

Analysis Big O

1. `for (int i = 0; i < n; i++)` $O(n)$
 $O(n)$

2. `for (int i = 0; i < n; i++) {` $O(n)$
`for (int j = 0; j < m; j++) {` $O(m)$
 $O(n) \times O(m)$
 $O(n \times m)$

3. `for (int i = 0; i < n; i++) {` $O(n)$
`for (int j = 0; j < n; j++) {` $O(n)$
 $O(n) \times O(n) = O(n^2)$

4. `int index = -1;` $O(1)$
`for (int i = 0; i < n; i++) {` $O(n)$
`if (array[i] == target) {` $O(1)$
`index = i;` $O(1)$
`break;`
 $O(1) + O(n) + O(1) + O(1)$
 $O(n)$

5. $\text{int left} = 0, \text{right} = n - 1, \text{index} = -1; O(n)$
 $\text{while} (\text{left} \leq \text{right}) \{ O(1)$
 $\text{int mid} = \text{left} + (\text{right} - \text{left}) / 2; O(\log n)$
 $\text{if} (\text{array}[\text{mid}] \leq \text{target}) \{ O(1)$
 $\text{index} = \text{mid}; O(1)$
 $\text{Break}; O(1)$
 $\} \text{ else if} (\text{array}[\text{mid}] < \text{target}) \{ O(1)$
 $\text{left} = \text{mid} + 1; O(1)$
 $\} \text{ else } \{ O(1)$
 $\text{right} = \text{mid} - 1; O(1)$
 $\} O(n) + O(1) + O(\log n) + O(1) + O(1) + O(1) + O(1)$
 $O(\log n)$

6. $\text{int row} = 0, \text{col} = \text{matrix}[0].\text{length} - 1, \text{indexRow} = -1$
 $\text{indexCol} = -1; O(1)$
 $\text{while} (\text{row} < \text{matrix}.\text{length} \ \&\& \ \text{col} \geq 0) \{ O(1)$
 $\text{if} (\text{matrix}[\text{row}][\text{col}] == \text{target}) \{ O(n+m)$
 $\text{indexRow} = \text{row}; O(n)$
 $\text{indexCol} = \text{col}; O(m)$
 $\text{Break}; O(1)$
 $\} \text{ else if} (\text{matrix}[\text{row}][\text{col}] < \text{target}) \{ O(n+m)$
 $\text{row}++; O(1)$
 $\} \text{ else } \{ O(1)$
 $\text{col}--; O(1)$
 $\} O(1) + O(m+n) + O(n) + O(m) + O(1) + O(n+m) + O(1)$
 $O(m+n)$

7. `void bubbleSort (int[] array) {` $O(1)$
`int n = array.length;` $O(1)$
`for (int i = 0; i < n - 1; i++) {` $O(n)$
`for (int j = 0; j < n - 1 - i; j++) {` $O(n)$
`if (array[j] > array[j + 1]) {` $O(1)$
`int temp = array[j];` $O(1)$
`array[j] = array[j + 1];` $O(1)$
`array[j + 1] = temp;` $O(1)$
`}`
`}`
 ~~$O(1) + O(1) + O(n \times n) + O(1) + O(1) + O(1) + O(1)$~~
 $O(n^2)$

8. `void selectionSort (int[] array) {` $O(1)$
`int n = array.length;` $O(1)$
`for (int i = 0; i < n - 1; i++) {` $O(n)$
`int minIndex = i;` $O(1)$
`for (int j = i + 1; j < n; j++) {` $O(n)$
`if (array[j] < array[minIndex]) {` $O(1)$
`minIndex = j;` $O(1)$
`}`
`}`

`int temp = array[i];` $O(1)$
`array[i] = array[minIndex];` $O(1)$
`array[minIndex] = temp;` $O(1)$

~~$O(1) + O(1) + O(n \times n) + O(1) + O(1)$~~
 $O(n^2)$


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9. Void insertionSort (int[] array) {
    int n = array.length;  $O(1)$ 
    for (int i = 1; i < n; i++) {  $O(n)$ 
        int key = array[i];  $O(1)$ 
        int j = i - 1;  $O(1)$ 
        while (j >= 0 && array[j] > key) {  $O(n)$ 
            array[j+1] = array[j];  $O(1)$ 
            j--;  $O(1)$ 
        }
        array[j+1] = key;  $O(1)$ 
    }
}
 $O(1) + O(n) + O(1) + O(1) + O(n) + O(1) + O(1)$ 
 $O(n^2)$ 

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10. Void mergeSort (int[] array, int left, int right) {  $O(1)$ 
    if (left < right) {  $O(1)$ 
        int mid = left + (right - left) / 2;  $O(\log n)$ 
        mergeSort (array, left, mid);  $O(1)$ 
        mergeSort (array, mid+1, right);  $O(1)$ 
        merge (array, left, mid, right);  $O(1)$ 
    }
}

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$O(1) + O(1) + O(\log n) + O(1) + O(1) + O(1)$
 $O(\log n)$

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11. void quickSort (int[] array, int low, int high) {  $O(1)$ 
    if (low < high) {  $O(1)$ 
        int pivotIndex = partition (array, low, high);  $O(1)$ 
        quickSort (array, low, pivotIndex - 1);  $O(n) - O(n \log n)$ 
        quickSort (array, pivotIndex + 1, high);  $O(n) - O(n \log n)$ 
    }
}  $O(1) + O(1) + O(1) + O(n \log n) + O(n \log n)$ 
 $O(n^2)$ 

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12. int fibonacci (int n) {  $O(1)$ 
    if (n <= 1) {  $O(1)$ 
        return n;  $O(1)$ 
    }

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    int[] dp = new int [n+1];  $O(1)$ 
    dp[0] = 0;  $O(1)$ 
    dp[1] = 1;  $O(1)$ 
    for (int i = 2; i <= n; i++) {  $O(n)$ 
        dp[i] = dp[i-1] + dp[i-2];  $O(1)$ 
    }
    return dp[n];  $O(1)$ 

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}  $O(1) + O(1) + O(1) + O(1) + O(n) + O(1) + O(1)$ 
 $O(n)$ 

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13. Void Linear Search (int[] array, int target) { $O(1)$
 for (int i = 0; i < array.length; i++) { $O(n)$
 if (array[i] == target) { $O(1)$
 // Encontrado
 return i;
 }
 // no Encontrado
 }
 ~~$O(1) + O(n) + O(1) = O(n)$~~

14. int binarySearch (int[] sortedArray, int target) { $O(1)$
 int left = 0, right = sortedArray.length - 1; $O(n)$
 while (left <= right) { $O(1)$
 int mid = left + (right - left) / 2; $O(\log n)$
 if (sortedArray[mid] == target) { $O(1)$
 return mid; // Indice del elemento encontrado $O(1)$
 } else if (sortedArray[mid] < target) { $O(1)$
 left = mid + 1; $O(1)$
 } else {
 right = mid - 1; $O(1)$
 }
 return -1; // Elemento no encontrado $O(1)$

~~$O(1) + O(n) + O(1) + O(\log n) + O(1) + O(1) + O(1) + O(1)$~~
 $O(\log n)$

15. `int factorial (int n) {` $O(1)$

`if (n == 0 || n == 1) {` $O(1)$

`return 1;` $O(1)$

`}`

`return n * factorial (n - 1);` $O(n-1)$

`}`

~~$O(1) + O(1) + O(1) + O(n)$~~

$O(n)$

$$\sqrt{3x^3}$$

1.

$$\sqrt[3]{(x^4 + 11x) - \frac{1}{2}} (3x^3)$$

$$u = 3x^4 + 11$$