

CS202 - Algorithm Analysis

Merge Sort

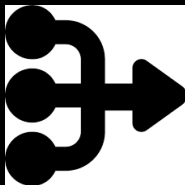
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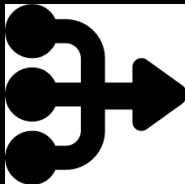
Merge Sort Algorithm



Strategy:

- **Divide:** if S has at least two elements, remove all the elements from S and put them into two sequences S_1 and S_2 , each containing about half of the elements of S . (i.e., S_1 contains the first floor $(n/2)$ elements and S_2 contains the remaining floor $(n/2)$ elements.
- **Conquer:** Sort sequences S_1 and S_2 using Merge Sort.
- **Combine:** Put back the elements into S by merging the sorted sequences S_1 and S_2 into one sorted sequence.

Merge Sort Algorithm



Characteristics:

- sort out of "place", i.e., does require an additional array
- uses divide and conquer principle
- worst case running time is $O(n \times \log(n))$

Merge Sort Algorithm

Merge Procedure (linear)

Algorithm - Merge(A, p, m, r)

Input: an n -element un-sorted array A of integer values, a lower bound p of the array A , and a pivot r in the array A .

Output: an n -element sorted array A of integer values.

$n_1 \leftarrow m - p$

$n_2 \leftarrow r - m$

Initialize Array L of size $n_1 + 1$

Initialize Array R of size $n_2 + 1$

for $i = 0$ to n_1 **do**

$L[i] \leftarrow A[p+i]$

end for

for $j = 0$ to n_2 **do**

$R[j] \leftarrow A[m+j]$

end for

$L[n_1 + 1] \leftarrow \infty$

$R[n_2 + 1] \leftarrow \infty$

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Merge Sort Algorithm

Merge Procedure (linear)

```
Initialize  $i, j \leftarrow 0$   
for  $k = p$  to  $r$  do  
    if  $L[i] \leq R[j]$  then  
         $A[k] \leftarrow L[i]$   
         $i \leftarrow i+1$   
    else  
         $A[k] \leftarrow R[j]$   
         $j \leftarrow j+1$   
    end if  
end for
```

Merge Sort Algorithm

MergeSort Procedure (logarithmic)

Algorithm - MergeSort(A, p, r)

Input: an n -element un-sorted array A of integer values, a lower bound p of the array A , and a pivot r in the array A .

Output: an n -element sorted array A of integer values.

if $p < r$ **then**

$m \leftarrow \text{Floor } (p + r)/2$

 MergeSort(A, p, m)

 MergeSort($A, m+1, r$)

 Merge(A, p, m, r)

end if

Merge Example

1	5	7	8	2	4	6	9
---	---	---	---	---	---	---	---

i

1	5	7	8	∞
---	---	---	---	----------

j

2	4	6	9	∞
---	---	---	---	----------

i

1	5	7	8	∞
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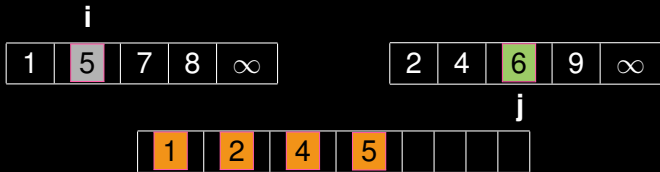
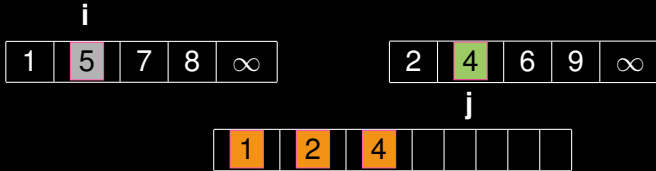
j

2	4	6	9	∞
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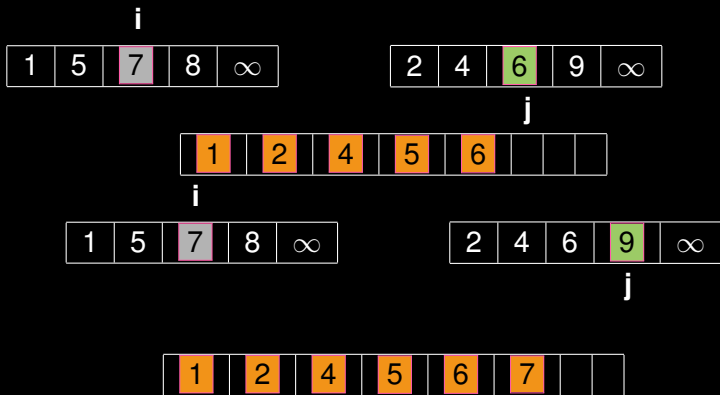
1							
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1	2						
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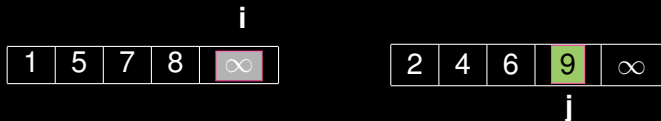
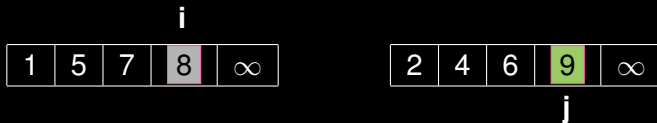
Merge Example



Merge Example



Merge Example



Questions?

Please ask if there are any Questions!

Sedgewick 2.2 Merge Sort

