**Boolean Gene Implication Network Construction and Visualization from Single-cell RNA-seq Data**

**Specific Aims**

Gene expression based network construction has long been a goal of transcriptomic endeavors. The realization of which, promises to unravel the genetic landscape of many biological contexts.  Many publications in the past have contributed to this particular effort [1, 2, 3, 4, 5, 6, 7]. But, one unifying problem that all these studies share is their reliance on tissue sample transcriptomic data—a drawback due to the mixture of different types of cells as well as heterogeneity among cells of the same type. Such endeavors are therefore not sufficient to answer questions targeting the molecular and cellular levels of biology. However, single-cell resolution has recently risen in popularity in the form of single-cell RNA sequencing (RNA-Seq) technology [8]. Proper utilization of this nascent technology may help overcome the interpretation issues of past works and identify functional relationships between genes that would be otherwise obscured by averaging effects of tissue sample transcriptomics.

Functional relationships between genes can also be obscured by drastic differences in the proportions of represented cell types or states within a dataset. Intuition for this comes from the consideration of rare cell types, which—although small in number—may harbor important, discerning information regarding the shape of a functional relationship between two genes. A number of works in the past have implemented density-dependent normalization techniques to counter this type of disproportional representation [9, 10, 11].

Finally, the utilization of single-cell RNA-Seq methodologies, although promising in theory, suffer in practice from characteristically high technical variation [reference needed]. This fact restricts the application of single-cell transcriptomic technologies to many scientific endeavors—gene expression based network construction among their ranks. We hypothesize that the estimation and subsampling of conditional probability pair-wise gene data can result in novel functional relationship detection in gene expression based network construction when compared to the same analysis considering only the pair-wise joint distributions of genes. Furthermore, we hypothesize that attenuate the effects of technical and biological variation with our proposed methodology.

**Aim 1. Develop a workflow to construct directed Boolean gene implication networks conducive to intuitive analysis of gene expression at the cellular level using single-cell RNA-seq data.**

**Impact:** Networks constructed by our novel workflow will be capable of capturing functional relationships implication Boolean implications resulting from the consideration of rare cell types/states that former methodologies would not be able to capture. Furthermore, our networks promise to be readily interpretable at the cellular and molecular genetics level.

**Aim 2. Visualize the constructed directed Boolean gene implication network in an intuitive hypothesis generation tool allowing biomedical researchers to develop new hypothesis on gene relationships.**

**Impact:** This tool promises to make our results even more user-friendly to hypothesis generation over previous works by combining the interpretability of our results in aim 1 with the navigational and organizational tools of an interactive visualization tool.

**Research Strategy**

***Significance:*** Gene dependence and correlation analyses have long been used to investigate the biological processes underpinning samples of interest. Recent work has been done regarding the susceptibility of traditional transcriptomic technologies to Simpson’s Paradox—the confounding of a mixture of signals that suggests a trend With the rise of single-cell RNAseq technologies, transcriptomics can now play a role in answering questions regarding tissue heterogeneity [13, 14, 15, 9, 16, 17]. Our proposed methodology promises a glimpse of the ‘rules of the game’ within this heterogeneity for a given progression across a dynamic cellular biological process. Pervious works suffer, in part, from poor interpretability given the unknown cellular composition of the input datasets. A single-celled perspective in theory does not suffer from the averaging effects of bulk sample transcriptomics data and therefore derived implications in this work will not suffer from the same interpretation issues. Furthermore*,*aim 2, provides an exciting first look into the dynamics of Boolean implication of a given dataset and biological context.

***Innovation:*** To our knowledge no work has attempted to infer Boolean implication networks from single-cell RNASeq data. Neither have other publications attempted to combine the works of Sahoo’s Boolean implication inference methodologies [2, 3] with the DREMI dependency metric [10]. We believe that the combination of these techniques will be able to detect potential bivariate gene implications that would otherwise be masked due to the rarity of certain cellular states in a given dataset. Finally, no work has proposed to look at the dynamics of Boolean gene implication networks in any biological context to our knowledge.

**Approach:**

**Aim 1. To construct directed Boolean gene implication networks conducive to intuitive analysis of gene expression at the cellular level.**

Our first goal is to develop a novel methodology to infer Boolean implication gene networks from single-cell RNASeq data. The DREMI metric [Eq. 4] is of particular interest to this investigation because it has been shown to expose functional relationships between variables whose joint probability is dominated by a seemingly independent signature. DREMI is an application of mutual information [18] that measures the decrease in uncertainty of one variable given the value of another. To grasp the metric fully, consider the following definitions:

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| Let and where |  |
| Let and |  |
| Let and |  |

Namely,andare vectors of random variables whileandare vectors of a sample’s X and Y components from the joint distribution .

Imagine that there may exist cell populations that are dominated by a particular cellular state or subtype (we’ll just say ‘state’ here for simplicity). Values in and may be dominated by a specific sub-range of the spans of and. If values in the dominant cell state are centralized around some (x, y) value, then many metrics may conclude that no relationship exists between genes X and Y. However, rare signatures for X and Y may offer discerning information regarding the functional dependence of genes X and Y. DREMI addresses this issue by subsampling according to an estimation of rather than . We’ll refer to this subsampling as along with the following definitions:

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DREMI deconvolution is achieved by estimating via a non-parametric diffusion kernel [Eq. 1] applied over bins of X values. Data is resampled according to this estimated conditional probability. And finally, mutual information [Eq. 2] is calculated for the down-sampled data. They show that this is equivalent to mutual information [Eq. 3] where every sample is weighted by [Eq. 4].

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The DREMI metric gives a reasonable measure for the strength of functional relationships between gene X and gene Y. The next step is to extract inference wherever possible. In other words, we want to turn our undirected network into a directed one. A number of previous works attempt to infer directionality in transcriptome data (Sahoo 2008). Previous work from our lab have successfully utilized the approach used by Sahoo et al. for the ‘fuzzification’ and directionality inference of relationships extracted from microarray data [1]. We intend to use the same basic methodology applied to the down-sampled technique described in Pe’er et al.

For a scatterplot of , we start by discretizing the resampled by labeling a given gene expression value as either ‘high’ or ‘low’. This is done by first ordering all observed values of from smallest to largest and fitting a step function to those ordered values using StepMiner [3]—an algorithm presented in Sahoo et al. These step functions aim to minimize the mean squared error (MSE) using an adaptive regression process. Next, the average of the high and low steps in a fitted step function serve to be the decision threshold between fuzzy ‘high’ and ‘low’ labels for gene X.

To discretize , we may be able to take advantage of the P(Y|X) normalization effects that occur in the subsampling proposed by Pe’er et al. In our lab’s original work, step function fitting was chosen, in part, because the minimization of MSE can still find a suitable boundary decision line in the presence of outliers. However, Pe’er’s conditional probability normalization resampling methodology can serve to remove outliers. We propose that a simpler boundary decision can be found:

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After discretization, we continue Sahoo’s workflow to test for sparsity amongst the quadrants formed by the decision boundaries for X and Y. This is done by testing sample counts in a quadrant against the null hypothesis of uniformity in the distribution of samples. For instance, consider the test for the quadrant corresponding to low values of both X and Y. Letting , , , and be the number of samples categorized with X and Y labels ‘low’ and ‘low’, ‘low’ and ‘high, ‘high and ‘low’, and ‘high and ‘high respectively. Sparsity of the low-low quadrant is determined as follows:

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|  |  | (8) |

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|  |  | (9) |

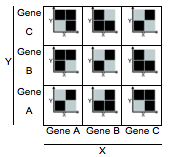
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| , for thresholds and | () |

Analogous calculations are performed to determine , , and . Now let, , , , and be Boolean variables that are true when, for a particular biological context, gene X or Y is highly expressed or not highly expresses (note that and ). Depending on the sparsity profile of the quadrants we propose that the following implications can be drawn.

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|  |  |  |  | Class | Conclusion |
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| 1 | 0 | 1 | 0 | Macintosh HD:Users:Brian:Documents:Research:CandidacyProposal:Figures:1010.png | No implication |
| 0 | 1 | 0 | 1 | Macintosh HD:Users:Brian:Documents:Research:CandidacyProposal:Figures:0101.png | No implication |
| 1 | 0 | 0 | 1 | Macintosh HD:Users:Brian:Documents:Research:CandidacyProposal:Figures:1001.png |  |
| 0 | 1 | 1 | 0 | Macintosh HD:Users:Brian:Documents:Research:CandidacyProposal:Figures:0110.png |  |

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|  |  |  |  | Class | Conclusion |
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The set of resulting, gene pair-wise Boolean implications constitute a Boolean implication network between ‘fuzzified’ expression values in a given biological context. An example of one such network containing 3 genes—A,B, and C—is illustrated in Figure 1.



**Figure 1|** Example implications (Left), and implication network (Right) for a set of three genes A, B, and C.

Note that the conditional probability subsampling methodology proposed does not guarantee symmetric implications about X and Y. Non-symmetric patterns may be of interest biologically—potentially indicating the presence of a rare expression pattern.

**Outcomes, Pitfalls, and Alternative Plans:** The primary output of aim 1 is a Boolean implication network between genes. Major foreseeable obstacles for this step of the proposal revolve around the known noisiness of single-cell RNA-seq data. The prevalence of dropout events (missing values) has plagued the analysis of this technology. Applying appropriate normalization techniques and accounting for technical bias with spike-in controlled datasets, however, will greatly increase the signal to noise ratio of our data. Furthermore, massively parallelized single-cell RNA-seq data boasts not only increased sample sizes but also reduced technical bias owing to the utilization of unique molecular identifier (UMI) barcoding. Dropout events can be countered with low rank matrix estimation diffusion techniques or mixture model estimation.

**Aim 2. Aside from gene expression profiles, functional relationships can also change between different cellular states and cellular subtypes. The challenge is to broaden our Boolean implication network to analyze the dynamics of a biological process.**

Next, we attempt to decouple functional relationships between gene X and gene Y from conditional dependence upon a factor that Trapnell et al. refer to as ‘pseudotime’—“a quantitative measure of progress through a biological process” [12]. The interplay of genes is known to change as a cell progresses through dynamic biological processes such as differentiation, cell cycle, or oncogenic transformation. Our approach may not be able to identify strong relationships between X and Y when considering cells from multiple cellular states if the true, underlying relationships between X and Y in those states differ. For example, consider the example illustrated by Figure 2. Clusters and , when considered together, yield no implication. However, partitioning of the samples gives rise to separate implications. Moreover, if these clusters represent cellular states along a biological progression, we may gain valuable information by analyzing the difference in the class of implications yielded by each partition.

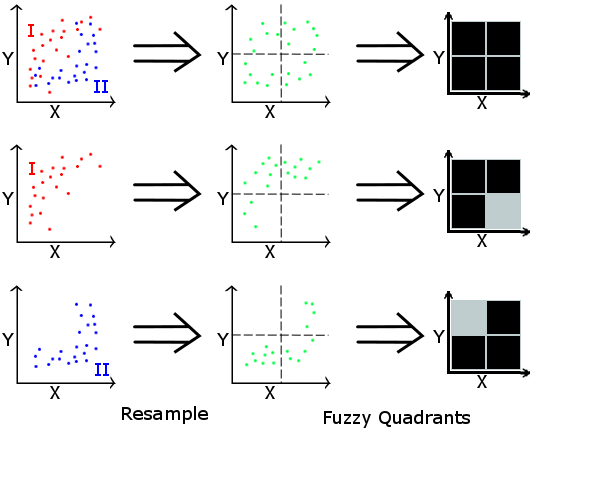


Figure 2| Somewhat contrived example of the convolution of signal that may exist in a dataset due to the combination of biologically differentiable cellular states.

To overcome this convolution of signals through pseudotime, we combine sample clustering with the temporal ordering output of an algorithm presented in Trapnell et al.—Monocle [12]. We plan to cluster samples in 2-dimensional independent component analysis (ICA) [19] space using hierarchical clustering. Let sets define these output clusters such that . And then check for agreement between our clustering and Monocle’s output as described below.

First, an overview of the algorithm in question: Monocle orders single-cells along an inferred smooth transition function in Euclidean gene expression space. Here represent the true set of expression values between states, and captures biological and technical noise. Monocle estimates by adapting a methodology that was first introduced by Magwene et al [20]. First, independent component analysis (ICA) [19] is performed on the data, and fitted with a minimum spanning tree (MST) in 2-dimensional independent component space. The diameter of the MST is taken as an estimate of . The algorithm goes on to find potential orderings of samples in the data relative to using a PQ tree. A PQ tree defines a family of orderings of discrete elements in a set; it is a tree with two types of nodes—a Q node whose children are ordered (although reversible), and a P type node where children are permutable. So, a PQ tree is created with a single Q node denoted QMain. All vertices along the diameter of the MST with degree greater than 2 are deemed ‘indecisive’, and ‘decisive’ otherwise. The ‘indecisive backbone’ of the diameter is located—the longest sequence of vertices for which the endpoints are indecisive. All decisive vertices along the indecisive backbone are added to QMain in an ordered fashion. Then for any indecisive vertex along the indecisive backbone, a P node is appended to the tree and the indecisive vertex is added as a child of that P node. This same approach is then applied recursively to each branch of the indecisive vertex. Possible orderings of samples in pseudotime are given by those orders extractable from the final PQ tree.

Using the ordering proposed by the PQ tree with the shortest total distance in component space to define our samples’ ordering in pseudotime, we can define an order between sample clusters. We’ll let be the ordered set of indices output by Monocle that orders our samples in pseudotime. Clusters can then be ordered by We will say that a given clustering agrees with the MST output by Monocle if the variance of per cluster is sufficiently small. We purposely supply this crude definition of ‘agree’ because clustering can be a highly customizable process by method selection and parameterization therein. Furthermore, we believe that the clustering achieved by hierarchical clustering and the ordering of individual samples by Monocle will largely agree because, if two samples are assigned to the same cluster, they are relatively close to each other and Monocle will therefore likely assign indices that are relatively close to each other as well.

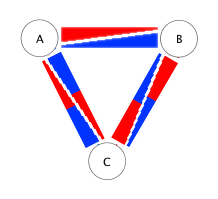
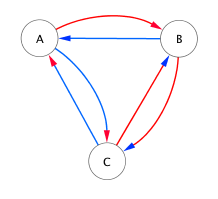
At this point, we will assume that constitute different cellular states separated by different progressions through pseudotime. By constructing Boolean implication networks by the approach outlined for aim 1 for each individual cluster, we are, in a sense, looking at relational dependencies between genes at different slices of pseudotime. More interestingly, maybe, are the Boolean implication networks that result from considering samples that belong to pairs of adjacent clusters, where adjacency is defined according to and Monocle’s MST. Effectively we can construct the rules of genetic interplay for both major cellular states in a dynamic biological process as well as for the transitions between those states.

**Outcomes, Pitfalls, and Alternative Plans:** The primary output of aim 2 is a series of Boolean implication networks that represented of clustered and pairs of clustered samples. Secondary output includes the pseudotemporal ordering of clusters and the differentiation tree of cell states hypothesized by Monocle. Do to the partitioning required to constitute different states in pseudotime, sample-size will most likely be a limiting factor for success. Publicly accessible GEO dataset GSE65525 provides ~3000 UMI-barcoded, differentiating, embryonic mouse stem cells RNA-seq samples. This extreme number of samples will not only provide sufficient samples that can be separated by biological differentiation, but UMI barcoding can also prove to reduce noise.

**Aim 3. Visualize for hypothesis generation tool while providing an array of organizational and information tools to aid investigators’ navigation.**

We will build an interactive visualization that will allow investigators to navigate the networks constructed by the approaches outlined in aim 1—complete with appropriate organizational and informational tools that can help the user with gene regulation oriented hypothesis generation.

First we wish to develop a concise visual encoding capable of conveying all classes of Boolean implication between gene pairs possible as output of aim 1 of this proposal. A traditional Boolean implication network visualization, as seen in Figure 1, requires nodes (‘high’ expression and ‘low’ expression labels per gene). Such a separation can complicate hypothesis generation. For this reason, we strive for a visualization consisting of a one-to-one mapping between genes and nodes. However, because traditional Boolean implication network nodes capture the state of Boolean variables, the proposed consolidation requires a translation of this information into another encoding. We propose capturing the state of a given variable in an implication in the directed edge between nodes as seen in the center panel of Figure 3. Finally we propose to further consolidate the information contained in this graph by consolidating implication classes between two genes using edge glyphs as seen in the right panel of Figure 3.



**Figure 3|** Example Boolean implication network from Figure 1 (Left). A node-consolidated visualization of the same example (Middle). Colors denote high (red) and low (blue) labels of genes in an implication relationship. Colors of arrow stems map to the upstream gene in an implication while arrowheads map to the downstream gene in an implication. And our proposed glyph encoding of edges (Right) which captures the same information.

Additional visual encodings:

* Edge thickness or transparency will be proportional to DREMI .
* Node color will denote user-specified gene groupings.
* Pairs of directed Boolean implication classes will be encoded according to the following chart:

Our application will be provided as an R package developed using the web interface framework Shiny [21]. Using a web interface framework like Shiny that can also be run locally provides the flexibility of future extension into a web service without sacrificing benefits of local applications (latency, data security, etc…). Scatterplots and heatmaps will be realized using the ggplots [22] package and network data structures, manipulations (such as layout), and visualizations will be handled using the igraphs package [23].

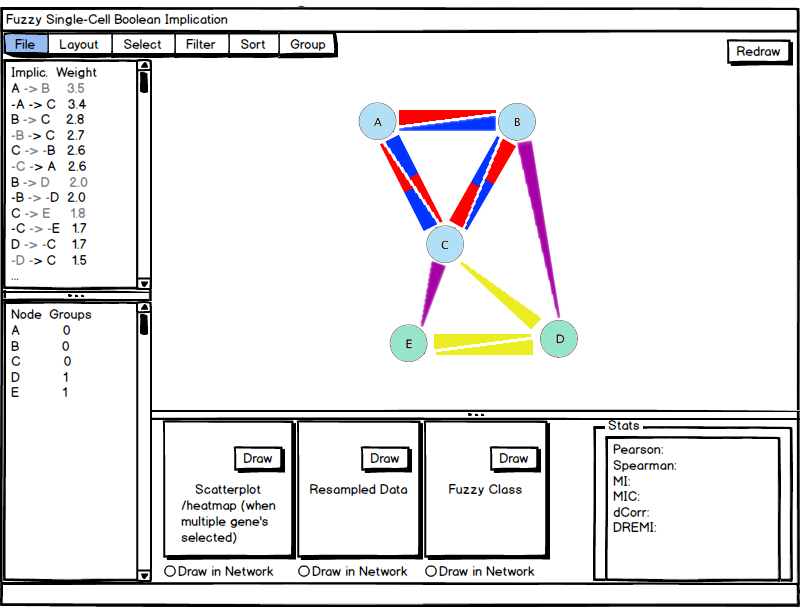
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Figure 4| Mockup of proposed interactive visualization application.

Proposed features:

* Import/export of data matrices.
* Boolean implication network with aforementioned visual encodings.
  + Click and drag interaction support.
  + Automatic node layout algorithm support.
* Node organization tools: criteria/manual selection, filter, sort, and grouping.
* Edge organization tools: criteria/manual selection, filter, and sorting.
* Sample organization tools: criteria/manual filtering.
* Node information tools: histogram
* Node group information tools:
  + Color-coding user specified
  + Use biomaRt [24] to query gene selections against public genetics databases.
  + Heatmap
* Edge information tools:
  + Visualization of underlying scatterplots, resampled data, and implication class progression.
  + Various statistics that can be calculated on the fly for a given relationship.
    - Pearson, Spearman, mutual information (MI) [18], maximum information coefficient (MIC) [25], distance correlation (dCorr) [26], and DREMI.
* Sample information tools:
  + Color-coding (to be viewed in scatterplots).
* Computationally intensive operations should be user initiated—never automatic.

**Outcomes:** The primary output of aim 3 is a visualization software package developed for the R programing environment that will aid investigators in hypothesis generation, navigation, and organization of the data structures output from aims 1 and 2.

**Validation**

Validation of our construction can be made by comparison with known biological pathways found in the KEGG Pathway database. Gene products in these pathways have a causal relationship. If latency is sufficiently low, edges of our implication networks should capture those causal relationships.

One can also think of an implication network as a large machine learning undertaking. With this perspective, classical cross-validation between split training and testing sets may help us glean the predictive utility of our construction.

To take full advantage of the resolution of this technology, the datasets selected for analysis should include samples of likely different cellular subtypes. Therefore, tissue whose cells are suspected of going through a dynamic biological process such as proliferation, differentiation, or transition into malignancy may be of interest. Such datasets would also be well suited for evaluation of aim 2. Furthermore, the number of samples per subtype will impact the accuracy of estimated gene dependency metrics.

We will validate our methods on stem cell differentiation datasets with a large number of samples to test our analytics. There are a plethora of publically available datasets that meet our criteria. The datasets here represent the range of sample sizes available.

The DREMI metric specifically will be evaluated in the presence of a rare cellular subtype. GSE60749 is an examination of pluripotent stem cells (PSCs) in mus musculus brain tissues [17]. A cluster analysis by Kumar et al. find that there were two clusters. One composed of 98% of the samples and the other only 8% or 14 individual cells. This breakdown may constitute a rare cellular state suitable to evaluate the utility of DREMI-based subsampling techniques.

GSE64016 provides 460 human embryonic stem cells (hESC)—213 H1 single cells and 247 H1-Fucci labeled single cells. With a palatable number of samples, and labeled cycle stage data, this dataset can help evaluate the accuracy of pseudotemporal ordering.

GSE65525 provides ~3000 UMI-barcoded, differentiating, embryonic mouse stem cells from a massively parallelized microfluidics-based single-cell sequencing technology called DropSeq [27]. This dataset may be able to alleviate obstacles that arise from insufficient sample sizes.

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