

Fractal dimension and clinical neurophysiology fusion to gain a deeper brain signal understanding: A systematic review

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Background

Fractal Geometry

- Fractals are structures that repeat patterns at different scales (*self-similarity*).
- Basis for measuring complexity in nature and biological systems.

Fractal Dimension (FD)

- FD quantifies **irregularity and complexity** of a signal or structure.
- Higher FD = greater complexity and variability.
- Applied to **time series signals** to capture dynamics beyond linear methods.

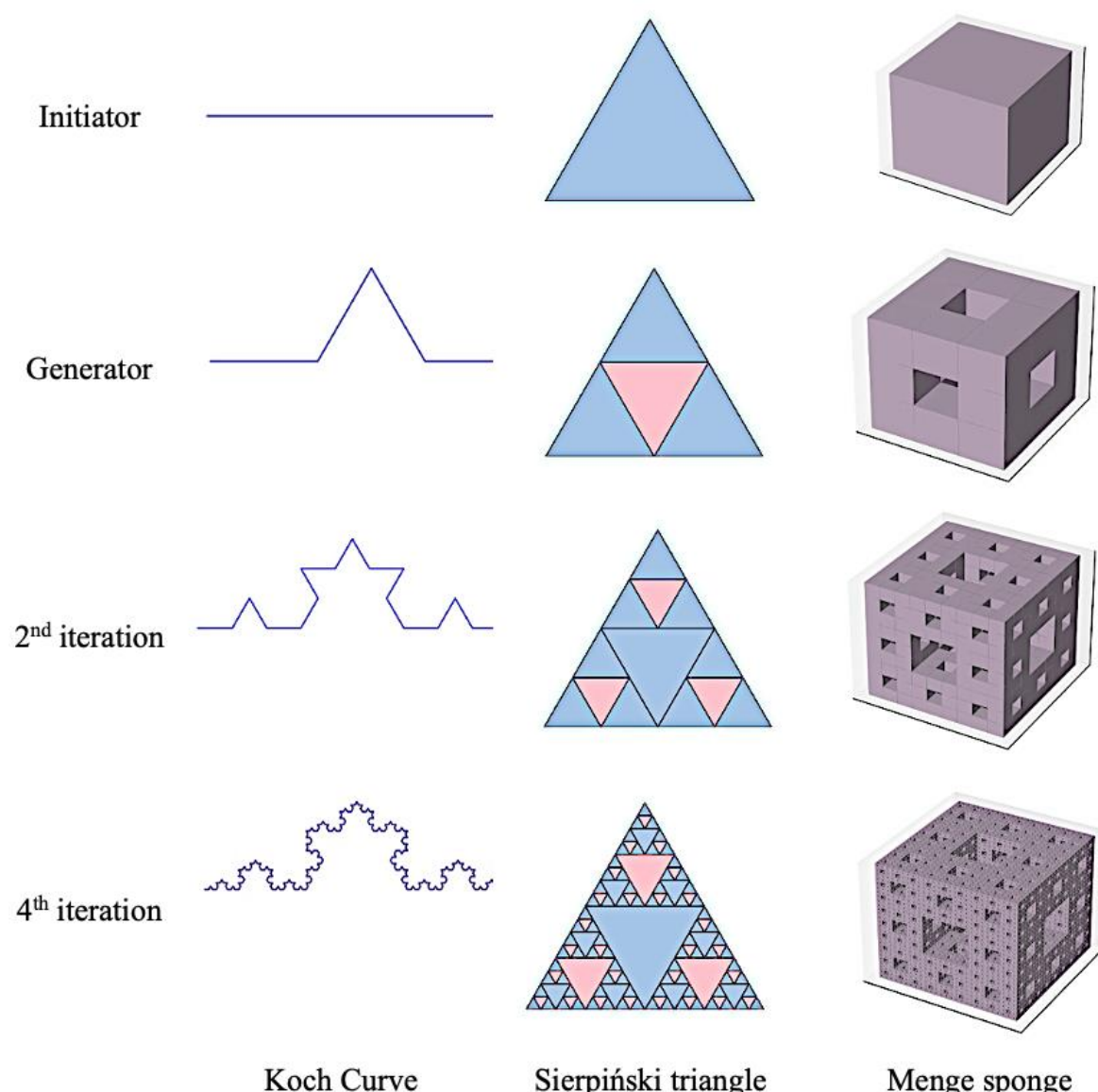
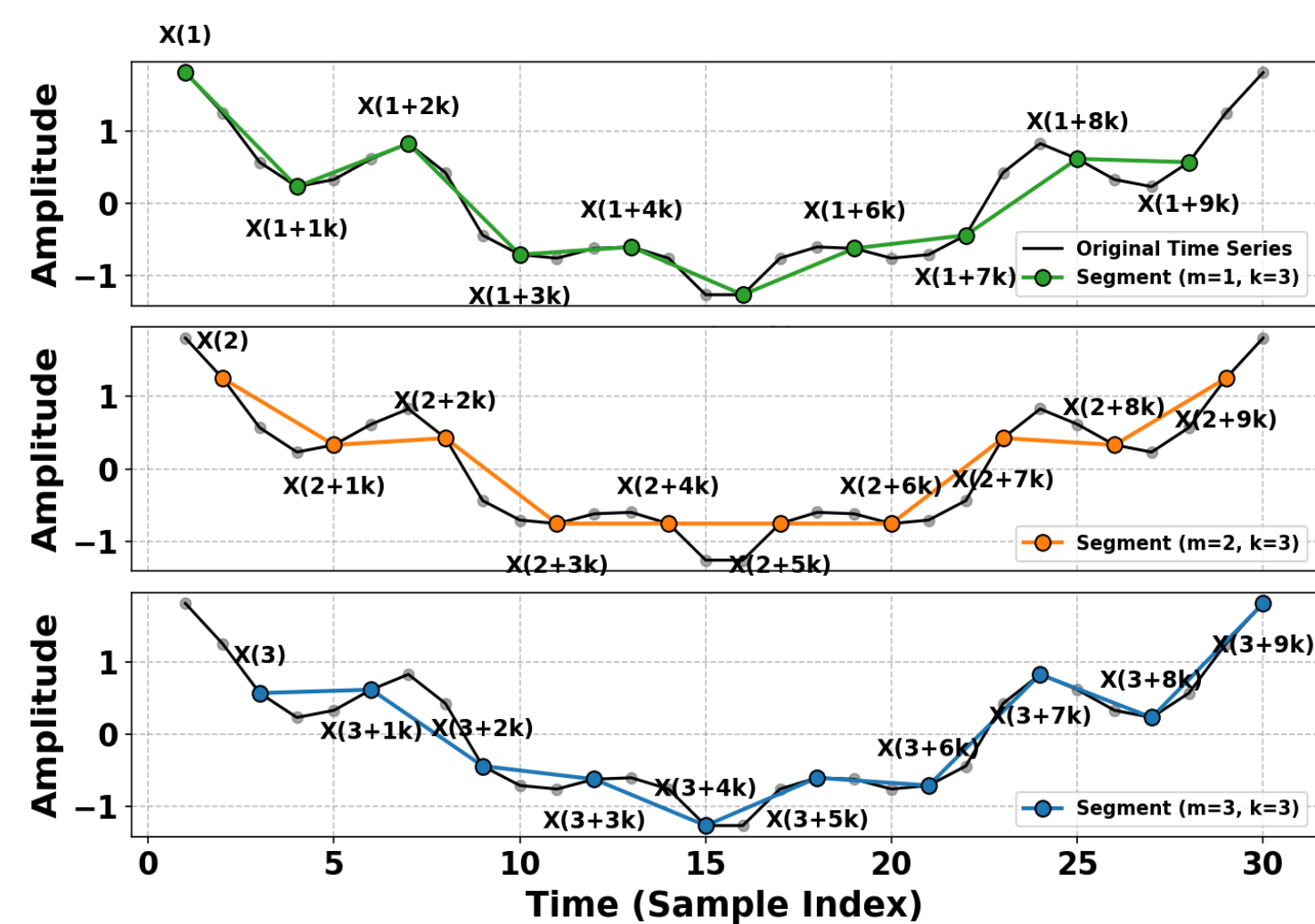


Fig1. Fractal Geometry (Koch curve, Sierpiński triangle, Menger sponge).

FD Calculation Methods

- Multiple algorithms exist: **sPSD** (Slope of Power Spectral Density), **DFA** (Detrended Fluctuation Analysis), **HE** (Hurst Exponent), **HFD** (Higuchi's Fractal Dimension), **KFD** (Katz's Fractal Dimension).



Higuchi Fractal Dimension (HFD)

- Estimates FD **directly in the time domain**.
- Well suited for **short, noisy, non-stationary signals** (e.g., EEG).
- Method**: Split signal into subseries → compute curve lengths → average → slope of log-log plot gives HFD.

Fig 2. Higuchi algorithm: the signal is segmented into subseries with different offsets (m) and step sizes (k) to compute curve lengths.

FD in Neurophysiology

- Brain signals (EEG, MEG, fMRI) are **non-linear and non-stationary**, making them difficult to analyze with classical linear methods. FD provides a mathematical measure of their complexity.

Objectives

- To systematically review applications of **FD** in clinical neurophysiology.
- To identify how FD has been used across neurological conditions.
- To evaluate the potential of FD as a **biomarker**.
- To summarize **meta-analysis findings** (Alzheimer's disease, stroke).

Methods

Database: PubMed was queried for the past 20 years using “fractal dimension” and “clinical neurophysiology” keywords. 499 articles identified.

Screening Process

- Excluded duplicates (n=2) and abstracts without full text (n=2).
- Removed studies on animals, retina, structural imaging (PET, CT), or brain morphology.
- Excluded cases where “fractal” was not used as a measure of signal complexity.
- Review papers were excluded but screened for relevant citations.

Citation search: added 9 additional studies.

Final Selection: 59 studies included in the review.

Trend: > 60% of studies were published in the last 5 years

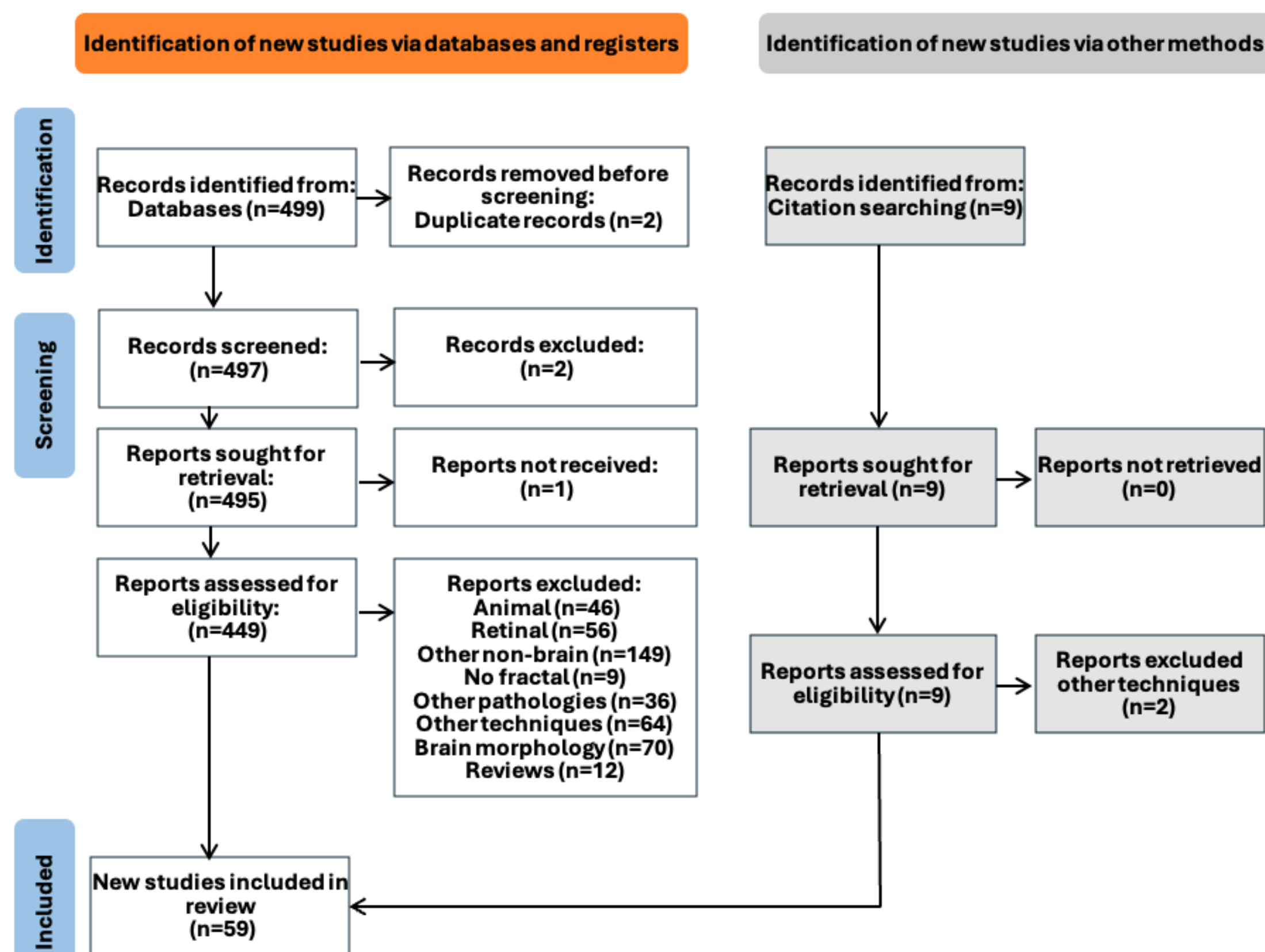


Fig3. PRISMA flow diagram of study selection

Findings Across Neurological Conditions

- Based on 59 studies included in this systematic review, FD shows disease-specific changes across several neurological conditions.
- Forest plots display the mean effect size (Hedges' g) with 95% confidence intervals, where negative values indicate a reduction in FD compared to healthy controls (HC).

Alzheimer's Disease (AD)

- FD is consistently **reduced** across EEG, MEG, and fMRI studies.
- This reduction is robust across multiple independent cohorts.
- Meta-analysis shows a significant overall decrease in FD** (summary effect size < 0, CI not overlapping zero), supporting FD as a reliable biomarker for AD detection and monitoring.

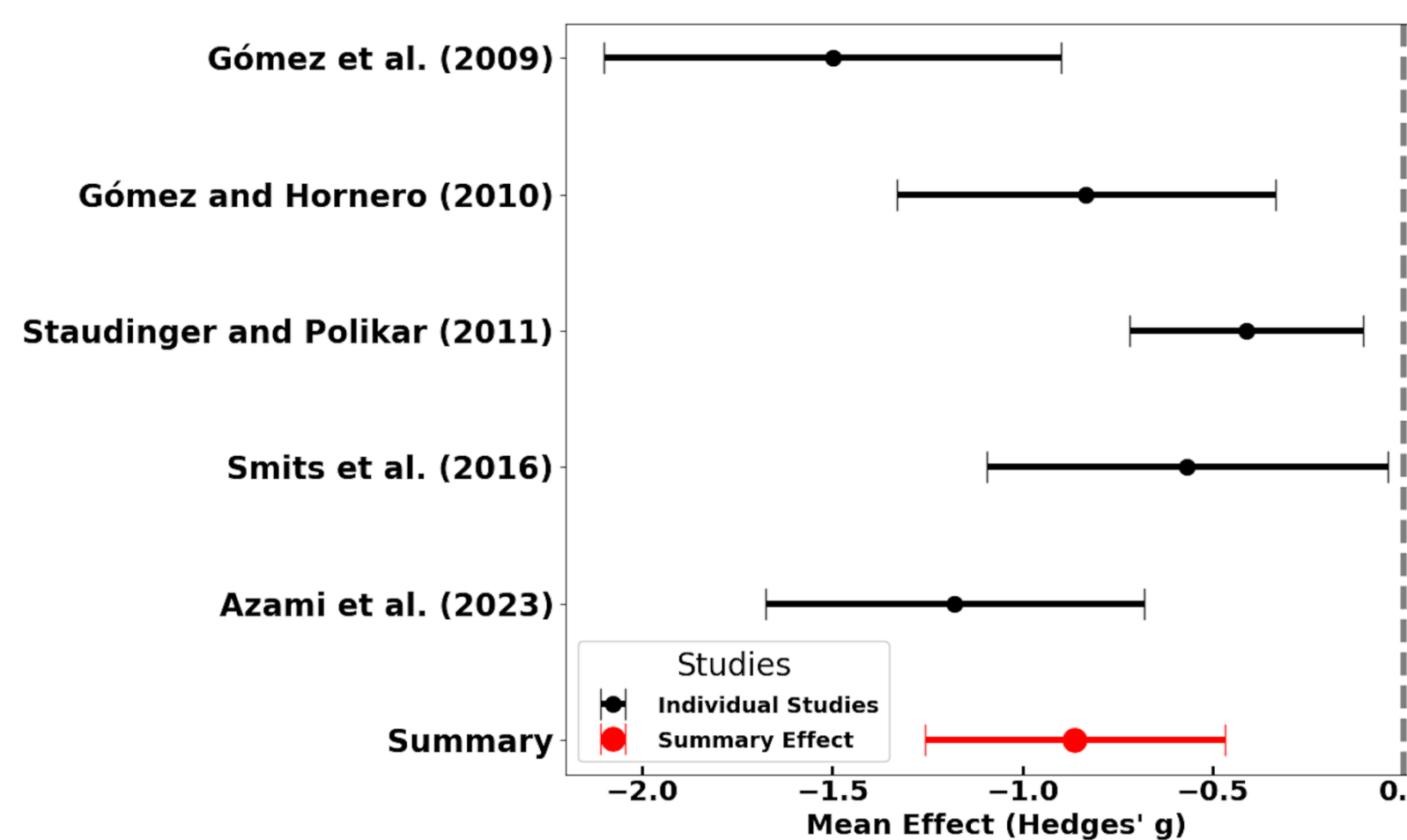


Fig4. Forest Plot of HFD Differences AD and Healthy Controls for meta analysis

Parkinson's Disease (PD)

- FD alterations correlate with **cognitive decline**.
- Suggests FD as a marker of disease-related brain dynamics.

Stroke

- FD shows a pronounced **reduction in the acute phase**.
- Demonstrates sensitivity to sudden neural damage.
- Meta-analysis supports FD reduction during acute and early subacute stages.

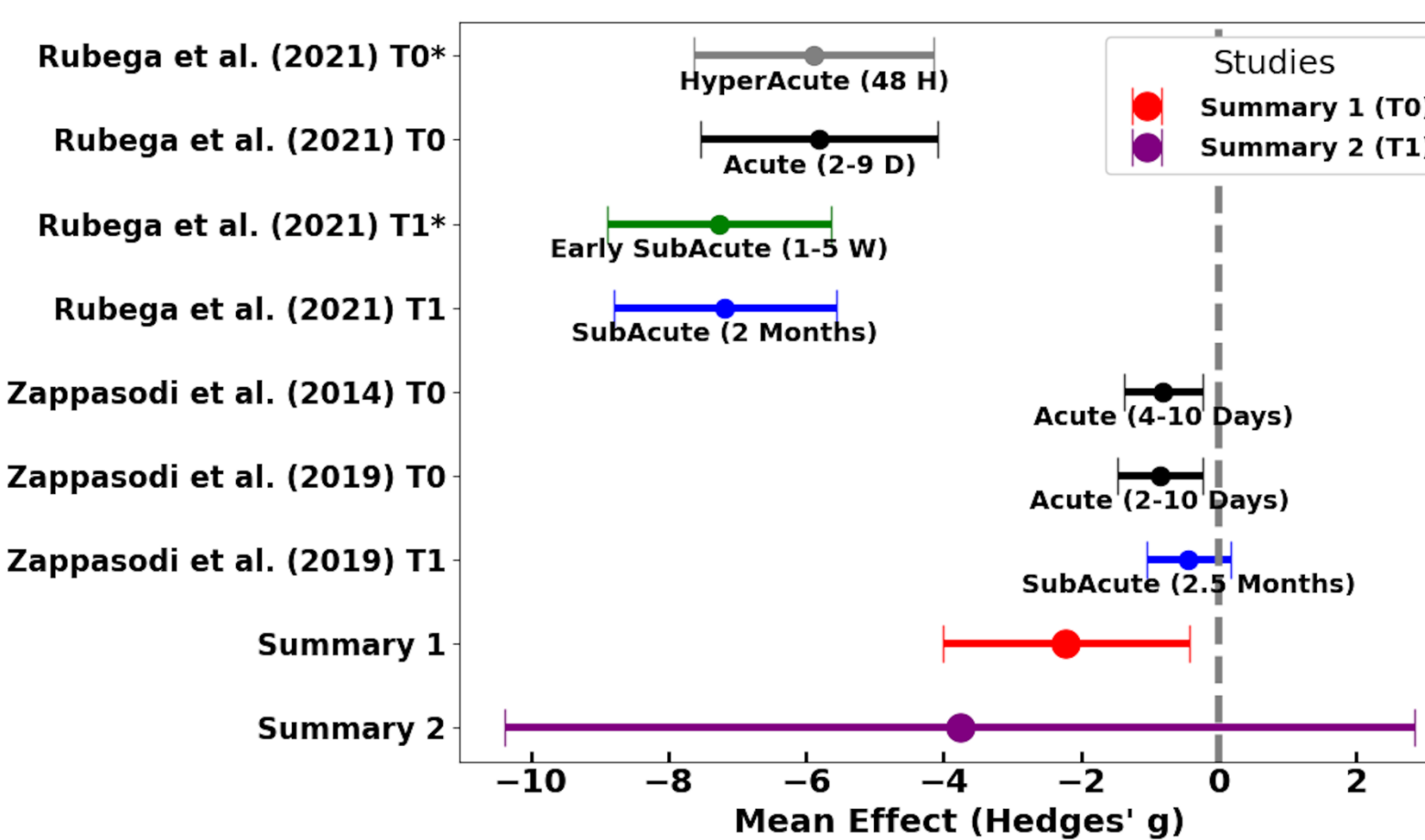


Fig5. Forest Plot of HFD Differences Stroke and Healthy Controls for meta analysis

Multiple Sclerosis (MS)

- FD is **altered** and responds to **stimulation paradigms**.
- Highlights FD's potential to track neuroplastic changes.

Schizophrenia (Scz)

- FD alterations and **multifractality** indicate disrupted network complexity.
- Meta-analysis shows significant FD reduction compared to controls**.

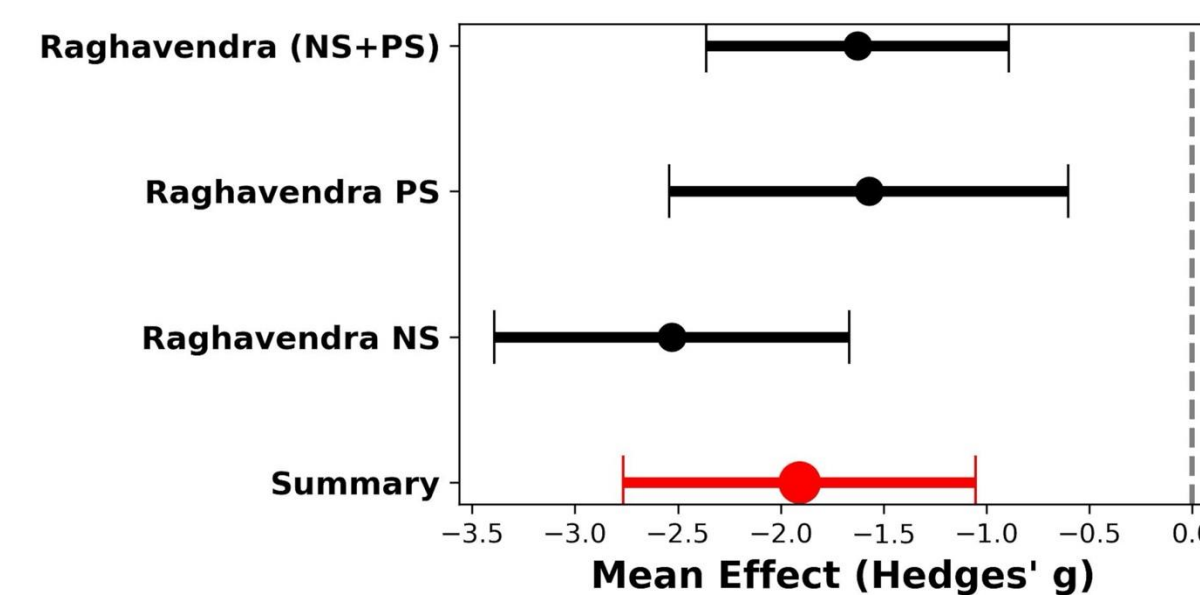


Fig6. Forest Plot of HFD Differences Scz and Healthy Controls for meta analysis

Aging

- FD follows an **inverted U-shaped trajectory**: higher in midlife, declining with older age.
- Reflects age-related reductions in brain signal complexity.
- Meta-analysis confirms FD decline with aging**.

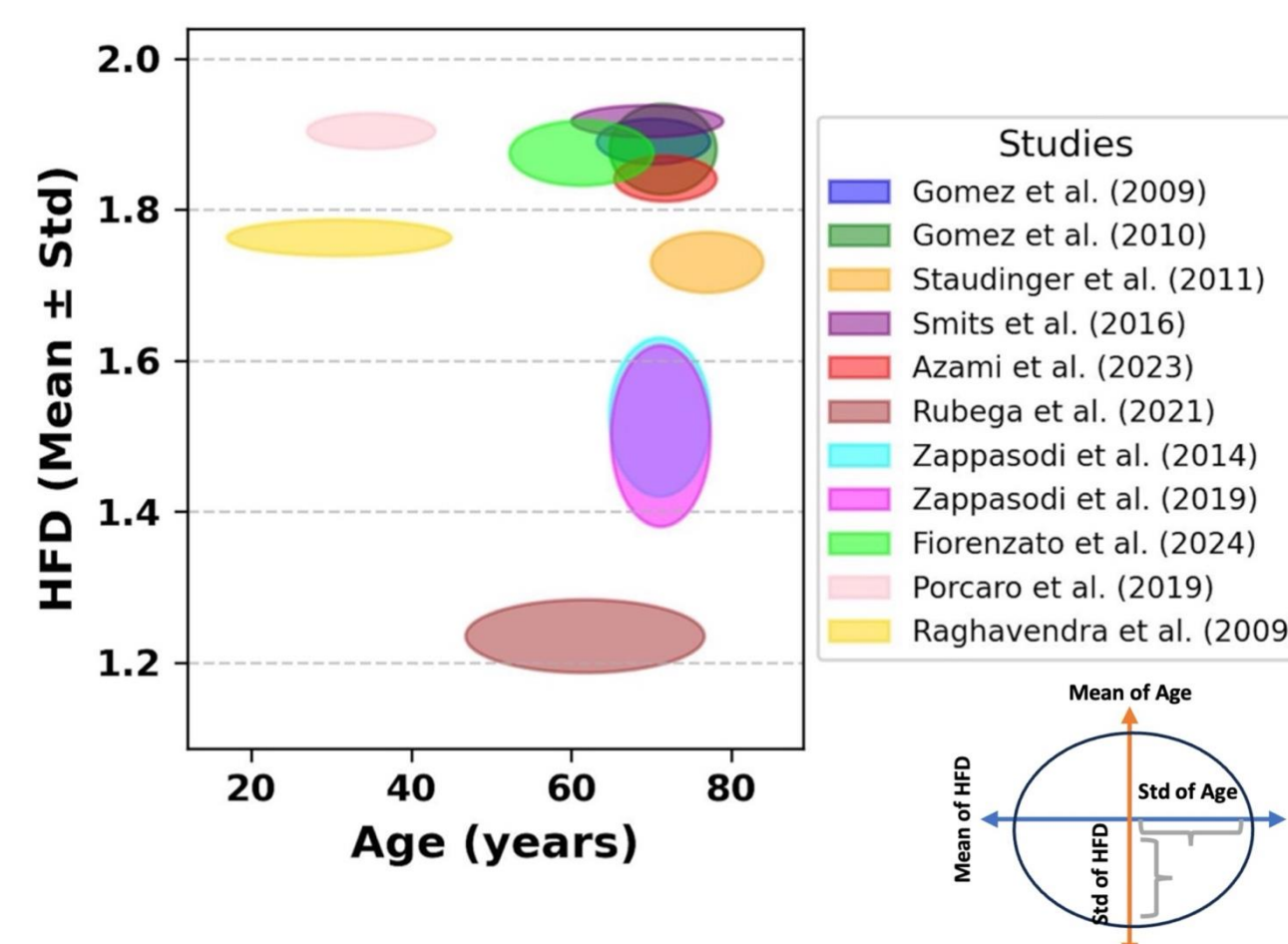


Fig7. HFD of HC subjects with different ages from different studies

Conclusion and Outlook

- FD provides a robust framework to capture **brain signal complexity**.
- Across **59 studies**, **Meta-analyses confirm significant FD reductions** in Alzheimer's disease, stroke, schizophrenia, and aging.
- HFD** is the most widely applied method for clinical signals.
- FD shows strong promise as a **biomarker** for diagnosis, monitoring.

Future Directions

- Standardize FD estimation methods across studies.
- Explore **longitudinal and real-time applications** in clinical practice.

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Summary of the reviewed literature on Higuchi's Fractal Dimension in Neurophysiology

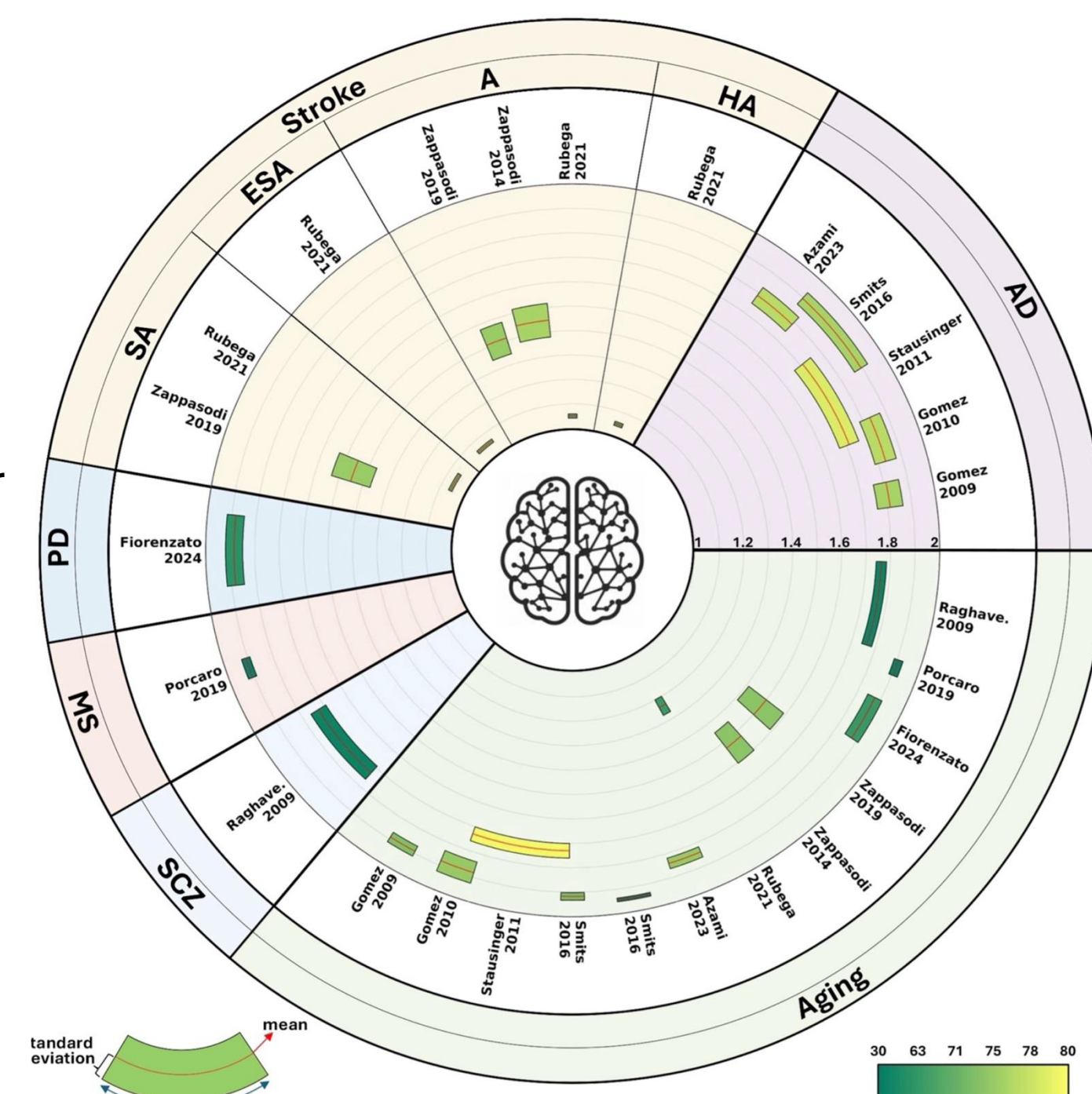


Fig8. Summary of the reviewed literature on HFD in neurophysiology across neurological conditions, showing sample size, variability, and age distribution.

