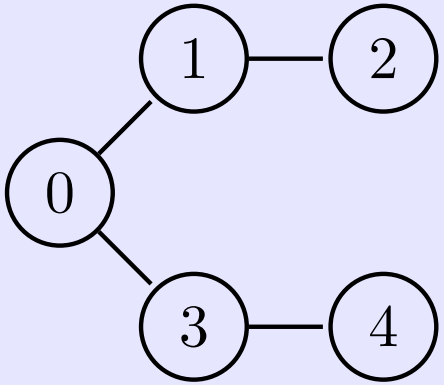


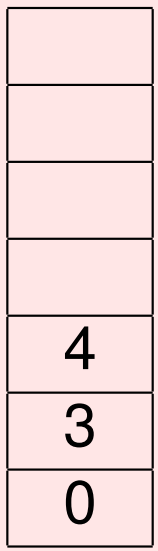


Stack



DFS example





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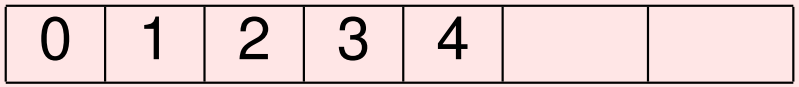
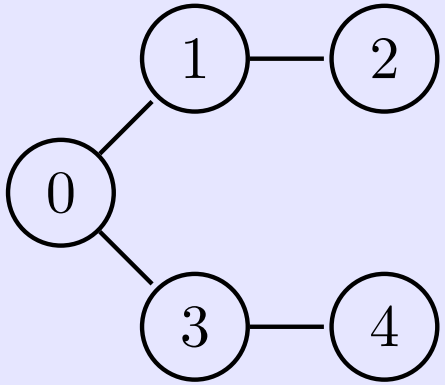
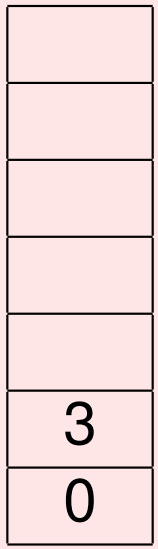


DFS example

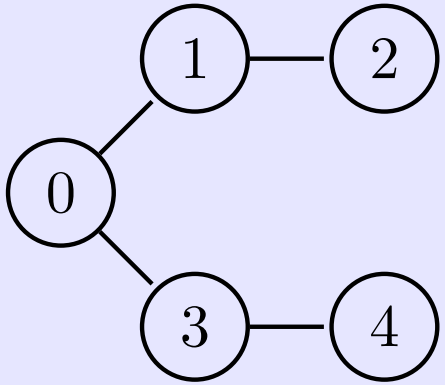


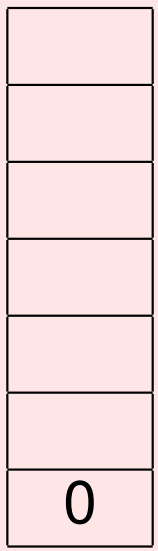


Stack

0	1	2	3	4		

DFS example

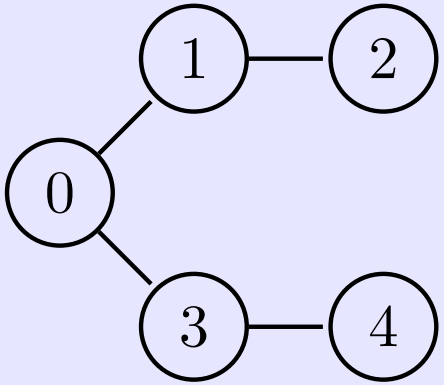


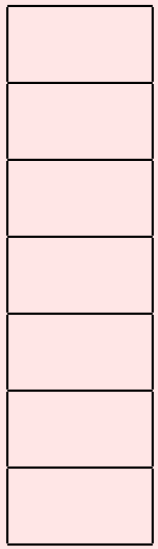


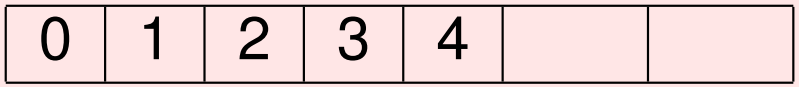
0	1	2	3	4		

Stack

DFS example







Stack

Depth First Search (DFS) Algorithm

DFS(G, u)

Input: Graph G = (V, E) directed or undirected, vertex u (element of) V

Output: DFS traversal order from node u

```
create a Stack S
mark u as visited
push(S, u)
while S is not empty
    v = peek(S)
    if v has an unvisited neighbour w then
        mark w as visted
        push(S, w)
    else
        pop(S)
    end if
end while
```

Complexity Analysis

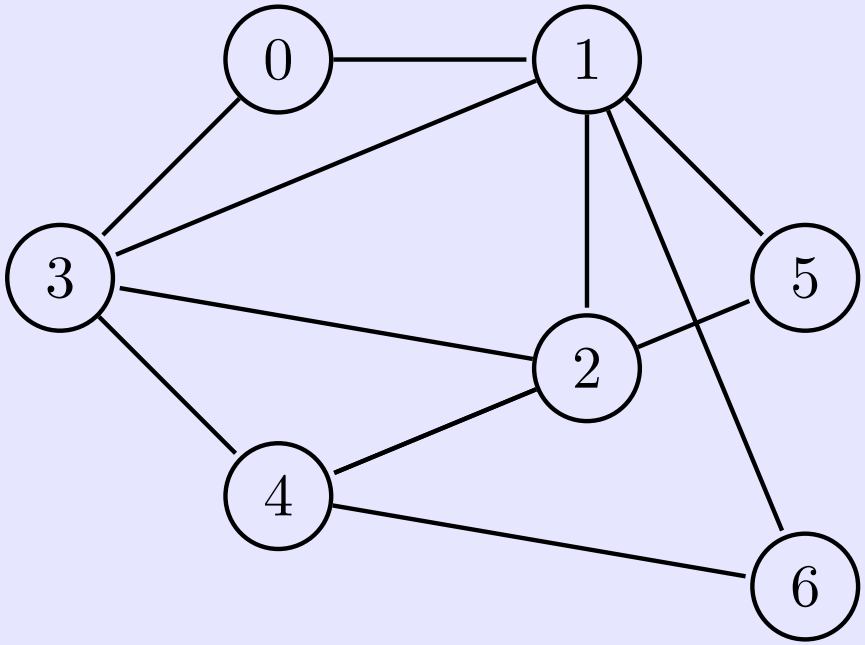
Time Complexity - O(V + E)

Detect Cycle

How do we detect cycles in a Graph using DFS?

During DFS traversal, if we find a node that is already in the Stack then there is a cycle.

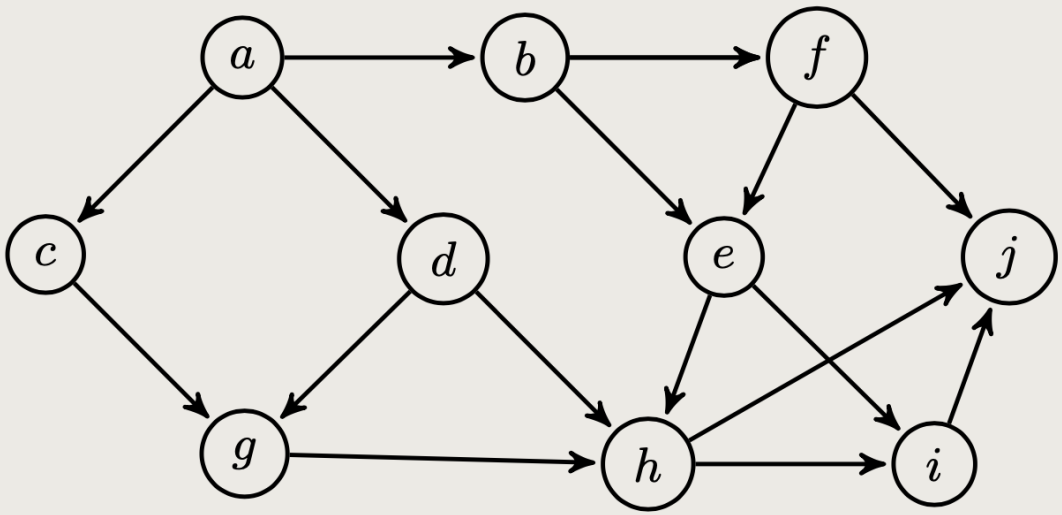
Let us Try this



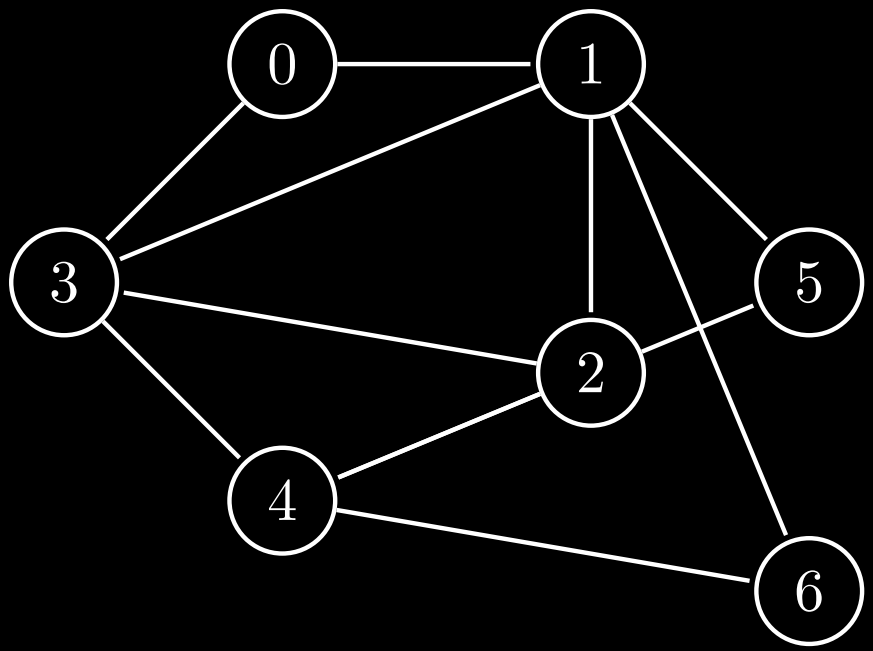
Traverse graph by starting from 0

Try out 1

- **Compute** the DFS traversal order in the Graph provided below, starting from vertex **a**:

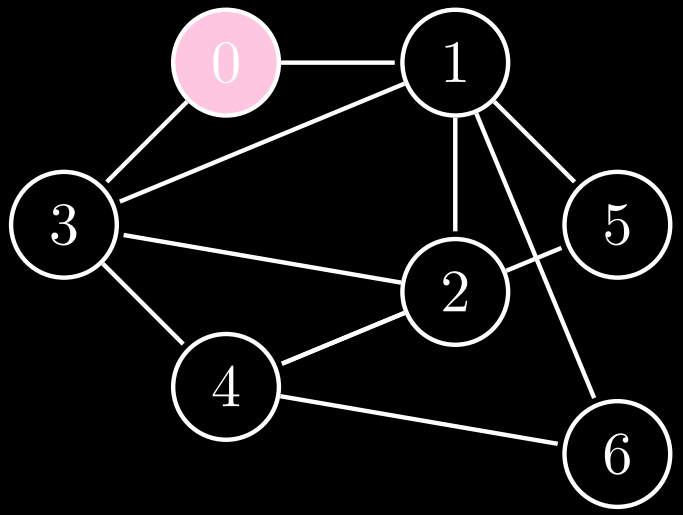


BFS example

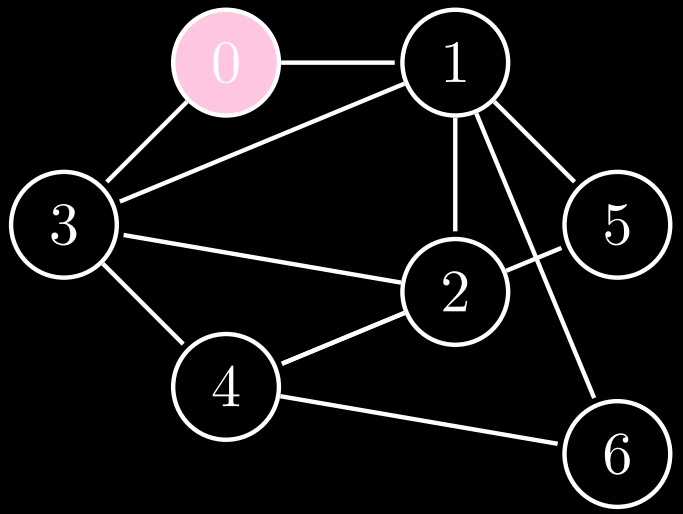


Traverse graph by starting from 0

BFS example (1)



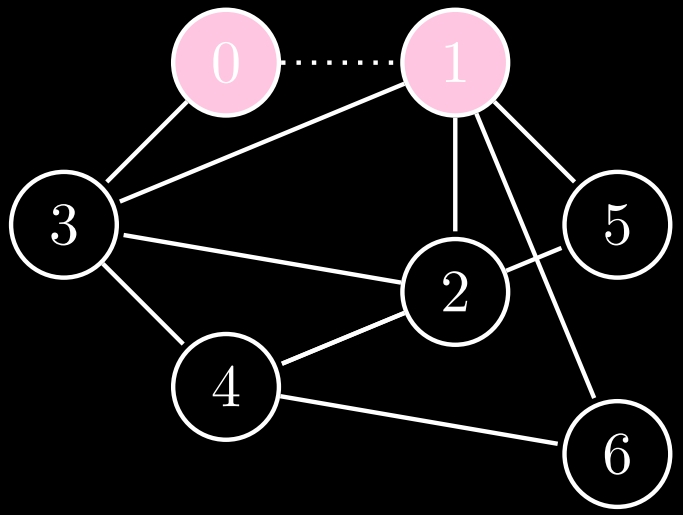
BFS example (1)



Queue	~~0~~	1	3				

Result	0						

BFS example (1)



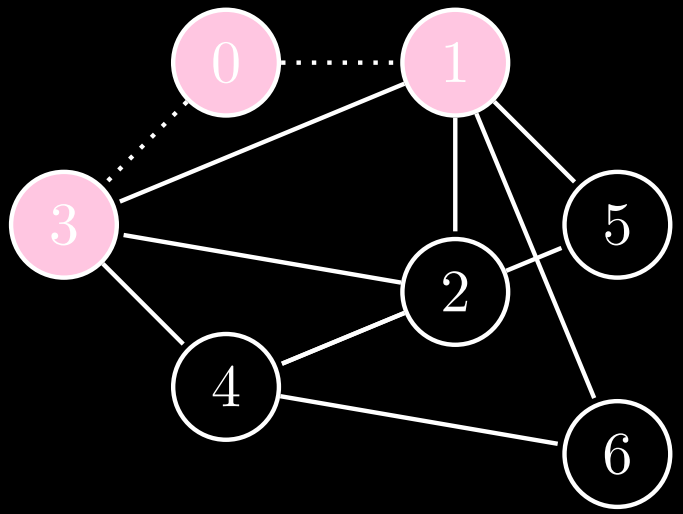
Queue

~~1~~	3	2	5	6		

Result

0	1					

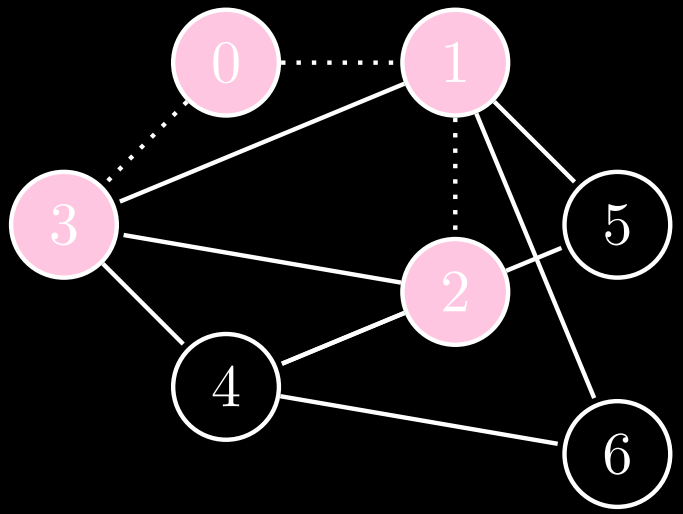
BFS example (1)



Queue	~~3~~	2	5	6	4		

Result	0	1	3				

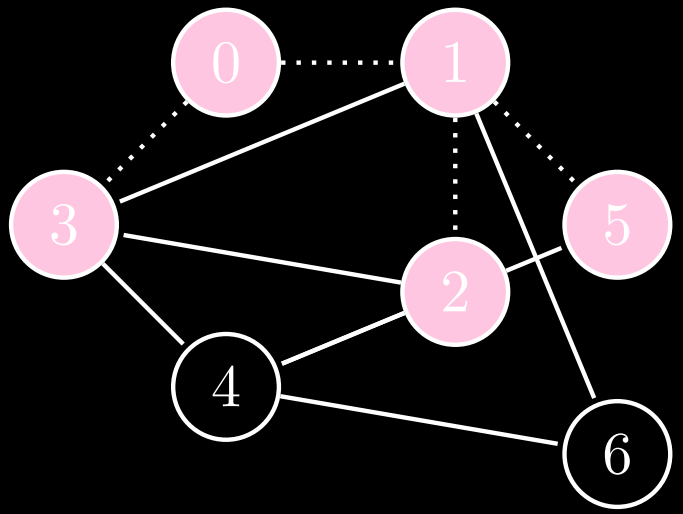
BFS example (1)



Queue	~~2~~	5	6	4			

Result	0	1	3	2			

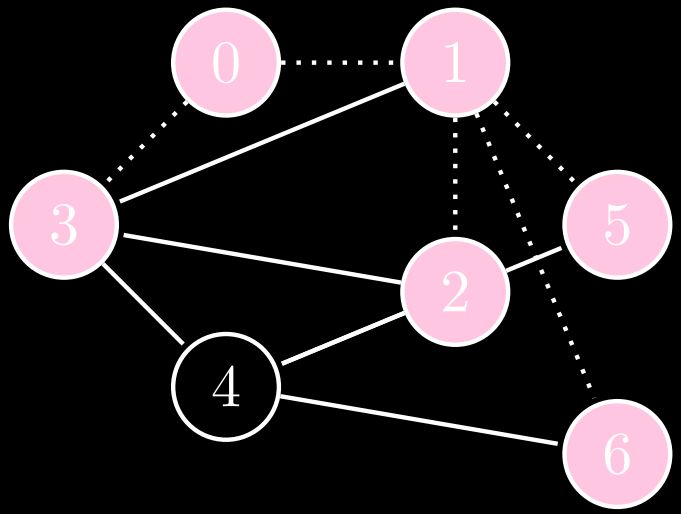
BFS example (1)



Queue	~~5~~	6	4				

Result	0	1	3	2	5		

BFS example (1)



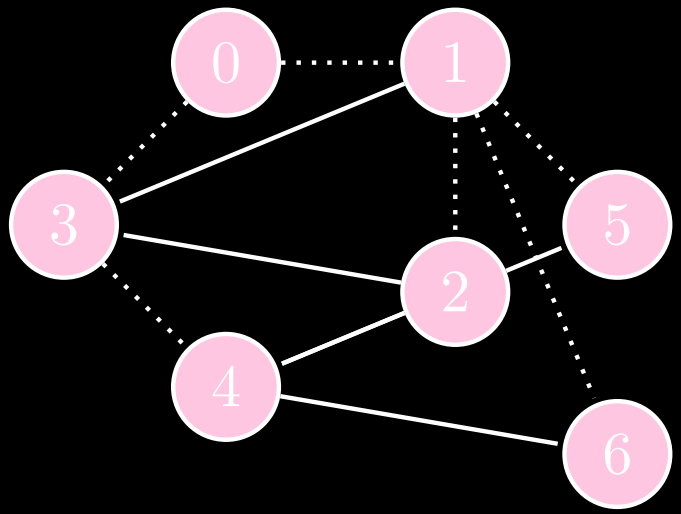
Queue

~~6~~	4					

Result

0	1	3	2	5	6	

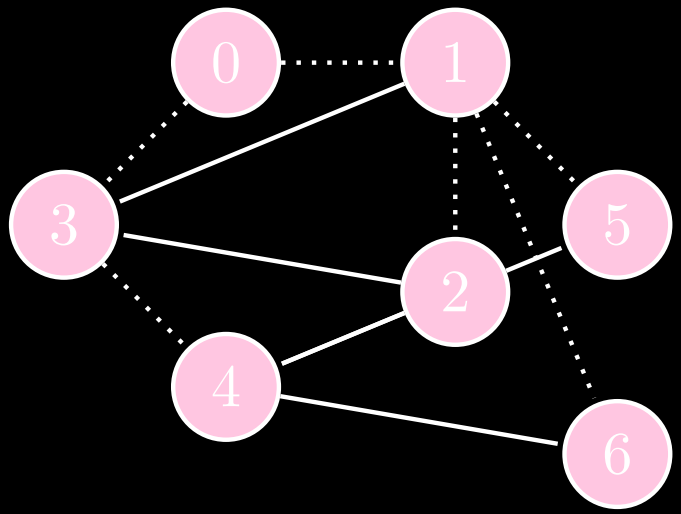
BFS example (1)



Queue	4						

Result	0	1	3	2	5	6	4

BFS example (1)



Queue

Result

0	1	3	2	5	6	4

Breadth First Search (BFS) Algorithm

BFS(G, u)

Input: Graph G = (V, E) directed or undirected, vertex u (element of) V

Output: BFS traversal order from node u

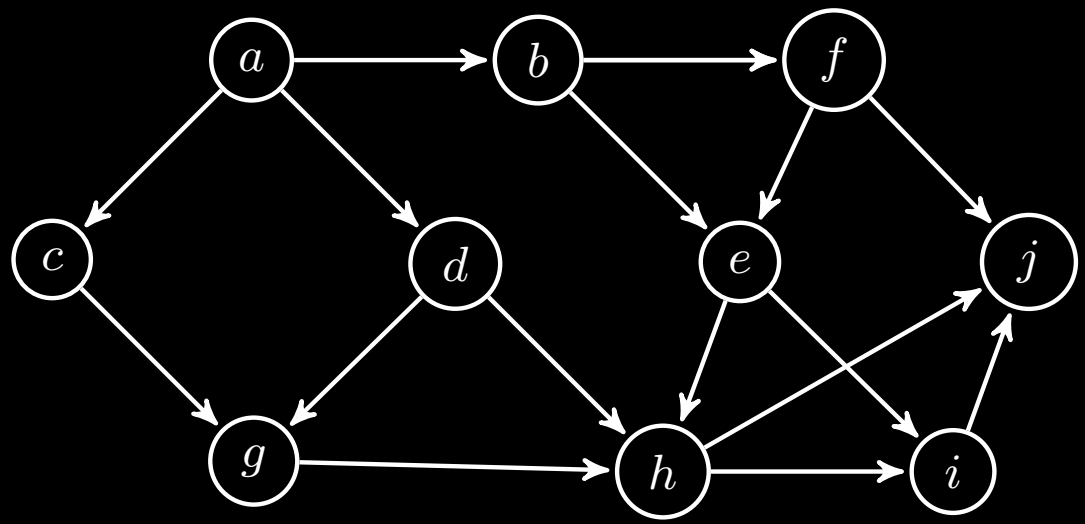
```
create a Queue Q
enqueue(Q, u)
while(Q is not empty)
  s = Dequeue(Q)
  if (visited of vertex s == false)
    result.add(s)
    visited of vertex s = true
  end if
  for all m (element of) neighbours of s
    if (visited of vertex m == false and m not in Q)
      enqueue(Q, m)
    end if
  end for
end while
return result
```

Complexity Analysis

Time Complexity - O(V + E)

Try out 2

- **Compute** the BFS traversal order in the Graph provided below, starting from vertex **a**. Show the Queue and Result array in your solution.



Next:

- **Graph Shortest Path Algorithms:**
  Dijkstras algorithm.

Reading Assignment

Sedgewick 4.1 and 4.2

Questions?

Please ask if there are any Questions
through Slack, Email, and/or during the virtual office hours!