

Activity__Explore probability distributions

January 7, 2024

1 Activity: Explore probability distributions

1.1 Introduction

The ability to determine which type of probability distribution best fits data, calculate z-score, and detect outliers are essential skills in data work. These capabilities enable data professionals to understand how their data is distributed and identify data points that need further examination.

In this activity, you are a member of an analytics team for the United States Environmental Protection Agency (EPA). The data includes information about more than 200 sites, identified by state, county, city, and local site names. One of your main goals is to determine which regions need support to make air quality improvements. Given that carbon monoxide is a major air pollutant, you will investigate data from the Air Quality Index (AQI) with respect to carbon monoxide.

1.2 Step 1: Imports

Import relevant libraries, packages, and modules. For this lab, you will need `numpy`, `pandas`, `matplotlib.pyplot`, `statsmodels.api`, and `scipy`.

```
[1]: # Import relevant libraries, packages, and modules.  
  
import numpy as np  
import pandas as pd  
import matplotlib.pyplot as plt  
import statsmodels.api as sm  
from scipy import stats
```

A subset of data was taken from the air quality data collected by the EPA, then transformed to suit the purposes of this lab. This subset is a .csv file named `modified_c4_epa_air_quality.csv`. As shown in this cell, the dataset has been automatically loaded in for you. You do not need to download the .csv file, or provide more code, in order to access the dataset and proceed with this lab. Please continue with this activity by completing the following instructions.

```
[2]: # RUN THIS CELL TO IMPORT YOUR DATA.  
  
### YOUR CODE HERE ###  
data = pd.read_csv("modified_c4_epa_air_quality.csv")
```

Hint 1

Refer to what you learned about loading data in Python.

Hint 2

There is a function in the `pandas` library that allows you to load data from a `.csv` file into a `DataFrame`.

Hint 3

Use the `read_csv()` function and pass in the name of the csv file as a string.

1.3 Step 2: Data exploration

Display the first 10 rows of the data to get a sense of how the data is structured.

```
[3]: # Display first 10 rows of the data.
```

```
data.head(10)
```

```
[3]:
```

	date_local	state_name	county_name	city_name	\
0	2018-01-01	Arizona	Maricopa	Buckeye	
1	2018-01-01	Ohio	Belmont	Shadyside	
2	2018-01-01	Wyoming	Teton	Not in a city	
3	2018-01-01	Pennsylvania	Philadelphia	Philadelphia	
4	2018-01-01	Iowa	Polk	Des Moines	
5	2018-01-01	Hawaii	Honolulu	Not in a city	
6	2018-01-01	Hawaii	Honolulu	Not in a city	
7	2018-01-01	Pennsylvania	Erie	Erie	
8	2018-01-01	Hawaii	Honolulu	Honolulu	
9	2018-01-01	Colorado	Larimer	Fort Collins	

	local_site_name	parameter_name	\
0	BUCKEYE	Carbon monoxide	
1	Shadyside	Carbon monoxide	
2	Yellowstone National Park - Old Faithful Snow ...	Carbon monoxide	
3	North East Waste (NEW)	Carbon monoxide	
4	CARPENTER	Carbon monoxide	
5	Kapolei	Carbon monoxide	
6	Kapolei	Carbon monoxide	
7	NaN	Carbon monoxide	
8	Honolulu	Carbon monoxide	
9	Fort Collins - CSU - S. Mason	Carbon monoxide	

	units_of_measure	aqi_log
0	Parts per million	2.079442
1	Parts per million	1.791759
2	Parts per million	1.098612

```
3 Parts per million 1.386294
4 Parts per million 1.386294
5 Parts per million 2.708050
6 Parts per million 1.098612
7 Parts per million 1.098612
8 Parts per million 1.791759
9 Parts per million 1.945910
```

Hint 1

Refer to what you learned about exploring datasets in Python.

Hint 2

There is a function in the **pandas** library that allows you to display a specific number of rows from the top of a DataFrame.

Hint 3

Use the **head()** function and pass in how many rows from the top of the DataFrame you want to display.

The **aqi_log** column represents AQI readings that were transformed logarithmically to suit the objectives of this lab. Taking a logarithm of the aqi to get a bell-shaped distribution is outside the scope of this course, but is helpful to see the normal distribution.

To better understand the quantity of data you are working with, display the number of rows and the number of columns.

```
[8]: # Display number of rows, number of columns.

data.shape
```

```
[8]: (260, 8)
```

Hint 1

Refer to what you learned about exploring datasets in Python.

Hint 2

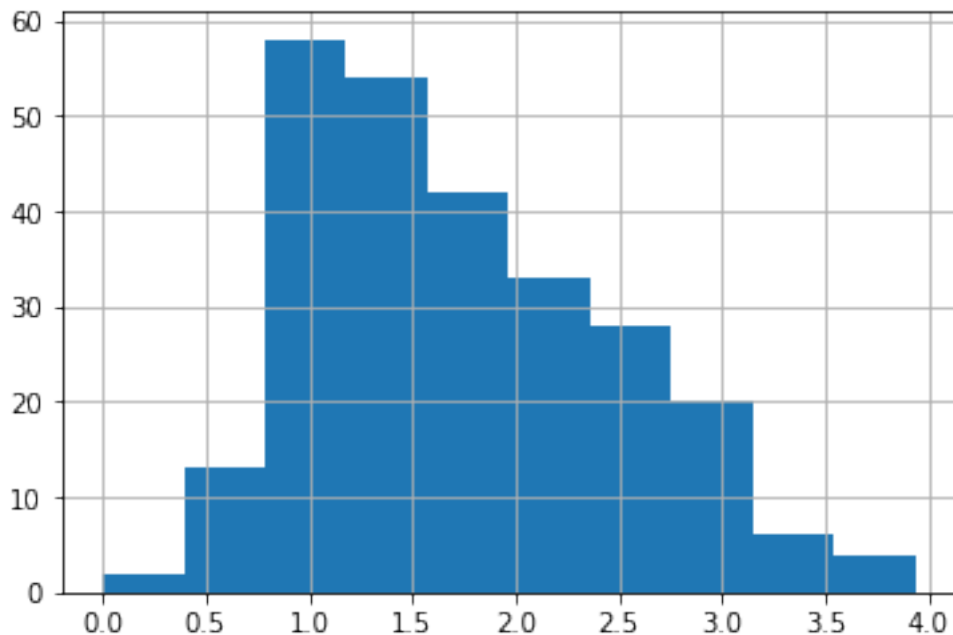
Every DataFrame in **pandas** has a property that gives you access to the number of rows and number of columns in that DataFrame.

Hint 3

Call the **shape** property of the DataFrame, which will display the number of rows and the number of columns as a tuple.

Now, you want to find out whether **aqi_log** fits a specific type of probability distribution. Create a histogram to visualize the distribution of **aqi_log**. Then, based on its shape, visually determine if it resembles a particular distribution.

```
[9]: # Create a histogram to visualize distribution of aqi_log.  
data["aqi_log"].hist();
```



Hint 1

Refer to the video about creating a histogram to visualize the distribution of a particular variable in the data.

Hint 2

There is a function in the `matplotlib` library that can be called to create a histogram.

Hint 3

The `hist()` function can be called directly on the `aqi_log` column from the data.

A semicolon can be used at the end as a quick way to make sure only the plot gets displayed (other text does not get displayed).

Question: What do you observe about the shape of the distribution from the histogram?

The distribution should be normal but has a right leaning skew.

1.4 Step 3: Statistical tests

Use the empirical rule to observe the data, then test and verify that it is normally distributed.

As you have learned, the empirical rule states that, for every normal distribution: - 68% of the data fall within 1 standard deviation of the mean - 95% of the data fall within 2 standard deviations of

the mean - 99.7% of the data fall within 3 standard deviations of the mean

First, define two variables to store the mean and standard deviation, respectively, for `aqi_log`. Creating these variables will help you easily access these measures as you continue with the calculations involved in applying the empirical rule.

```
[10]: # Define variable for aqi_log mean.  
  
mean_aqi_log = data["aqi_log"].mean()  
  
# Print out the mean.  
  
print(mean_aqi_log)
```

1.7669210929985577

```
[11]: # Define variable for aqi_log standard deviation.  
  
std_aqi_log = data["aqi_log"].std()  
  
# Print out the standard deviation.  
  
print(std_aqi_log)
```

0.7147155520223721

Hint 1

Refer to the lesson about calculating the mean and standard deviation for a particular variable in the data.

Hint 2

There are functions in the `numpy` library that can be called to calculate mean and standard deviation, respectively.

Hint 3

The `mean()` function can be called directly on the `aqi_log` column from the data to compute the mean.

The `std()` function can be called directly on the `aqi_log` column from the data to compute the standard deviation.

Now, check the first part of the empirical rule: whether 68% of the `aqi_log` data falls within 1 standard deviation of the mean.

To compute the actual percentage of the data that satisfies this criteria, define the lower limit (for example, 1 standard deviation below the mean) and the upper limit (for example, 1 standard deviation above the mean). This will enable you to create a range and confirm whether each value falls within it.

```
[12]: # Define variable for lower limit, 1 standard deviation below the mean.
```

```
lower_limit = mean_aqi_log - 1 * std_aqi_log
```

```
# Define variable for upper limit, 1 standard deviation above the mean.
```

```
upper_limit = mean_aqi_log + 1 * std_aqi_log
```

```
# Display lower_limit, upper_limit.
```

```
print(lower_limit, upper_limit)
```

```
1.0522055409761855 2.48163664502093
```

Hint 1

Refer to the video about using the empirical rule.

Hint 2

The lower limit here is $mean - 1 * std$.

The upper limit here is $mean + 1 * std$.

The `print` function can be called to display.

Hint 3

Use the variables that you defined for mean and standard deviation of `aqi_log`, ensuring the spelling is correct.

Call the `print` function and pass in the values one after the other, with a comma between them.

```
[13]: # Display the actual percentage of data that falls within 1 standard deviation
      ↪ of the mean.
```

```
((data["aqi_log"] >= lower_limit) & (data["aqi_log"] <= upper_limit)).mean() *
      ↪ 100
```

```
[13]: 76.15384615384615
```

Hint 1

Refer to the video about using the empirical rule.

Hint 2

The `>=` operator can be used to confirm whether one value is greater than or equal to another value.

The `<=` operator can be used to check whether one value is less than or equal to another value.

The `&` operator can be used to check if one condition and another condition is met.

Hint 3

The `mean()` function can be used to compute the proportion of the data that satisfies the specified conditions.

Multiplying that proportion by 100 can get you the percentage.

Now, consider the second part of the empirical rule: whether 95% of the `aqi_log` data falls within 2 standard deviations of the mean.

To compute the actual percentage of the data that satisfies this criteria, define the lower limit (for example, 2 standard deviations below the mean) and the upper limit (for example, 2 standard deviations above the mean). This will enable you to create a range and confirm whether each value falls within it.

```
[14]: # Define variable for lower limit, 2 standard deviations below the mean.
```

```
lower_limit = mean_aqi_log - 2 * std_aqi_log
```

```
# Define variable for upper limit, 2 standard deviations below the mean.
```

```
upper_limit = mean_aqi_log + 2 * std_aqi_log
```

```
# Display lower_limit, upper_limit.
```

```
print(lower_limit, upper_limit)
```

```
0.33748998895381344 3.1963521970433018
```

Hint 1

Refer to the video about using the empirical rule.

Hint 2

The lower limit here is $mean - 2 * std$.

The upper limit here is $mean + 2 * std$.

The `print` function can be called to display.

Hint 3

Use the variables that you defined for mean and standard deviation of `aqi_log`, ensuring the spelling is correct.

Call the `print` function and pass in the values one after the other, with a comma between them.

```
[16]: # Display the actual percentage of data that falls within 2 standard deviations  
      ↳ of the mean.
```

```
((data["aqi_log"] >= lower_limit) & (data["aqi_log"] <= upper_limit)).mean() * 100
```

[16]: 95.76923076923077

Hint 1

Refer to the video section about using the empirical rule.

Hint 2

The `>=` operator can be used to confirm whether one value is greater than or equal to another value.

The `<=` operator can be used to check whether one value is less than or equal to another value.

The `&` operator can be used to check if one condition and another condition is met.

Hint 3

The `mean()` function can be used to compute the proportion of the data that satisfies the specified conditions.

Multiplying that proportion by 100 can get you the percentage.

Now, consider the third part of the empirical rule: whether 99.7% of the `aqi_log` data falls within 3 standard deviations of the mean.

To compute the actual percentage of the data that satisfies this criteria, define the lower limit (for example, 3 standard deviations below the mean) and the upper limit (for example, 3 standard deviations above the mean). This will enable you to create a range and confirm whether each value falls within it.

```
[17]: # Define variable for lower limit, 3 standard deviations below the mean.
```

```
lower_limit = mean_aqi_log - 3 * std_aqi_log
```

```
# Define variable for upper limit, 3 standard deviations above the mean.
```

```
upper_limit = mean_aqi_log + 3 * std_aqi_log
```

```
# Display lower_limit, upper_limit.
```

```
print(lower_limit, upper_limit)
```

-0.3772255630685586 3.911067749065674

Hint 1

Refer to the video about using the empirical rule.

Hint 2

The lower limit here is $mean - 3 * std$.

The upper limit here is $mean + 3 * std$.

The `print` function can be called to display.

Hint 3

Use the variables that you defined for mean and standard deviation of `aqi_log`, ensuring the spelling is correct.

Call the `print` function and pass in the values one after the other, with a comma between them.

```
[18]: # Display the actual percentage of data that falls within 3 standard deviations
      ↪ of the mean.

      ((data["aqi_log"] >= lower_limit) & (data["aqi_log"] <= upper_limit)).mean() * 100
      ↪
```

```
[18]: 99.61538461538461
```

Hint 1

Refer to the video about using the empirical rule.

Hint 2

The `>=` operator can be used to confirm whether one value is greater than or equal to another value.

The `<=` operator can be used to check whether one value is less than or equal to another value.

The `&` operator can be used to check if one condition and another condition is met.

Hint 3

The `mean()` function can be used to compute the proportion of the data that satisfies the specified conditions.

Multiplying that proportion by 100 can get you the percentage.

1.5 Step 4: Results and evaluation

Question: What results did you attain by applying the empirical rule?

76.15% falls within 1 standard deviation 95.77% falls within 2 standard deviation 99.62% falls within 3 standard deviation

Question: How would you use z-score to find outliers?

Z-scores help identify values outside of 3 standard deviations and can uncover outliers otherwise unseen.

Compute the z-score for every `aqi_log` value. Then, add a column named `z_score` in the data to store those results.

```
[27]: # Compute the z-score for every aqi_log value, and add a column named z_score
      ↪ in the data to store those results.
```

```
data["z_score"] = stats.zscore(data["aqi_log"])
```

```
# Display the first 5 rows to ensure that the new column was added.
```

```
data.head()
```

```
[27]:
```

	date_local	state_name	county_name	city_name \
0	2018-01-01	Arizona	Maricopa	Buckeye
1	2018-01-01	Ohio	Belmont	Shadyside
2	2018-01-01	Wyoming	Teton	Not in a city
3	2018-01-01	Pennsylvania	Philadelphia	Philadelphia
4	2018-01-01	Iowa	Polk	Des Moines

	local_site_name	parameter_name \
0	BUCKEYE	Carbon monoxide
1	Shadyside	Carbon monoxide
2	Yellowstone National Park - Old Faithful Snow ...	Carbon monoxide
3	North East Waste (NEW)	Carbon monoxide
4	CARPENTER	Carbon monoxide

	units_of_measure	aqi_log	z_score
0	Parts per million	2.079442	0.438109
1	Parts per million	1.791759	0.034820
2	Parts per million	1.098612	-0.936873
3	Parts per million	1.386294	-0.533584
4	Parts per million	1.386294	-0.533584

Hint 1

Refer to the video about calculating z-score.

Hint 2

There is a function in the **stats** module of the **scipy** library that you can call to calculate z-score.

Hint 3

Call the **zscore()** function and pass in the **aqi** column from the data.

Identify the parts of the data where **aqi_log** is above or below 3 standard deviations of the mean.

```
[29]: # Display data where `aqi_log` is above or below 3 standard deviations of the
      ↪ mean
```

```
data[(data["z_score"] > 3) | (data["z_score"] < -3)]
```

```
[29]:      date_local state_name county_name city_name local_site_name \
244  2018-01-01      Arizona      Maricopa      Phoenix      WEST PHOENIX

      parameter_name  units_of_measure  aqi_log  z_score
244  Carbon monoxide  Parts per million  3.931826  3.034886
```

Hint 1

Refer to the video about outlier detection.

Hint 2

The > operator can be used to evaluate whether one value is greater than another value.

The < operator can be used to evaluate whether one value is less than another value.

The | operator can be used to evaluate whether one condition or another condition is met.

Hint 3

To index the DataFrame, place a pair of parentheses around the evaluation of the two conditions and pass that into a pair of square brackets. This will allow you to get all rows in the data where the specified criteria is met.

Make sure the spelling of the column matches the name you specified when creating that column.

Question: What do you observe about potential outliers based on the calculations?

The outlier has a z score of 3 which is very far from the standard deviations of the normal mean. This shows Phoenix has the worst air quality out of the data set

Question: Why is outlier detection an important part of this project?

Detecting outliers is important because these outliers can be a small portion of the dataset but hold valuable information that could be useful to our analysis.

1.6 Considerations

What are some key takeaways that you learned during this lab?

Using the process of standard deviation we can find so much useful information through just a bit of code. Even using this code we can have small visualizations to help further the understanding.

What summary would you provide to stakeholders? Consider the distribution of the data and which sites would benefit from additional research.

The distribution of the aqi is normal, the one area you'll need to focus more on would be west Phoenix as they have the worst aqi out the entire sample.

Reference

US EPA, OAR. 2014, July 8. [Air Data: Air Quality Data Collected at Outdoor Monitors Across the US](#).

Congratulations! You've completed this lab. However, you may not notice a green check mark next to this item on Coursera's platform. Please continue your progress regardless of the check mark. Just click on the "save" icon at the top of this notebook to ensure your work has been logged.