

# PyGeNN: A Python library for GPU-enhanced neural networks

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## 2 ABSTRACT

3 More than half of the Top 10 supercomputing sites worldwide use GPU accelerators and they  
4 are becoming ubiquitous in workstations and edge computing devices. GeNN is a C++ library for  
5 generating efficient spiking neural network simulation code for GPUs. However, until now, the full  
6 flexibility of GeNN could only be harnessed by writing model descriptions and simulation code in  
7 C++. Here we present PyGeNN, a Python package which exposes all of GeNN's functionality to  
8 Python with minimal overhead. This provides an alternative, arguably more user-friendly, way  
9 of using GeNN and allows modellers to use GeNN within the growing Python-based machine  
10 learning and computational neuroscience ecosystems. In addition, we demonstrate that, in both  
11 Python and C++ GeNN simulations, the overheads of recording spiking data can strongly affect  
12 runtimes and show how a new spike recording system can reduce these overheads by up to  
13 10×. Using the new recording system, we demonstrate that by using PyGeNN on a modern GPU,  
14 we can simulate a full-scale model of a cortical column faster even than real-time neuromorphic  
15 systems. Finally, we show that long simulations of a smaller model with complex stimuli and  
16 a custom three-factor learning rule defined in PyGeNN can be simulated almost two orders of  
17 magnitude faster than real-time.

18 **Keywords:** GPU, high-performance computing, parallel computing, benchmarking, computational neuroscience, spiking neural  
19 networks, Python

## 1 INTRODUCTION

20 A wide range of spiking neural network (SNN) simulators are available, each with their own application  
21 domains. NEST (Gewaltig and Diesmann, 2007) is widely used for large-scale point neuron simulations  
22 on distributed computing systems; NEURON (Carnevale and Hines, 2006) and Arbor (Akar et al., 2019)  
23 specialise in the simulation of complex multi-compartmental models; NeuroKernel (Givon and Lazar, 2016)  
24 is focused on emulating fly brain circuits using Graphics Processing Units (GPUs); and CARLsim (Chou  
25 et al., 2018), ANNarchy (Vitay et al., 2015), NeuronGPU (Golosio et al., 2021) and GeNN (Yavuz et al.,  
26 2016) use GPUs to accelerate point neuron models. For performance reasons, many of these simulators are  
27 written in C++ and, especially amongst the older simulators, users describe their models either using a  
28 Domain-Specific Language (DSL) or directly in C++. For programming language purists, fully custom

DSLs such as the HOC network description language in NEURON (Carnevale and Hines, 2006) or the NestML (Plotnikov et al., 2016) neuron modelling language may be elegant solutions and, for simulator developers, using C++ directly and not having to add bindings to another language is convenient. However, both choices act as a barrier to potential users. Therefore, with both the computational neuroscience and machine learning communities gradually coalescing towards a Python-based ecosystem with a wealth of mature libraries for scientific computing (Hunter, 2007; Van Der Walt et al., 2011; Millman and Aivazis, 2011), exposing spiking neural network simulators to Python with minimal domain specific modifications seems like a pragmatic choice. NEST (Eppler et al., 2009), NEURON (Hines et al., 2009) and CARLsim (Balaji et al., 2020) have all taken this route and now all offer Python interfaces. Furthermore, newer simulators such as Arbor and Brian2 (Stimberg et al., 2019) have been designed from the ground up with a Python interface.

Our GeNN simulator can already be used as a backend for the Python-based Brian2 simulator (Stimberg et al., 2019) using the Brian2GeNN interface (Stimberg et al., 2020) which modifies the C++ backend “cpp\_standalone” of Brian 2 to generate C++ input files for GeNN. As for cpp\_standalone, initialisation of simulations is mostly done in C++ on the CPU and recording data is saved into binary files and re-imported into Python using Brian 2’s native methods. While we have recently demonstrated some very competitive performance results (Knight and Nowotny, 2018, 2020) using GeNN in C++, and through the Brian2GeNN interface (Stimberg et al., 2020), GeNN could so far not be used directly from Python and it is not possible to expose all of GeNN’s unique features through the Brian2 API. Specifically, GeNN not only allows users to easily define their own neuron and synapse models but, also ‘snippets’ for offloading the potentially costly initialisation of model parameters and connectivity onto the GPU. Additionally, GeNN provides a lot of freedom for users to integrate their own code into the simulation loop. In this paper we describe the implementation of PyGeNN – a Python package which aims to expose the full range of GeNN functionality with minimal performance overheads. Unlike in the majority of other SNN simulators PyGeNN allows defining bespoke neuron and synapse models directly from Python without requiring users to extend the underlying C++ code. Below, we demonstrate the flexibility and performance of PyGeNN in two scenarios where minimising performance overheads is particularly critical.

- In a simulation of a large, highly-connected model of a cortical microcircuit (Potjans and Diesmann, 2014) with small simulation timesteps. Here the cost of copying spike data off the GPU from a large number of neurons every timestep can become a bottleneck.
- In a simulation of a much smaller model of Pavlovian conditioning (Izhikevich, 2007) where learning occurs over 1 h of biological time and stimuli are delivered – following a complex scheme – throughout the simulation. Here any overheads are multiplied by a large number of timesteps and copying stimuli to the GPU can become a bottleneck.

Using the facilities provided by PyGeNN, we show that both scenarios can be simulated from Python with only minimal overheads over a pure C++ implementation.

## 2 MATERIALS AND METHODS

### 2.1 GeNN

GeNN (Yavuz et al., 2016) is a library for generating CUDA (NVIDIA et al., 2020) code for the simulation of spiking neural network models. GeNN handles much of the complexity of using CUDA directly and automatically performs device-specific optimizations so as to maximize performance. GeNN consists of a

69 main library – implementing the API used to define models as well as the generic parts of the code generator  
 70 – and an additional library for each backend (currently there is a reference C++ backend for generating  
 71 CPU code and a CUDA backend. An OpenCL backend is under development). Users describe their model  
 72 by implementing a `modelDefinition` function within a C++ file. For example, a model consisting of 4  
 73 Izhikevich neurons with heterogeneous parameters, driven by a constant input current might be defined as  
 74 follows:

```

75 void modelDefinition(ModelSpec &model)
76 {
77     model.setDT(0.1);
78     model.setName("izhikevich");
79
80     NeuronModels::IzhikevichVariable::VarValues popInit(
81         -65.0, -20.0, uninitialisedVar(), uninitialisedVar(),
82         uninitialisedVar(), uninitialisedVar());
83
84     model.addNeuronPopulation<NeuronModels::IzhikevichVariable>(
85         "Pop", 4, {}, popInit);
86
87     model.addCurrentSource<CurrentSourceModels::DC>(
88         "CS", "Pop", {10.0}, {});
89 }
```

90 The `genn-buildmodel` command line tool is then used to compile this file; link it against the main GeNN  
 91 library and the desired backend library; and finally run the resultant executable to generate the source code  
 92 required to build a simulation dynamic library (a .dll file on Windows or a .so file on Linux and Mac). This  
 93 dynamic library can then either be linked against a simulation loop provided by the user or dynamically  
 94 loaded by the user's simulation code. To demonstrate this latter approach, the following example uses the  
 95 `SharedLibraryModel` helper class supplied with GeNN to dynamically load the previously defined model,  
 96 initialise the heterogenous neuron parameters and print each neuron's membrane voltage every timestep:

```

97 #include "sharedLibraryModel.h"
98
99 int main()
100 {
101     SharedLibraryModel<float> model("./", "izhikevich");
102     model.allocateMem();
103     model.initialize();
104     float *aPop = model.getScalar<float>("aPop");
105     float *bPop = model.getScalar<float>("bPop");
106     float *cPop = model.getScalar<float>("cPop");
107     float *dPop = model.getScalar<float>("dPop");
108     aPop[0] = 0.02; bPop[0] = 0.2; cPop[0] = -65.0; dPop[0] = 8.0;
109     aPop[1] = 0.1; bPop[1] = 0.2; cPop[1] = -65.0; dPop[1] = 2.0;
110     aPop[2] = 0.02; bPop[2] = 0.2; cPop[2] = -50.0; dPop[2] = 2.0;
111     aPop[3] = 0.02; bPop[3] = 0.2; cPop[3] = -55.0; dPop[3] = 4.0;
112     model.initializeSparse();
113
114     float *vPop = model.getScalar<float>("VPop");
115     while(model.getTime() < 200.0f) {
```

```

116     model.stepTime();
117     model.pullVarFromDevice("Pop", "V");
118     printf("%f, %f, %f, %f, %f\n",
119           t, VPop[0], VPop[1], VPop[2], VPop[3]);
120 }
121 return EXIT_SUCCESS;
122 }

```

## 123 2.2 SWIG

124 In order to use GeNN from Python, both the model creation API and the `SharedLibraryModel`  
 125 functionality need to be ‘wrapped’ so they can be called from Python. While this is possible using  
 126 the API built into Python itself, wrapper functions would need to be manually implemented for each GeNN  
 127 function to be exposed which would result in a lot of maintenance overhead. Instead, we chose to use  
 128 SWIG (Beazley, 1996) to automatically generate wrapper functions and classes. SWIG generates Python  
 129 modules based on special interface files which can directly include C++ code as well as special ‘directives’  
 130 which control SWIG. For example, the following SWIG interface file would wrap the C++ code in `test.h` in  
 131 a Python module called `test_module` within a Python packages called `test_package`:

```

132 %module(package="test_package") test_module
133 %include "test.h"

```

134 The `%module` directive sets the name of the generated module and the package it will be located in and  
 135 the `%include` directive parses and automatically generates wrapper functions for the C++ header file. We  
 136 use SWIG in this manner to wrap both the model building and `SharedLibraryModel` APIs described in  
 137 section 2.1. However, key parts of GeNN’s API such as the `ModelSpec::addNeuronPopulation` method  
 138 employed in section 2.1, rely on C++ templates which are not directly translatable to Python. Instead, valid  
 139 template instantiations need to be given a unique name in Python using the `%template` SWIG directive:

```

140 %template(addNeuronPopulationLIF) ModelSpec::addNeuronPopulation<NeuronModels::LIF>;

```

141 Having to manually add these directives whenever a model is added to GeNN would be exactly the sort  
 142 of maintenance overhead we were trying to avoid by using SWIG. Therefore, when building the Python  
 143 wrapper, we instead search the GeNN header files for the macros used to declare models in C++ and  
 144 automatically generate SWIG `%template` directives.

145 As previously discussed, a key feature of GeNN is the ease with which it allows users to define their  
 146 own neuron and synapse models as well as ‘snippets’ defining how variables and connectivity should be  
 147 initialised. Beneath the syntactic sugar described in our previous work (Knight and Nowotny, 2018), new  
 148 models can be defined in C++ by defining a new class derived from, for example, the `NeuronModels::Base`  
 149 class. The ability to extend this system to Python was a key requirement of PyGeNN and, by using SWIG  
 150 ‘director’, C++ classes can be made inheritable from Python using a single SWIG directive:

```

151 %feature("director") NeuronModels::Base;

```

## 152 2.3 PyGeNN

153 While GeNN *could* be used from Python via the wrapper generated using SWIG, the resultant code  
 154 would be unpleasant to use directly. For example, rather than being able to specify neuron parameters  
 155 using a native Python types such as lists or dictionaries, one would have to use a wrapped type such as

156 `DoubleVector`([0.25, 10.0, 0.0, 0.0, 20.0, 2.0, 0.5]). Therefore, in order to provide a more  
 157 user-friendly and pythonic interface, we have built PyGeNN on top of the wrapper generated by SWIG.  
 158 PyGeNN combines the separate model building and simulation stages of building a GeNN model in  
 159 C++ into a single API, likely to be more familiar to users of existing Python-based model description  
 160 languages such as PyNEST (Eppler et al., 2009) or PyNN (Davison et al., 2008). By combining the two  
 161 stages together, PyGeNN can provide a unified dictionary-based API for initialising homogeneous and  
 162 heterogeneous parameters as shown in this re-implementation of the previous example:

```

163 from pygenn import genn_wrapper, genn_model
164
165 model = genn_model.GeNNModel("float", "izhikevich")
166 model.dT = 0.1
167
168 izk_init = {"V": -65.0,
169            "U": -20.0,
170            "a": [ 0.02, 0.1, 0.02, 0.02],
171            "b": [ 0.2, 0.2, 0.2, 0.2],
172            "c": [-65.0, -65.0, -50.0, -55.0],
173            "d": [ 8.0, 2.0, 2.0, 4.0]}
174
175 pop = model.add_neuron_population("Pop", 4, "IzhikevichVariable",
176                                 {}, izk_init)
177 model.add_current_source("CS", "DC", "Pop",
178                         {"amp": 10.0}, {})
179
180 model.build()
181 model.load()
182
183 v = pop.vars["V"].view
184 while model.t < 200.0:
185     model.step_time()
186     model.pull_state_from_device("Pop")
187     print("%f, %f, %f, %f, %f"
188           % (model.t, v[0], v[1], v[2], v[3]))

```

189 Initialisation of variables with homogeneous values – such as the neurons’ membrane potential – is  
 190 performed by initialisation kernels generated by GeNN and initialisation of variables with heterogeneous  
 191 values – such as the `a`, `b` and `c` parameters – are copied to the GPU by PyGeNN after the model is loaded.  
 192 While the PyGeNN API is more pythonic and, hopefully, more user-friendly than the C++ interface, it  
 193 still provides users with the same low-level control over the simulation. Furthermore, by using SWIG’s  
 194 numpy (Van Der Walt et al., 2011) interface, the host memory allocated by GeNN can be accessed directly  
 195 from Python using the `pop.vars["V"].view` syntax meaning that no potentially expensive additional  
 196 copying of data is required.

197 As illustrated in the previously-defined model, for convenience, PyGeNN allows users to access GeNN’s  
 198 built-in models. However, one of PyGeNN’s most powerful features is that it enables users to easily  
 199 define their own neuron and synapse models from within Python. For example, an Izhikevich neuron  
 200 model (Izhikevich, 2003) can be defined using the `create_custom_neuron_class` helper function which  
 201 provides some syntactic sugar over directly inheriting from the SWIG director class:



```

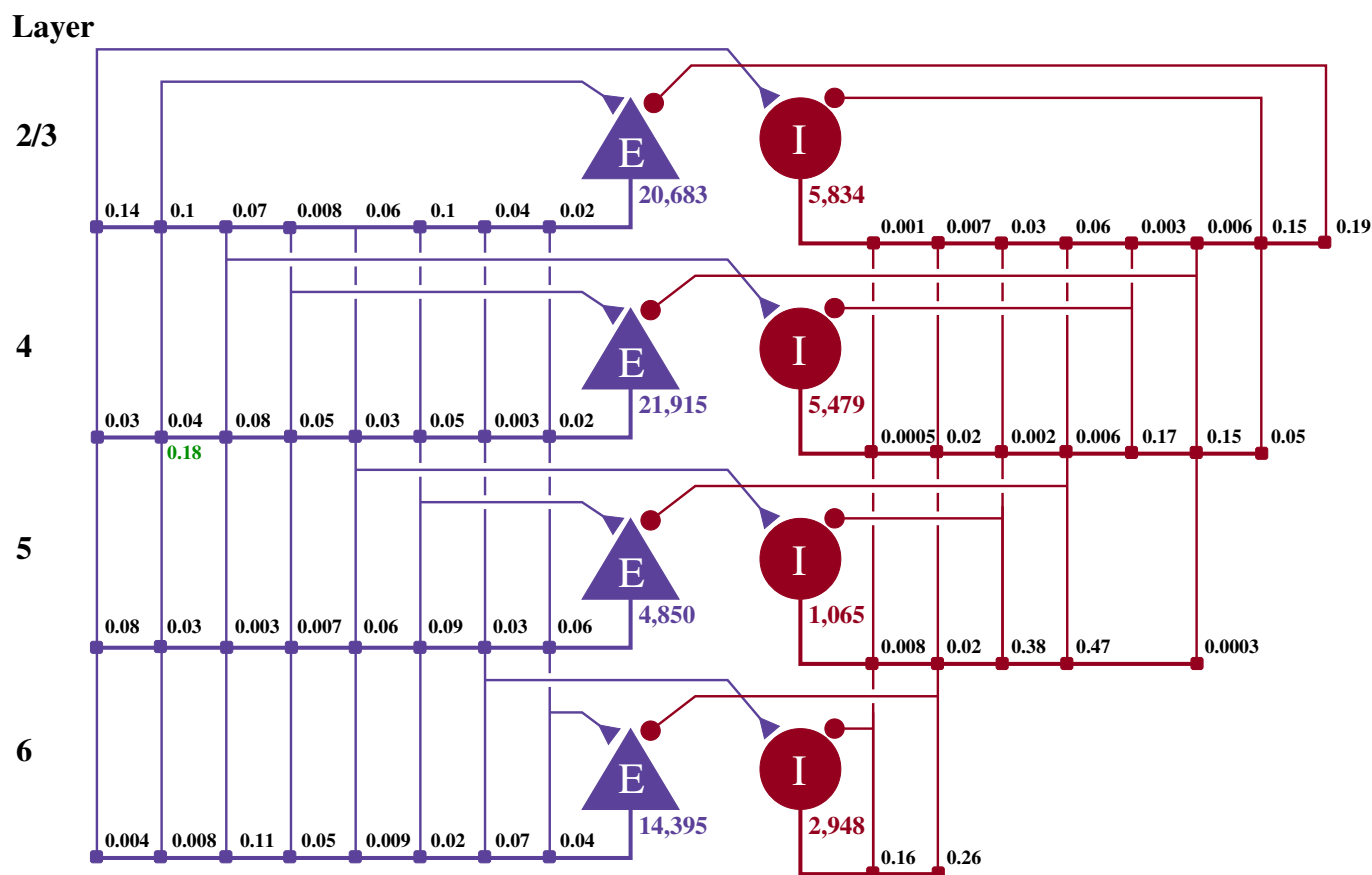
202 izk_model = genn_model.create_custom_neuron_class(
203     "izk",
204     param_names=["a", "b", "c", "d"],
205     var_name_types=[("V", "scalar"), ("U", "scalar")],
206     sim_code=
207         """
208         $(V) += 0.5 * (0.04 * $(V) * $(V) + 5.0 * $(V) + 140.0 - $(U) + $(Isyn)) * DT;
209         $(V) += 0.5 * (0.04 * $(V) * $(V) + 5.0 * $(V) + 140.0 - $(U) + $(Isyn)) * DT;
210         $(U) += $(a) * ($(b) * $(V) - $(U)) * DT;
211         """,
212     threshold_condition_code="$ (V) >= 30.0",
213     reset_code=
214         """
215         $(V) = $(c) ;
216         $(U) += $(d) ;
217         """)

```

218 The `param_names` list defines the real-valued parameters that are constant across the whole population of  
 219 neurons and the `var_name_types` list defines the model state variables and their type (the `scalar` type  
 220 is an alias for either single or double-precision floating point, depending on the precision passed to the  
 221 `GeNNModel` constructor). The behaviour of the model is then defined using a number of code strings. Unlike  
 222 in tools like Brian 2 (Stimberg et al., 2019), these code strings are specified in a C-like language rather  
 223 than using differential equations. This language provides standard C control flow statements as well as  
 224 the transcendental functions from the standard maths library. Additionally, variables provided by GeNN  
 225 such as the membrane voltage in the model above can be accessed using the `$(V)` syntax and functions  
 226 provided by GeNN can be called using the `$(F, 1, 2)` syntax (where `F` is a 2 argument function). This  
 227 allows expert users to choose their own solver for models described in terms of differential equations and to  
 228 programatically define models such as spike sources. For example, in the model presented above, we chose  
 229 to implement the neuron using the idiosyncratic forward Euler integration scheme employed by Izhikevich  
 230 (2003). Finally, the `threshold_condition_code` expression defines *when* the neuron will spike whereas  
 231 the `reset_code` code string defines how the state variables should be reset after a spike.

## 232 2.4 Spike recording system

233 Internally, GeNN stores the spikes emitted by a neuron population during one simulation timestep in  
 234 an array containing the indices of the neurons that spiked alongside a counter of how many spikes have  
 235 been emitted overall. Previously, recording spikes in GeNN was very similar to the recording of voltages  
 236 shown in the previous example code – the array of neuron indices was simply copied from the GPU to  
 237 the CPU every timestep. However, especially when simulating models with a small simulation timestep,  
 238 such frequent synchronization between the CPU and GPU is costly – especially if a slower, interpreted  
 239 language such as Python is involved. Furthermore, biological neurons typically spike at a low rate (in the  
 240 cortex, the average firing rate is only around 3 Hz (Buzsáki and Mizuseki, 2014)) meaning that the amount  
 241 of spike data transferred every timestep is typically very small. One solution to these inefficiencies is to  
 242 store many timesteps worth of spike data on the GPU and use more infrequent, larger transfers to copy it  
 243 to the CPU. At low firing rates, the most memory efficient solution would be to simply store the indices  
 244 of neurons which spiked each timestep, for example in a data structure similar to a Yale sparse matrix  
 245 with each ‘row’ representing a timestep (**TODO: CITE**). However, not only would the efficiency of this  
 246 approach rely on GeNN *only* being used for models with biologically-plausible firing rates, but the amount



**Figure 1.** Illustration of the microcircuit model. Blue triangles represent excitatory populations, red circles represent inhibitory populations and the number beneath each symbol shows the number of neurons in each population. Connection probabilities are shown in small bold numbers at the appropriate point in the connection matrix. All excitatory synaptic weights are normally distributed with a mean of 0.0878 nA (unless otherwise indicated in green) and a standard deviation of 0.008 78 nA. All inhibitory synaptic weights are normally distributed with a mean of 0.3512 nA and a standard deviation of 0.035 12 nA.

of memory required to store the spikes for a given number of timesteps could not be determined ahead of time. In a CPU-based simulator, this would not be problematic as additional memory could be allocated as required. However, the fine grained global synchronisation this would require would not be easily achievable on a GPU. Therefore, we instead represent the spikes emitted by a population of  $N$  neurons in a single simulation timestep as a  $N$ bit bitfield where a '1' represents a spike and a '0' the absence of one. Spiking data over multiple timesteps is then represented by a circular buffer of these bitfields. While at very low firing rates, this approach uses more memory than storing the indices of the neurons which spiked, it still allows the spiking output of relatively large models, running for many timesteps to be stored in a small amount of memory. For example, the spiking output of a model with  $100 \times 10^3$  neurons running for  $10 \times 10^3$  simulation timesteps, required less than 120 MB – a small fraction of the memory on a modern GPU. While efficiently handling spikes stored in a bitfield is a little trickier than working with a list of neuron indices, GeNN provides an efficient C++ helper function for saving the spikes stored in a bitfield to a text file and a numpy-based method for decoding them in PyGeNN.

## 260 2.5 Cortical microcircuit model

Potjans and Diesmann (2014) developed the cortical microcircuit model of  $1 \text{ mm}^3$  of early-sensory cortex illustrated in figure 1. The model consists of 77 169 LIF neurons, divided into separate populations representing the excitatory and inhibitory population in each of 4 cortical layers (2/3, 4, 5 and 6). The membrane voltage  $V_i$  of each neuron  $i$  is modelled as:

$$\tau_m \frac{dV_i}{dt} = (V_{\text{rest}} - V_i) + R_m(I_{\text{syn}_i} + I_{\text{ext}_i}), \quad (1)$$

where  $\tau_m = 10 \text{ ms}$  and  $R_m = 40 \text{ M}\Omega$  represent the time constant and resistance of the neuron's cell membrane,  $V_{\text{rest}} = -65 \text{ mV}$  defines the resting potential,  $I_{\text{syn}_i}$  represents the synaptic input current and  $I_{\text{ext}_i}$  represents an external input current. When the membrane voltage crosses a threshold  $V_{\text{th}} = -50 \text{ mV}$  a spike is emitted, the membrane voltage is reset to  $V_{\text{rest}}$  and updating of  $V$  is suspended for a refractory period  $\tau_{\text{ref}} = 2 \text{ ms}$ . Neurons in each population are connected randomly with numbers of synapses derived from an extensive review of the anatomical literature. These synapses are current-based, i.e. presynaptic spikes lead to exponentially-decaying input currents  $I_{\text{syn}_i}$

$$\tau_{\text{syn}} \frac{dI_{\text{syn}_i}}{dt} = -I_{\text{syn}_i} + \sum_{j=0}^n w_{ij} \sum_{t_j} \delta(t - t_j), \quad (2)$$

where  $\tau_{\text{syn}} = 0.5 \text{ ms}$  represents the synaptic time constant,  $w_{ij}$  represents the synaptic weight and  $t_j$  are the arrival times of incoming spikes from  $n$  presynaptic neurons. Within each synaptic projection, all synaptic strengths and transmission delays are normally distributed using the parameters presented in Potjans and Diesmann (2014, table 5) and, in total, the model has approximately  $0.3 \times 10^9$  synapses. As well as receiving synaptic input, each neuron in the network also receives an independent Poisson input current, representing input from neighbouring not explicitly modelled cortical regions. The Poisson input is delivered to each neuron via  $I_{\text{ext}_i}$  with

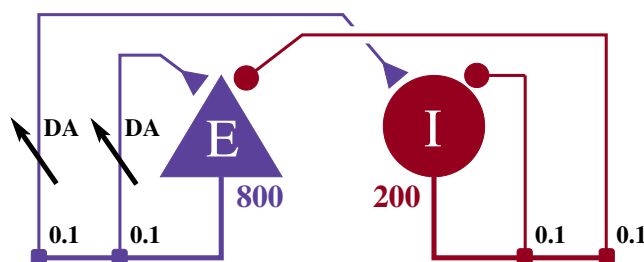
$$\tau_{\text{syn}} \frac{dI_{\text{ext}_i}}{dt} = -I_{\text{ext}_i} + w_{\text{ext}} \text{Poisson}(\nu_{\text{ext}} \Delta t), \quad (3)$$

261 where  $\nu_{\text{ext}}$  represents the mean input rate and  $w_{\text{ext}}$  represents the weight. The ordinary differential  
 262 Eq. 1, 2 and 3 are solved with an exponential Euler algorithm. For a full description of the model  
 263 parameters, please refer to Potjans and Diesmann (2014, tables 4 and 5) and for a description of the  
 264 strategies used by GeNN to parallelise the initialisation and subsequent simulation of this network, please  
 265 refer to Knight and Nowotny (2018, section 2.3). This model requires simulation using a relatively small  
 266 timestep of  $0.1 \text{ ms}$ , making the overheads of copying spikes from the GPU every timestep particularly  
 267 problematic.

## 268 2.6 Pavlovian conditioning model

269 The cortical microcircuit model described in the previous section is ideal for exploring the performance  
 270 of short simulations of relatively large models. However, the performance of longer simulations of smaller  
 271 models is equally vital. Such models can be particularly troublesome for GPU simulation as, not only might  
 272 they not offer enough parallelism to fully occupy the device but, each timestep can be simulated so quickly  
 273 that the overheads of launching kernels etc can dominate. Additional overheads can be incurred when  
 274 models require injecting external stimuli throughout the simulation. Longer simulations are particularly





**Figure 2.** Illustration of the balanced random network model. The blue triangle represents the excitatory population, the red circle represents the inhibitory population, and the numbers beneath each symbol show the number of neurons in each population. Connection probabilities are shown in small bold numbers at the appropriate point in the connection matrix. All excitatory synaptic weights are plastic and initialised to 1 and all inhibitory synaptic weights are initialised to  $-1$ .

useful when exploring synaptic plasticity so, to explore the performance of PyGeNN in this scenario, we simulate a model of Pavlovian conditioning using a three-factor Spike-Timing-Dependent Plasticity (STDP) learning rule (Izhikevich, 2007).

## 2.6.1 Neuron model

The model illustrated in figure 2 consists of an 800 neuron excitatory population and a 200 neuron inhibitory population, within which, each neuron  $i$  is modelled using the Izhikevich model (Izhikevich, 2003) whose dimensionless membrane voltage  $V_i$  and adaption variables  $U_i$  evolve such that:

$$\frac{dV_i}{dt} = 0.04V_i^2 + 5V_i + 140 - U_i + I_{\text{syn}_i} + I_{\text{ext}_i} \quad (4)$$

$$\frac{dU_i}{dt} = a(bV_i - U_i) \quad (5)$$

When the membrane voltage rises above 30, a spike is emitted and  $V_i$  is reset to  $c$  and  $d$  is added to  $U_i$ . Excitatory neurons use the regular-spiking parameters (Izhikevich, 2003) where  $a = 0.02$ ,  $b = 0.2$ ,  $c = -65.0$ ,  $d = 8.0$  and inhibitory neurons use the fast-spiking parameters (Izhikevich, 2003) where  $a = 0.1$ ,  $b = 0.2$ ,  $c = -65.0$ ,  $d = 2.0$ . Again,  $I_{\text{syn}_i}$  represents the synaptic input current and  $I_{\text{ext}_i}$  represents an external input current. While there are numerous ways to solve Eq. 4 and 5 (Humphries and Gurney, 2007; Hopkins and Furber, 2015; Pauli et al., 2018), we chose to use the idiosyncratic forward Euler integration scheme employed by Izhikevich (2003) in the original work (Izhikevich, 2007). Under this scheme, Eq. 4 is first integrated for two 0.5 ms timesteps and then, based on the updated value of  $V_i$ , Eq. 5 is integrated for a single 1 ms timestep.

## 2.6.2 Synapse models

The excitatory and inhibitory neural populations are connected recurrently, as shown in figure 1, with instantaneous current-based synapses:

$$I_{\text{syn}_i}(t) = \sum_{j=0}^n w_{ij} \sum_{t_j} \delta(t - t_j), \quad (6)$$

where  $t_j$  are the arrival times of incoming spikes from  $n$  presynaptic neurons. Inhibitory synapses are static with  $w_{ij} = -1.0$  and excitatory synapses are plastic. Each plastic synapse has an eligibility trace  $C_{ij}$  as

well as a synaptic weight  $w_{ij}$  and these evolve according to a three-factor STDP learning rule (Izhikevich, 2007):

$$\frac{dC_{ij}}{dt} = -\frac{C_{ij}}{\tau_c} + \text{STDP}(\Delta t)\delta(t - t_{\text{pre/post}}) \quad (7)$$

$$\frac{dw_{ij}}{dt} = -C_{ij}D_j \quad (8)$$

where  $\tau_c = 1000$  ms represents the decay time constant of the eligibility trace and  $\text{STDP}(\Delta t)$  describes the magnitude of changes made to the eligibility trace in response to the relative timing of a pair of pre and postsynaptic spikes with temporal difference  $\Delta t = t_{\text{post}} - t_{\text{pre}}$ . These changes are only applied to the trace at the times of pre and postsynaptic spikes as indicated by the Dirac delta function  $\delta(t - t_{\text{pre/post}})$ . Here, a double exponential STDP kernel is employed such that:

$$\text{STDP}(\Delta t) = \begin{cases} A_+ \exp\left(-\frac{\Delta t}{\tau_+}\right) & \text{if } \Delta t > 0 \\ A_- \exp\left(\frac{\Delta t}{\tau_-}\right) & \text{if } \Delta t < 0 \\ 0 & \text{otherwise} \end{cases} \quad (9)$$

where the time constant of the STDP window  $\tau_+ = \tau_- = 20$  ms and the strength of potentiation and depression are  $A_+ = 0.1$  and  $A_- = 0.15$  respectively. Finally, each excitatory neuron has an additional variable  $D_j$  which describes extracellular dopamine concentration:

$$\frac{D_j}{t} = -\frac{D_j}{\tau_d} + \text{DA}(t) \quad (10)$$

289 where  $\tau_d = 200$  ms represents the time constant of dopamine uptake and  $\text{DA}(t)$  the dopamine input over  
290 time.

### 291 2.6.3 PyGeNN implementation of three-factor STDP

292 The first step in implementing this learning rule in PyGeNN is to implement the STDP updates and decay  
293 of  $C_{ij}$  using GeNN's event-driven plasticity system, the implementation of which was described in our  
294 previous work (Knight and Nowotny, 2018). Using a similar syntax to that described in section 2.3, we first  
295 create a new 'weight update model' with the learning rule parameters and the  $w_{ij}$  and  $C_{ij}$  state variables:

```
296 izhikevich_stdp_model = create_custom_weight_update_class(
297     "izhikevich_stdp",
298
299     param_names=["tauPlus", "tauMinus",
300                 "tauC", "aPlus", "aMinus"],
301     var_name_types=[("w", "scalar"), ("c", "scalar")],
```

302 We then instruct GeNN to record the times of current and previous pre and postsynaptic spikes. The current  
303 spike time will equal the current time if a spike of this sort is being processed in the current timestep  
304 whereas the previous spike time only tracks spikes which have occurred *before* the current timestep:

```
305     is_pre_spike_time_required=True,
306     is_post_spike_time_required=True,
307
```

```

308     is_prev_pre_spike_time_required=True,
309     is_prev_post_spike_time_required=True,

```

310 Next we define the ‘sim code’ which is called whenever presynaptic spikes arrive at the synapse. This code  
 311 first implements Eq. 6 – adding the synaptic weight ( $w_{ij}$ ) to the postsynaptic neuron’s input ( $I_{\text{syn}_i}$ ) using  
 312 the `$(addToInSyn, x)` function.

```

313     sim_code=
314         """
315         $(addToInSyn, $(w));

```

316 Within the sim code we also need to calculate the time that has elapsed since the last update of  $C_{ij}$  using  
 317 the spike times we previously requested that GeNN record. Within a timestep, GeNN processes presynaptic  
 318 spikes before postsynaptic spikes so the time of the last update to  $C_{ij}$  will be the latest time either type of  
 319 spike was processed in previous timesteps:

```

320         const scalar tc = fmax($(prev_sT_pre),
321                                $(prev_sT_post));

```

322 Using this time, we can now calculate how much to decay  $C_{ij}$  using the closed-form solution to Eq. 7:

```

323         const scalar tagDecay = exp(-$(t) - tc) / $(tauC);
324         scalar newTag = $(c) * tagDecay;

```

325 To complete the sim code we calculate the depression case of Eq. 9 (here we use the *current* postsynaptic  
 326 spike time as, if a postsynaptic and presynaptic spike occur in the same timestep, there should be no  
 327 update).

```

328         const scalar dt = $(t) - $(sT_post);
329         if (dt > 0) {
330             newTag -= ($(aMinus) * exp(-dt / $(tauMinus)));
331         }
332         $(c) = newTag;
333         """

```

334 Finally we define the ‘learn post code’ which is called whenever a postsynaptic spike arrives at the synapse.  
 335 Other than implementing the potentiation case of Eq. 9 and using the *current* presynaptic spike time when  
 336 calculating the time since the last update of  $C_{ij}$  – in order to correctly handle presynaptic updates made in  
 337 the same timestep – this code is very similar to the sim code:

```

338     learn_post_code=
339         """
340         const scalar tc = fmax($(sT_pre),
341                                $(prev_sT_post));
342
343         const scalar tagDecay = exp(-$(t) - tc) / $(tauC);
344         scalar newTag = $(c) * tagDecay;
345
346         const scalar dt = $(t) - $(sT_pre);
347         if (dt > 0) {
348             newTag += ($(aPlus) * exp(-dt / $(tauPlus)));

```

```

349     }
350     $(c) = newTag;
351     """)

```

352 Adding the synaptic weight  $w_{ij}$  update described by Eq. 8 requires two further additions to the model.  
353 As well as the pre and postsynaptic spikes, the weight update model needs to receive events whenever  
354 dopamine is injected via DA. GeNN supports such events via the ‘spike-like event’ system which allows  
355 events to be triggered based on an expression evaluated on the presynaptic neuron. In this case, this  
356 expression simply tests an `injectDopamine` flag which gets set by the dopamine injection logic in our  
357 presynaptic neuron model:

```

358     event_threshold_condition_code="injectDopamine",

```

359 In order to extend our event-driven update of  $C_{ij}$  to include spike-like events we need to instruct GeNN to  
360 record the times at which they occur:

```

361     is_pre_spike_event_time_required=True,
362     is_prev_pre_spike_event_time_required=True,

```

363 The spike-like events can now be handled using a final ‘event code’ string:

```

364     event_code=
365     ""
366     const scalar tc = fmax($(sT_pre), fmax($(prev_sT_post), $(prev_seT_pre)));
367     const scalar tagDecay = exp(-$(t) - tc) / $(tauC));
368     $(c) *= tagDecay;
369     "",

```

After updating the previously defined calculations of `tc` in the sim code and learn post code in the same way to also include the times of spike-like events, all that remains is to update  $w_{ij}$ . Mikaitis et al. (2018) showed how Eq. 8 could be solved algebraically, allowing  $w_{ij}$  to be updated in an event-driven manner with:

$$\Delta w_{ij} = \frac{C(t_c^{last})D(t_d^{last})}{-\left(\frac{1}{\tau_c} + \frac{1}{\tau_d}\right)} \left( e^{-\frac{t-t_c^{last}}{\tau_c}} e^{-\frac{t-t_d^{last}}{\tau_d}} - e^{-\frac{t_w^{last}-t_c^{last}}{\tau_c}} e^{-\frac{t_w^{last}-t_d^{last}}{\tau_d}} \right) \quad (11)$$

where  $t_c^{last}$ ,  $t_w^{last}$  and  $t_d^{last}$  represent the last times at which  $C_{ij}$ ,  $W_{ij}$  and  $D_j$  respectively were updated. Because we will always update  $w_{ij}$  and  $C_{ij}$  together when presynaptic, postsynaptic and spike-like events occur,  $t_c^{last} = t_w^{last}$  and Eq. 11 can be simplified to:

$$\Delta w_{ij} = \frac{C(t_c^{last})D(t_d^{last})}{-\left(\frac{1}{\tau_c} + \frac{1}{\tau_d}\right)} \left( e^{-\frac{t-t_c^{last}}{\tau_c}} e^{-\frac{t-t_d^{last}}{\tau_d}} - e^{-\frac{t_c^{last}-t_d^{last}}{\tau_d}} \right) \quad (12)$$

370 and this update can now be added to each of our three event handling code strings to complete the  
371 implementation of the learning rule.

## 2.6.4 PyGeNN implementation of Pavlovian conditioning experiment

To perform the Pavlovian conditioning experiment described by Izhikevich (2007) using this model, we chose 100 random groups of 50 neurons (each representing stimuli  $S_1 \dots S_{100}$ ) from amongst the two neural populations. Stimuli are presented to the network in a random order, separated by intervals sampled from  $U(100, 300)$ ms. The neurons associated with an active stimulus are stimulated for a single 1 ms simulation timestep with a current of 40.0 nA, in addition to the random background current of  $U(-6.5, 6.5)$ nA, delivered to each neuron via  $I_{\text{ext}_i}$  throughout the simulation.  $S_1$  is arbitrarily chosen as the Conditional Stimuli (CS) and, whenever this stimuli is presented, a reward in the form of an increase in dopamine is delivered by setting  $\text{DA}(t) = 0.5$  after a delay sampled from  $U(0, 1000)$ ms. This delay period is large enough to allow a few irrelevant stimuli to be presented which act as distractors. The simplest way to implement this stimulation regime is to add a current source to the excitatory and inhibitory neuron populations which adds the uniformly-distributed input current to an externally-controllable per-neuron current. In PyGeNN, the following model can be defined to do just that:

```
stim_noise_model = create_custom_current_source_class(
    "stim_noise",
    param_names=["n"],
    var_name_types=[("iExt", "scalar", VarAccess_READ_ONLY)],
    injection_code=
        """
        $(injectCurrent, $(iExt) + ($(gennrand_uniform) * $(n) * 2.0) - $(n));
        """
)
```

where the `n` parameter sets the magnitude of the background noise, the `$(injectCurrent, i)` function injects a current of  $I$ nA into the neuron and `$(gennrand_uniform)` samples from  $U(0, 1)$  using the ‘XORWOW’ pseudo-random number generator provided by cuRAND (NVIDIA Corporation, 2019). Once a current source population using this model has been instantiated and a memory view to `iExt` obtained in the manner described in section 2.3, in timesteps when stimulus injection is required, current can be injected into the list of neurons contained in `stimuli_input_set` with:

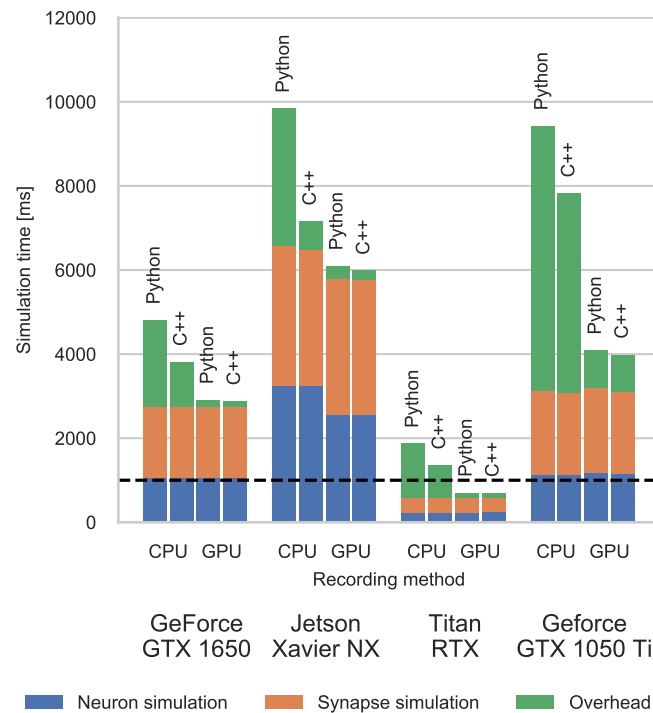
```
curr_ext_view[stimuli_input_set] = 40.0
curr_pop.push_var_to_device("iExt")
```

The same approach can then be used to zero the current afterwards.

## 3 RESULTS

In the following subsections we will analyse the performance of the models introduced in sections 2.5 and 2.6 on a representative selection of NVIDIA GPU hardware:

- Jetson Xavier NX – a low-power embedded system with a GPU based on the Volta architecture with 8 GB of shared memory.
- GeForce GTX 1050Ti – a low-end desktop GPU based on the Pascal architecture with 4 GB of dedicated memory.
- GeForce GTX 1650 – a low-end desktop GPU based on the Turing architecture with 4 GB of dedicated memory.



**Figure 3.** Simulation times of the microcircuit model running on various GPU hardware for 1 s of biological time. ‘Overhead’ refers to time spent in simulation loop but not within CUDA kernels. The dashed horizontal line indicates realtime performance

- Titan RTX – a high-end workstation GPU based on the Turing architecture with 24 GB of dedicated memory.

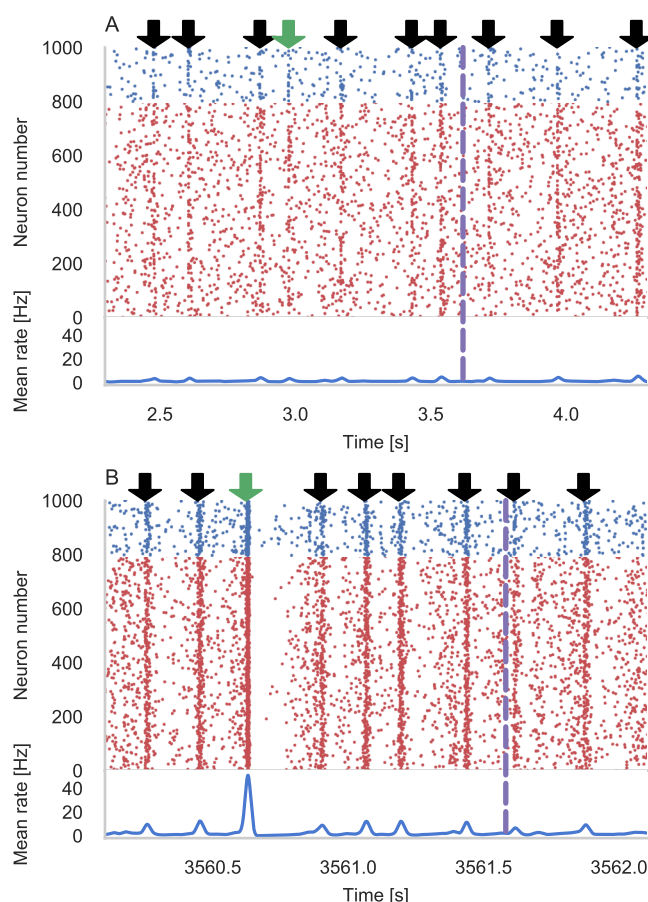
All of these systems run Ubuntu 18 apart from the system with the GeForce 1050 Ti which runs Windows 10.

### 3.1 Cortical microcircuit model performance

Figure 3 shows the simulation times for the full-scale microcircuit model. We measured the total simulation time by querying the `std::chrono::high_resolution_clock` in C++ and the `time.perf_counter` in Python before and after the simulation loop; and used CUDA’s own event timing system (NVIDIA Corporation, 2021, Section 3.2.6.7) to record the time taken by the neuron and synapse kernels. As one might predict, the Jetson Xavier NX is slower than the three desktop GPUs but, considering that it only consumes a maximum of 15 W compared to 75 W or 320 W for the GeForce cards and Titan RTX respectively, it still performs impressively. The time taken to actually simulate the models (‘Neuron simulation’ and ‘Synapse simulation’) are the same when using Python and C++ as all GeNN optimisation options are exposed to PyGeNN. Interestingly, when simulating *this* model, the larger L1 cache and architectural improvements present in the Turing-based GTX 1650 do not result in significantly improved performance over the Pascal-based GTX 1050Ti. Instead, the slightly improved performance of the GTX 1650 can probably be explained by its additional 128 CUDA cores.

Without the recording system described in section 2.4, the CPU and GPU need to be synchronised after every timestep to allow spike data to be copied off the GPU and stored in a suitable data structure. The ‘overheads’ shown in figure 3 indicate the time taken by these processes as well as the unavoidable

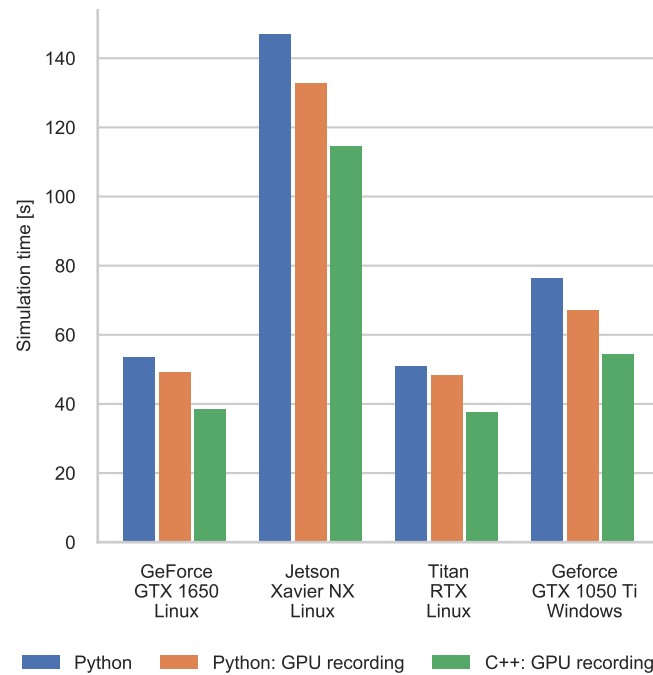




**Figure 4.** Results of Pavlovian conditioning experiment. Raster plot and spike density function (SDF) (Szücs, 1998) showing activity centred around first delivery of Conditional Stimulus (CS) during initial (A) and final (B) 50 s of simulation. Downward green arrows indicate times at which CS is delivered and downward black arrows indicate times when other, un-rewarded stimuli are delivered. Vertical dashed lines indicate times at which dopamine is delivered. The population SDF was calculated by convolving the spikes with a Gaussian kernel of  $\sigma = 10$  ms width.

overheads of launching CUDA kernels etc. Because Python is an interpreted language, updating the spike data structures is somewhat slower and this is particularly noticeable on devices with a slower CPU such as the Jetson Xavier NX. However, unlike the desktop GPUs, the Jetson Xavier NX's 8 GB of memory is shared between the GPU and the CPU meaning that data does not need to be copied between their memories and can instead be accessed by both. While, using this shared memory for recording spikes reduces the overhead of copying data off the device, because the GPU and CPU caches are not coherent, caching must be disabled on this memory which reduces the performance of the neuron kernel. Although the Windows machine has a relatively powerful CPU, the overheads measured in both the Python and C++ simulations run on this system are extremely large due to additional queuing between the application and the GPU driver caused by the Windows Display Driver Model (WDDM). When small – in this case 0.1 ms – simulation timesteps are used, this makes per-timestep synchronisation disproportionately expensive.

However, when the spike recording system described in section 2.4 is used, spike data is kept in GPU memory until the end of the simulation and overheads are reduced by up to  $10\times$ . Because synchronisation with the CPU is no longer required every timestep, simulations run approximately twice as fast on the Windows machine. Furthermore, on the high-end desktop GPU, the simulation now runs faster than



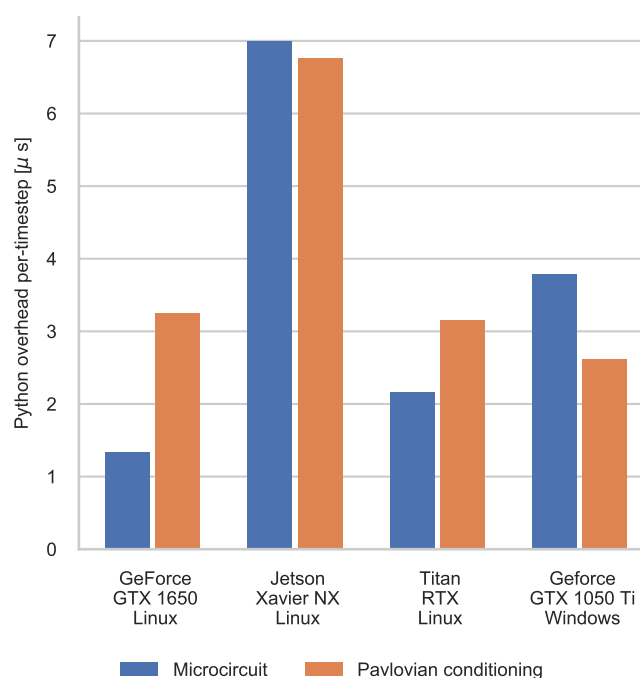
**Figure 5.** Simulation times of the Pavlovian Conditioning model running on various GPU hardware for 1 h of biological time. ‘GPU recording’ indicates simulations where the new recording system is employed. Times are taken from averages calculated over 5 runs of each model.

real-time in both Python and native C++ versions – significantly faster than other recently published GPU simulators (Golosio et al., 2021) and even specialised neuromorphic systems (Rhodes et al., 2020).

### 3.2 Pavlovian conditioning performance

Figure 4 shows the results of an example simulation of the Pavlovian conditioning model. At the beginning of each simulation (Figure 4A), the neurons representing every stimulus respond equally. However, after 1 h of simulation, the response to the CS becomes much stronger (Figure 4B) – showing that these neurons have been selectively associated with the stimulus even in the presence of the distractors and the delayed reward.

In figure 5, we show the runtime performance of simulations of the Pavlovian conditioning model, running on the GPUs described above using PyGeNN with and without the recording system described in section 2.4. These PyGeNN results are compared to a C++ simulation which also uses the recording system. Because each simulation timestep only takes a few  $\mu$ s, the overhead of using CUDA timing events significantly alters the performance so, for this model, we only measure the duration of the simulation loop using the approaches described in the previous section. Although we only record the spiking activity during the first and last 50 s, using the recording system still significantly improves the overall performance on all devices – especially on the Jetson Xavier NX with its slower CPU. Interestingly the Titan RTX and GTX 1650 perform identically in this benchmark with speedups ranging from  $62\times$  to  $72\times$  real-time. This is because, as discussed previously, this model is simply not large enough to fill the 4608 CUDA cores present on the Titan RTX. Therefore, as the two GPUs share the same Turing architecture and have very similar clock speeds (1350 MHz–1770 MHz for the Titan RTX and 1485 MHz–1665 MHz for the GTX 1650), the two GPUs perform very similarly. Similarly to the simulations of the microcircuit model, the Jetson Xavier NX performs rather slower than the desktop GPUs but still achieves speedups of up to  $31\times$ .



**Figure 6.** Comparison of the duration of individual timestep in Python and C++ simulation in microcircuit and Pavlovian conditioning experiments. Times are taken from averages calculated over 5 runs of the fastest version of each model i.e. the versions using the GPU recording system.

467 Interestingly, unlike in the simulations of the microcircuit model, here the GTX 1050 Ti performs  
 468 rather differently. Although the clock speed of this device is approximately the same as the other GPUs  
 469 (1290 MHz–1392 MHz) and it has a similar number of CUDA cores to the GTX 1650, its performance  
 470 is significantly worse. The difference in performance across all configurations is likely to be due to  
 471 architectural differences between the older Pascal; and newer Volta and Turing architectures. Specifically,  
 472 Pascal GPUs have one type of Arithmetic Logic Unit (ALU) which handles both integer and floating point  
 473 arithmetic whereas, the newer Volta and Turing architectures have equal numbers of dedicated integer and  
 474 floating point ALUs as well as significantly larger L1 caches. As discussed in our previous work (Knight  
 475 and Nowotny, 2018), these architectural features are particularly beneficial for SNN simulations with STDP  
 476 where a large amount of floating point computation is required to update the synaptic state *and* additional  
 477 integer arithmetic is required to calculate the indices into the sparse matrix data structures.

478 The difference between the speeds of the Python and C++ simulations of the Pavlovian conditioning  
 479 model (figure 5) *appear* much larger than those of the microcircuit model (figure 3). However, as figure 6  
 480 illustrates, for individual timesteps the excess time due to overheads is approximately the same for both  
 481 models and consistent with the cost of a small number of Python to C++ function calls (Apache Crail,  
 482 2019). Depending on the size and complexity of the model as well as the hardware used, this overhead may  
 483 or may not be important. For example, when simulating the microcircuit model for 1 s on the Titan RTX,  
 484 the overhead of using Python is less than 0.2 % but, when simulating the Pavlovian conditioning model on  
 485 the same device, the overhead of using Python is almost 31 %.

## 4 DISCUSSION

486 In this paper we have introduced PyGeNN, a Python interface to the C++ based GeNN library for GPU  
487 accelerated spiking neural network simulations.

488 Uniquely, the new interface provides access to all the features of GeNN, without leaving the comparative  
489 simplicity of Python and with, as we have shown, typically negligible overheads from the Python  
490 bindings. PyGeNN also allows bespoke neuron and synapse models to be defined from within Python,  
491 making PyGeNN much more flexible and broadly applicable than, for instance, the Python interface  
492 to NEST (Eppler et al., 2009) or the PyNN model description language used to expose CARLsim to  
493 Python (Balaji et al., 2020).

494 In many ways, the new interface resembles elements of the Python-based Brian 2 simulator (Stimberg  
495 et al., 2019) (and it's Brian2GeNN backend (Stimberg et al., 2020)) with two key differences. Unlike in  
496 Brian 2, bespoke models in PyGeNN are defined with 'C-like' code snippets. This has the advantage of  
497 unparalleled flexibility for the expert user, but comes at the cost of more complexity as the code for a  
498 timestep update needs to include a suitable solver as well as merely differential equations. The second  
499 difference lies in how data structures are handled. Whereas simulations run using the C++ or Brian2GeNN  
500 Brian 2 backends use files to exchange data with Python, the underlying GeNN data structures are directly  
501 accessible from PyGeNN meaning that no disk access is involved.

502 As we have demonstrated, the PyGeNN wrapper, exactly like native GeNN, can be used on a variety  
503 of hardware from data centre scale down to mobile devices such as the NVIDIA Jetson. This allows for  
504 the same codes to be used in large-scale brain simulations and embedded and embodied spiking neural  
505 network research. Supporting the popular Python language in this interface makes this ecosystem available  
506 to a wider audience of researchers in both Computational Neuroscience, bio-mimetic machine learning and  
507 autonomous robotics.

508 The new interface also opens up opportunities to support researchers that work with other Python based  
509 systems. In the Computational Neuroscience and Neuromorphic computing communities, we can now build  
510 a PyNN (Davison et al., 2008) interface on top of PyGeNN and, in fact, a prototype of such an interface is  
511 in development. Furthermore, for the burgeoning spike-based machine learning community, we can use  
512 PyGeNN as the basis for a spike-based machine learning framework akin to TensorFlow or PyTorch for  
513 rate-based models. A prototype interface of this sort called mlGeNN is in development and close to release.

514 In this work we have introduced a new spike recording system for GeNN and have shown that, using this  
515 system, we can now simulate the Potjans microcircuit model (Potjans and Diesmann, 2014) faster than  
516 real-time and, to the best of our knowledge, faster than any other system. Finally, the excellent performance  
517 we have demonstrated using low-end Turing architecture GPUs is very exciting in terms of increasing the  
518 accessibility of GPU accelerated Computational Neuroscience and SNN machine learning research.

## CONFLICT OF INTEREST STATEMENT

519 The authors declare that the research was conducted in the absence of any commercial or financial  
520 relationships that could be construed as a potential conflict of interest.

## AUTHOR CONTRIBUTIONS

JK and TN wrote the paper. TN is the original developer of GeNN. AK was the original developer of PyGeNN. JK is currently the primary developer of both GeNN and PyGeNN and was responsible for implementing the spike recording system. JK performed the experiments and the analysis of the results that are presented in this work.

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## DATA AVAILABILITY STATEMENT

All models, data and analysis scripts used for this study can be found in [https://github.com/BrainsOnBoard/pygenn\\_paper](https://github.com/BrainsOnBoard/pygenn_paper). All experiments were carried out using the GeNN 4.4.0 which is available from <https://doi.org/10.5281/zenodo.4419159>.

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