

PyGeNN: A Python library for GPU-enhanced neural networks

James C Knight^{1,*}, Anton Komissarov^{2,3}, Thomas Nowotny¹

¹*Centre for Computational Neuroscience and Robotics, School of Engineering and Informatics, University of Sussex, Brighton, United Kingdom*

²*Bernstein Center for Computational Neuroscience Berlin, Germany*

³*Technische Universität Berlin, Germany*

Correspondence*:

James C Knight

J.C.Knight@sussex.ac.uk

2 ABSTRACT

3 More than half of the Top 10 supercomputing sites worldwide use GPU accelerators and they
4 are becoming ubiquitous in workstations and edge computing devices. GeNN is a C++ library for
5 generating efficient spiking neural network simulation code for GPUs. However, until now, the full
6 flexibility of GeNN could only be harnessed by writing model descriptions and simulation code in
7 C++. Here we present PyGeNN, a Python package which exposes all of GeNN's functionality to
8 Python with minimal overhead. This provides an alternative, arguably more user-friendly, way
9 of using GeNN and allows modellers to use GeNN within the growing Python-based machine
10 learning and computational neuroscience ecosystems. In addition, we demonstrate that, in both
11 Python and C++ GeNN simulations, the overheads of recording spiking data can strongly affect
12 runtimes and show how a new spike recording system can reduce these overheads by up to
13 10×. Using the new recording system, we demonstrate that by using PyGeNN on a modern GPU,
14 we can simulate a full-scale model of a cortical column faster even than real-time neuromorphic
15 systems. Finally, we show that long simulations of a smaller model with complex stimuli and a
16 custom three-factor learning rule defined in PyGeNN can be simulated up to 72× faster than
17 real-time.

18 **Keywords:** GPU, high-performance computing, parallel computing, benchmarking, computational neuroscience, spiking neural
19 networks, Python

1 INTRODUCTION

20 A wide range of spiking neural network (SNN) simulators are available, each with their own application
21 domains. NEST (Gewaltig and Diesmann, 2007) is widely used for large-scale point neuron simulations
22 on distributed computing systems; NEURON (Carnevale and Hines, 2006) and Arbor (Akar et al., 2019)
23 specialise in the simulation of complex multi-compartmental models; NeuroKernel (Givon and Lazar, 2016)
24 is focused on emulating fly brain circuits using Graphics Processing Units (GPUs); and CARLsim (Chou
25 et al., 2018), ANNarchy (Vitay et al., 2015), NeuronGPU (?) and GeNN (Yavuz et al., 2016) use GPUs to
26 accelerate point neuron models. For performance reasons, many of these simulators are written in C++
27 and, especially amongst the older simulators, users describe their models either using a Domain-Specific
28 Language (DSL) or directly in C++. For programming language purists, fully custom DSLs such as

the HOC model description language in NEURON (Carnevale and Hines, 2006) or NestML (Plotnikov et al., 2016) may be elegant ways of describing an SNN network model and, for simulator developers, not having to add bindings to another language is convenient. However, both choices act as a barrier to potential users. Therefore, with both the computational neuroscience and machine learning communities gradually coalescing towards a Python-based ecosystem with a wealth of mature libraries for scientific computing (Hunter, 2007; Van Der Walt et al., 2011; Millman and Aivazis, 2011), exposing spiking neural network simulators to Python with minimal domain specific modifications seems like a pragmatic choice. NEST (Eppler et al., 2009), NEURON (Hines et al., 2009) and CARLsim (Balaji et al., 2020) have all taken this route and now all offer Python interfaces. Furthermore, newer simulators such as Arbor and Brian2 (Stimberg et al., 2019) have been designed from the ground up with a Python interface.

Our GeNN simulator can already be used as a backend for the Python-based Brian2 simulator (Stimberg et al., 2019) using the Brian2GeNN interface (Stimberg et al., 2020) which modifies the C++ backend “cpp_standalone” of Brian 2 to generate C++ input files for GeNN. As for cpp_standalone, initialisation of simulations is mostly done in C++ on the CPU and recording data is saved into binary files and re-imported into Python using Brian 2’s native methods. While we have recently demonstrated some very competitive performance results (Knight and Nowotny, 2018, 2020) using GeNN in C++, and through the Brian2GeNN interface (Stimberg et al., 2020), GeNN could so far not be used directly from Python and it is not possible to expose all of GeNN’s unique features through the Brian2 API. Specifically, GeNN not only allows users to easily define their own neuron and synapse models but, also ‘snippets’ for offloading the potentially costly initialisation of model parameters and connectivity onto the GPU. Additionally, GeNN provides a lot of freedom for users to integrate their own code into the simulation loop. In this paper we describe the implementation of PyGeNN – a Python package which aims to expose the full range of GeNN functionality with minimal performance overheads. Unlike in the majority of other SNN simulators PyGeNN allows defining bespoke neuron and synapse models directly from Python without requiring users to extend the underlying C++ code. Below, we demonstrate the flexibility and performance of PyGeNN in two scenarios where minimising performance overheads is particularly critical.

- In a simulation of a large, highly-connected model of a cortical microcircuit (Potjans and Diesmann, 2014) with small simulation timesteps. Here the cost of copying spike data off the GPU from a large number of neurons every timestep can become a bottleneck.
- In a simulation of a much smaller model of Pavlovian conditioning (Izhikevich, 2007) where learning occurs over 1 h of biological time and stimuli are delivered – following a complex scheme – throughout the simulation. Here any overheads are multiplied by a large number of timesteps and copying stimuli to the GPU can become a bottleneck.

Using the facilities provided by PyGeNN, we show that both scenarios can be simulated from Python with only minimal overheads over a pure C++ implementation.

2 MATERIALS AND METHODS

2.1 GeNN

GeNN (Yavuz et al., 2016) is a library for generating CUDA (NVIDIA et al., 2020) code for the simulation of spiking neural network models. GeNN handles much of the complexity of using CUDA directly and automatically performs device-specific optimizations so as to maximize performance. GeNN consists of a main library – implementing the API used to define models as well as the generic parts of the code generator

69 – and an additional library for each backend (currently there is a reference C++ backend for generating
 70 CPU code and a CUDA backend. An OpenCL backend is under development). Users describe their model
 71 by implementing a `modelDefinition` function within a C++ file. For example, a model consisting of 4
 72 Izhikevich neurons with heterogeneous parameters, driven by a constant input current might be defined as
 73 follows:

```
74 void modelDefinition(ModelSpec &model)
75 {
76     model.setDT(0.1);
77     model.setName("izhikevich");
78
79     NeuronModels::IzhikevichVariable::VarValues popInit(
80         -65.0, -20.0, uninitialisedVar(), uninitialisedVar(),
81         uninitialisedVar(), uninitialisedVar());
82
83     model.addNeuronPopulation<NeuronModels::IzhikevichVariable>(
84         "Pop", 4, {}, popInit);
85
86     model.addCurrentSource<CurrentSourceModels::DC>(
87         "CS", "Pop", {10.0}, {});
88 }
```

89 The *genn-buildmodel* command line tool is then used to compile this file; link it against the main GeNN
 90 library and the desired backend library; and finally run the resultant executable to generate the source code
 91 required to build a simulation dynamic library (a .dll file on Windows or a .so file on Linux and Mac). This
 92 dynamic library can then either be linked against a simulation loop provided by the user or dynamically
 93 loaded by the user's simulation code. To demonstrate this latter approach, the following example uses the
 94 `SharedLibraryModel` helper class supplied with GeNN to dynamically load the previously defined model,
 95 initialise the heterogenous neuron parameters and print each neuron's membrane voltage every timestep:

```
96 #include "sharedLibraryModel.h"
97
98 int main()
99 {
100     SharedLibraryModel<float> model("./", "izhikevich");
101     model.allocateMem();
102     model.initialize();
103     float *aPop = model.getScalar<float>("aPop");
104     float *bPop = model.getScalar<float>("bPop");
105     float *cPop = model.getScalar<float>("cPop");
106     float *dPop = model.getScalar<float>("dPop");
107     aPop[0] = 0.02; bPop[0] = 0.2; cPop[0] = -65.0; dPop[0] = 8.0;
108     aPop[1] = 0.1; bPop[1] = 0.2; cPop[1] = -65.0; dPop[1] = 2.0;
109     aPop[2] = 0.02; bPop[2] = 0.2; cPop[2] = -50.0; dPop[2] = 2.0;
110     aPop[3] = 0.02; bPop[3] = 0.2; cPop[3] = -55.0; dPop[3] = 4.0;
111     model.initializeSparse();
112
113     float *vPop = model.getScalar<float>("vPop");
114     while(model.getTime() < 200.0f) {
115         model.stepTime();
```

```

116     model.pullVarFromDevice("Pop", "V");
117     printf("%f, %f, %f, %f, %f\n",
118           t, VPop[0], VPop[1], VPop[2], VPop[3]);
119 }
120 return EXIT_SUCCESS;
121 }

```

122 2.2 SWIG

123 In order to use GeNN from Python, both the model creation API and the `SharedLibraryModel`
 124 functionality need to be ‘wrapped’ so they can be called from Python. While this is possible using
 125 the API built into Python itself, wrapper functions would need to be manually implemented for each GeNN
 126 function to be exposed which would result in a lot of maintenance overhead. Instead, we chose to use
 127 SWIG (Beazley, 1996) to automatically generate wrapper functions and classes. SWIG generates Python
 128 modules based on special interface files which can directly include C++ code as well as special ‘directives’
 129 which control SWIG. For example, the following SWIG interface file would wrap the C++ code in `test.h` in
 130 a Python module called `test_module` within a Python packages called `test_package`:

```

131 %module(package="test_package") test_module
132 %include "test.h"

```

133 The `%module` directive sets the name of the generated module and the package it will be located in and
 134 the `%include` directive parses and automatically generates wrapper functions for the C++ header file. We
 135 use SWIG in this manner to wrap both the model building and `SharedLibraryModel` APIs described in
 136 section 2.1. However, key parts of GeNN’s API such as the `ModelSpec::addNeuronPopulation` method
 137 employed in section 2.1, rely on C++ templates which are not directly translatable to Python. Instead, valid
 138 template instantiations need to be given a unique name in Python using the `%template` SWIG directive:

```

139 %template(addNeuronPopulationLIF) ModelSpec::addNeuronPopulation<NeuronModels::LIF>;

```

140 Having to manually add these directives whenever a model is added to GeNN would be exactly the sort
 141 of maintenance overhead we were trying to avoid by using SWIG. Therefore, when building the Python
 142 wrapper, we instead search the GeNN header files for the macros used to declare models in C++ and
 143 automatically generate SWIG `%template` directives.

144 As previously discussed, a key feature of GeNN is the ease with which it allows users to define their
 145 own neuron and synapse models as well as ‘snippets’ defining how variables and connectivity should be
 146 initialised. Beneath the syntactic sugar described in our previous work (Knight and Nowotny, 2018), new
 147 models can be defined in C++ by defining a new class derived from, for example, the `NeuronModels::Base`
 148 class. The ability to extend this system to Python was a key requirement of PyGeNN and, by using SWIG
 149 ‘director’, C++ classes can be made inheritable from Python using a single SWIG directive:

```

150 %feature("director") NeuronModels::Base;

```

151 2.3 PyGeNN

152 While GeNN *could* be used from Python via the wrapper generated using SWIG, the resultant code
 153 would be unpleasant to use directly. For example, rather than being able to specify neuron parameters
 154 using a native Python types such as lists or dictionaries, one would have to use a wrapped type such as
 155 `DoubleVector([0.25, 10.0, 0.0, 0.0, 20.0, 2.0, 0.5])`. Therefore, in order to provide a more

user-friendly and pythonic interface, we have built PyGeNN on top of the wrapper generated by SWIG. PyGeNN combines the separate model building and simulation stages of building a GeNN model in C++ into a single API, likely to be more familiar to users of existing Python-based model description languages such as PyNEST (Eppler et al., 2009) or PyNN (Davison et al., 2008). By combining the two stages together, PyGeNN can provide a unified dictionary-based API for initialising homogeneous and heterogeneous parameters as shown in this re-implementation of the previous example:

```

162 from pygenn import genn_wrapper, genn_model
163
164 model = genn_model.GeNNModel("float", "izhikevich")
165 model.dT = 0.1
166
167 izk_init = {"V": -65.0,
168            "U": -20.0,
169            "a": [ 0.02, 0.1, 0.02, 0.02],
170            "b": [ 0.2, 0.2, 0.2, 0.2],
171            "c": [-65.0, -65.0, -50.0, -55.0],
172            "d": [ 8.0, 2.0, 2.0, 4.0]}
173
174 pop = model.add_neuron_population("Pop", 4, "IzhikevichVariable",
175                                 {}, izk_init)
176 model.add_current_source("CS", "DC", "Pop",
177                          {"amp": 10.0}, {})
178
179 model.build()
180 model.load()
181
182 v = pop.vars["V"].view
183 while model.t < 200.0:
184     model.step_time()
185     model.pull_state_from_device("Pop")
186     print("%f, %f, %f, %f, %f"
187           % (model.t, v[0], v[1], v[2], v[3]))

```

Initialisation of variables with homogeneous values – such as the neurons' membrane potential – is performed by initialisation kernels generated by GeNN and initialisation of variables with heterogeneous values – such as the **a**, **b** and **c** parameters – are copied to the GPU by PyGeNN after the model is loaded. While the PyGeNN API is more pythonic and, hopefully, more user-friendly than the C++ interface, it still provides users with the same low-level control over the simulation. Furthermore, by using SWIG's numpy (Van Der Walt et al., 2011) interface, the host memory allocated by GeNN can be accessed directly from Python using the `pop.vars["V"].view` syntax meaning that no potentially expensive additional copying of data is required.

As illustrated in the previously-defined model, for convenience, PyGeNN allows users to access GeNN's built-in models. However, one of PyGeNN's most powerful features is that it enables users to easily define their own neuron and synapse models from within Python. For example, an Izhikevich neuron model (Izhikevich, 2003) can be defined using the `create_custom_neuron_class` helper function which provides some syntactic sugar over directly inheriting from the SWIG director class:

```

201 izk_model = genn_model.create_custom_neuron_class(

```



```

202     "izk",
203     param_names=["a", "b", "c", "d"],
204     var_name_types=[("V", "scalar"), ("U", "scalar")],
205     sim_code=
206         """
207         $ (V) += 0.5 * (0.04 * $ (V) * $ (V) + 5.0 * $ (V) + 140.0 - $ (U) + $ (Isyn)) * DT;
208         $ (V) += 0.5 * (0.04 * $ (V) * $ (V) + 5.0 * $ (V) + 140.0 - $ (U) + $ (Isyn)) * DT;
209         $ (U) += $ (a) * ($ (b) * $ (V) - $ (U)) * DT;
210         """,
211     threshold_condition_code="$ (V) >= 30.0",
212     reset_code=
213         """
214         $ (V) = $ (c) ;
215         $ (U) += $ (d) ;
216         """)

```

217 The `param_names` list defines the real-valued parameters that are constant across the whole population of
 218 neurons and the `var_name_types` list defines the model state variables and their type (the `scalar` type
 219 is an alias for either single or double-precision floating point, depending on the precision passed to the
 220 `GeNNModel` constructor). The behaviour of the model is then defined using a number of code strings. Unlike
 221 in tools like Brian 2 (Stimberg et al., 2019), these code strings are specified in a C-like language rather than
 222 using differential equations. This allows expert users to choose their own solver for models described in
 223 terms of differential equations and to programatically define models such as spike sources. For example,
 224 in the model presented above, we chose to implement the neuron using the idiosyncratic forward Euler
 225 integration scheme employed by Izhikevich (2003). Finally, the `threshold_condition_code` expression
 226 defines *when* the neuron will spike whereas the `reset_code` code string defines how the state variables
 227 should be reset after a spike.

228 2.4 Spike recording system

229 Internally, GeNN stores the spikes emitted by a neuron population during one simulation timestep in
 230 an array containing the indices of the neurons that spiked alongside a counter of how many spikes have
 231 been emitted overall. Previously, recording spikes in GeNN was very similar to the recording of voltages
 232 shown in the previous example code – the array of neuron indices was simply copied from the GPU to the
 233 CPU every timestep. However, especially when simulating models with a small simulation timestep, such
 234 frequent synchronization between the CPU and GPU is costly – especially if a slower, interpreted language
 235 such as Python is involved. Furthermore, biological neurons typically spike at a low rate (in the cortex, the
 236 average firing rate is only around 3 Hz (Buzsáki and Mizuseki, 2014)) meaning that the amount of spike
 237 data transferred every timestep is typically very small. To address both of these sources of inefficiency,
 238 we have added a new data structure to GeNN which stores spike data for many timesteps on the GPU. To
 239 reduce the memory required for this data structure and to make its size independent of neural activity, the
 240 spikes emitted by a population of N neurons in a single simulation timestep are stored in a N bit bitfield
 241 where a ‘1’ represents a spike and a ‘0’ the absence of one. Spiking data over multiple timesteps is then
 242 represented by a circular buffer of these bitfields. Using this approach, even the spiking output of relatively
 243 large models, running for many timesteps can be stored in a small amount of memory. For example, the
 244 spiking output of a model with 100×10^3 neurons running for 10×10^3 simulation timesteps, required
 245 less than 120 MB – a small fraction of the memory on a modern GPU. While efficiently handling spikes

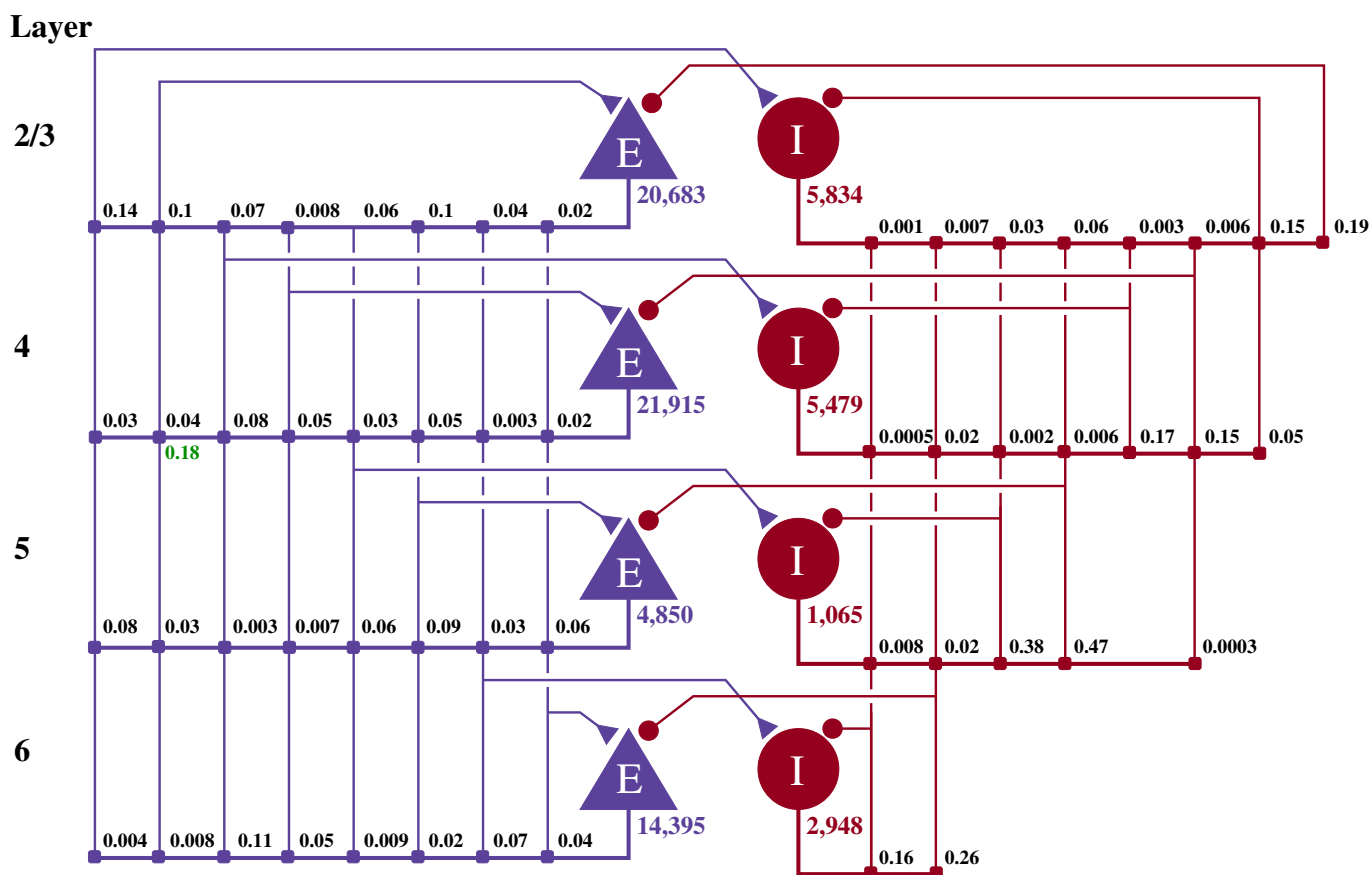


Figure 1. Illustration of the microcircuit model. Blue triangles represent excitatory populations, red circles represent inhibitory populations and the number beneath each symbol shows the number of neurons in each population. Connection probabilities are shown in small bold numbers at the appropriate point in the connection matrix. All excitatory synaptic weights are normally distributed with a mean of 0.0878 nA (unless otherwise indicated in green) and a standard deviation of 0.00878 nA. All inhibitory synaptic weights are normally distributed with a mean of 0.3512 nA and a standard deviation of 0.03512 nA.

246 stored in a bitfield is a little trickier than working with a list of neuron indices, GeNN provides an efficient
 247 C++ helper function for saving the spikes stored in a bitfield to a text file and a numpy-based method for
 248 decoding them in PyGeNN.

249 2.5 Cortical microcircuit model

Potjans and Diesmann (2014) developed the cortical microcircuit model of 1 mm³ of early-sensory cortex illustrated in figure 1. The model consists of 77 169 LIF neurons, divided into separate populations representing the excitatory and inhibitory population in each of 4 cortical layers (2/3, 4, 5 and 6). The membrane voltage V_i of each neuron i is modelled as:

$$\tau_m \frac{dV_i}{dt} = (V_{\text{rest}} - V_i) + R_m (I_{\text{syn}_i} + I_{\text{ext}_i}), \quad (1)$$

where $\tau_m = 10$ ms and $R_m = 40$ M Ω represent the time constant and resistance of the neuron's cell membrane, $V_{\text{rest}} = -65$ mV defines the resting potential, I_{syn_i} represents the synaptic input current and I_{ext_i} represents an external input current. When the membrane voltage crosses a threshold $V_{\text{th}} = -50$ mV a spike is emitted, the membrane voltage is reset to V_{rest} and updating of V is suspended for a refractory

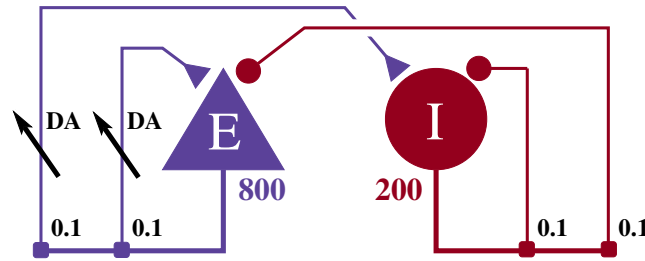


Figure 2. Illustration of the balanced random network model. The blue triangle represents the excitatory population, the red circle represents the inhibitory population, and the numbers beneath each symbol show the number of neurons in each population. Connection probabilities are shown in small bold numbers at the appropriate point in the connection matrix. All excitatory synaptic weights are plastic and initialised to 1 and all inhibitory synaptic weights are initialised to -1 .

period $\tau_{\text{ref}} = 2$ ms. Neurons in each population are connected randomly with numbers of synapses derived from an extensive review of the anatomical literature. These synapses are current-based, i.e. presynaptic spikes lead to exponentially-decaying input currents I_{syn_i}

$$\tau_{\text{syn}} \frac{dI_{\text{syn}_i}}{dt} = -I_{\text{syn}_i} + \sum_{j=0}^n w_{ij} \sum_{t_j} \delta(t - t_j), \quad (2)$$

where $\tau_{\text{syn}} = 0.5$ ms represents the synaptic time constant, w_{ij} represents the synaptic weight and t_j are the arrival times of incoming spikes from n presynaptic neurons. Within each synaptic projection, all synaptic strengths and transmission delays are normally distributed using the parameters presented in Potjans and Diesmann (2014, table 5) and, in total, the model has approximately 0.3×10^9 synapses. As well as receiving synaptic input, each neuron in the network also receives an independent Poisson input current, representing input from neighbouring not explicitly modelled cortical regions. The Poisson input is delivered to each neuron via I_{ext_i} with

$$\tau_{\text{syn}} \frac{dI_{\text{ext}_i}}{dt} = -I_{\text{ext}_i} + w_{\text{ext}} \text{Poisson}(\nu_{\text{ext}} \Delta t), \quad (3)$$

250 where ν_{ext} represents the mean input rate and w_{ext} represents the weight. The ordinary differential
 251 Eq. 1, 2 and 3 are solved with an exponential Euler algorithm. For a full description of the model
 252 parameters, please refer to Potjans and Diesmann (2014, tables 4 and 5) and for a description of the
 253 strategies used by GeNN to parallelise the initialisation and subsequent simulation of this network, please
 254 refer to Knight and Nowotny (2018, section 2.3). This model requires simulation using a relatively small
 255 timestep of 0.1 ms, making the overheads of copying spikes from the GPU every timestep particularly
 256 problematic.

257 2.6 Pavlovian conditioning model

258 The cortical microcircuit model described in the previous section is ideal for exploring the performance
 259 of short simulations of relatively large models. However, the performance of longer simulations of smaller
 260 models is equally vital. Such models can be particularly troublesome for GPU simulation as, not only might
 261 they not offer enough parallelism to fully occupy the device but, each timestep can be simulated so quickly
 262 that the overheads of launching kernels etc can dominate. Additional overheads can be incurred when
 263 models require injecting external stimuli throughout the simulation. Longer simulations are particularly

useful when exploring synaptic plasticity so, to explore the performance of PyGeNN in this scenario, we simulate a model of Pavlovian conditioning using a three-factor Spike-Timing-Dependent Plasticity (STDP) learning rule (Izhikevich, 2007).

2.6.1 Neuron model

The model illustrated in figure 2 consists of an 800 neuron excitatory population and a 200 neuron inhibitory population, within which, each neuron i is modelled using the Izhikevich model (Izhikevich, 2003) whose dimensionless membrane voltage V_i and adaption variables U_i evolve such that:

$$\frac{dV_i}{dt} = 0.04V_i^2 + 5V_i + 140 - U_i + I_{\text{syn}_i} + I_{\text{ext}_i} \quad (4)$$

$$\frac{dU_i}{dt} = a(bV_i - U_i) \quad (5)$$

When the membrane voltage rises above 30, a spike is emitted and V_i is reset to c and d is added to U_i . Excitatory neurons use the regular-spiking parameters (Izhikevich, 2003) where $a = 0.02$, $b = 0.2$, $c = -65.0$, $d = 8.0$ and inhibitory neurons use the fast-spiking parameters (Izhikevich, 2003) where $a = 0.1$, $b = 0.2$, $c = -65.0$, $d = 2.0$. Again, I_{syn_i} represents the synaptic input current and I_{ext_i} represents an external input current. While there are numerous ways to solve Eq. 4 and 5 (Humphries and Gurney, 2007; Hopkins and Furber, 2015; Pauli et al., 2018), we chose to use the idiosyncratic forward Euler integration scheme employed by Izhikevich (2003) in the original work (Izhikevich, 2007). Under this scheme, Eq. 4 is first integrated for two 0.5 ms timesteps and then, based on the updated value of V_i , Eq. 5 is integrated for a single 1 ms timestep.

2.6.2 Synapse models

The excitatory and inhibitory neural populations are connected recurrently, as shown in figure 1, with instantaneous current-based synapses:

$$I_{\text{syn}_i}(t) = \sum_{j=0}^n w_{ij} \sum_{t_j} \delta(t - t_j), \quad (6)$$

where t_j are the arrival times of incoming spikes from n presynaptic neurons. Inhibitory synapses are static with $w_{ij} = -1.0$ and excitatory synapses are plastic. Each plastic synapse has an eligibility trace C_{ij} as well as a synaptic weight w_{ij} and these evolve according to a three-factor STDP learning rule (Izhikevich, 2007):

$$\frac{dC_{ij}}{dt} = -\frac{C_{ij}}{\tau_c} + \text{STDP}(\Delta t)\delta(t - t_{\text{pre/post}}) \quad (7)$$

$$\frac{dw_{ij}}{dt} = -C_{ij}D_j \quad (8)$$

where $\tau_c = 1000$ ms represents the decay time constant of the eligibility trace and $\text{STDP}(\Delta t)$ describes the magnitude of changes made to the eligibility trace in response to the relative timing of a pair of pre and postsynaptic spikes with temporal difference $\Delta t = t_{\text{post}} - t_{\text{pre}}$. These changes are only applied to the trace at the times of pre and postsynaptic spikes as indicated by the Dirac delta function $\delta(t - t_{\text{pre/post}})$. Here, a

double exponential STDP kernel is employed such that:

$$\text{STDP}(\Delta t) = \begin{cases} A_+ \exp\left(-\frac{\Delta t}{\tau_+}\right) & \text{if } \Delta t > 0 \\ A_- \exp\left(\frac{\Delta t}{\tau_-}\right) & \text{if } \Delta t < 0 \\ 0 & \text{otherwise} \end{cases} \quad (9)$$

where the time constant of the STDP window $\tau_+ = \tau_- = 20$ ms and the strength of potentiation and depression are $A_+ = 0.1$ and $A_- = 0.15$ respectively. Finally, each excitatory neuron has an additional variable D_j which describes extracellular dopamine concentration:

$$\frac{D_j}{t} = -\frac{D_j}{\tau_d} + \text{DA}(t) \quad (10)$$

where $\tau_d = 200$ ms represents the time constant of dopamine uptake and $\text{DA}(t)$ the dopamine input over time.

2.6.3 PyGeNN implementation of three-factor STDP

The first step in implementing this learning rule in PyGeNN is to implement the STDP updates and decay of C_{ij} using GeNN's event-driven plasticity system, the implementation of which was described in our previous work (Knight and Nowotny, 2018). Using a similar syntax to that described in section 2.3, we first create a new 'weight update model' with the learning rule parameters and the w_{ij} and C_{ij} state variables:

```

285 izhikevich_stdp_model = create_custom_weight_update_class(
286     "izhikevich_stdp",
287
288     param_names=["tauPlus", "tauMinus",
289                 "tauC", "aPlus", "aMinus"],
290     var_name_types=[("w", "scalar"), ("c", "scalar")],

```

We then instruct GeNN to record the times of current and previous pre and postsynaptic spikes. The current spike time will equal the current time if a spike of this sort is being processed in the current timestep whereas the previous spike time only tracks spikes which have occurred *before* the current timestep:

```

294 is_pre_spike_time_required=True,
295 is_post_spike_time_required=True,
296
297 is_prev_pre_spike_time_required=True,
298 is_prev_post_spike_time_required=True,

```

Next we define the 'sim code' which is called whenever presynaptic spikes arrive at the synapse. This code first implements Eq. 6 – adding the synaptic weight (w_{ij}) to the postsynaptic neuron's input (I_{syn_i}) using the `$ (addToInSyn, x)` function.

```

302 sim_code=
303     """
304     $ (addToInSyn, $ (w) );

```

Within the sim code we also need to calculate the time that has elapsed since the last update of C_{ij} using the spike times we previously requested that GeNN record. Within a timestep, GeNN processes presynaptic

spikes before postsynaptic spikes so the time of the last update to C_{ij} will be the latest time either type of spike was processed in previous timesteps:

```
const scalar tc = fmax($(prev_sT_pre),
                        $(prev_sT_post));
```

Using this time, we can now calculate how much to decay C_{ij} using the closed-form solution to Eq. 7:

```
const scalar tagDecay = exp(-$(t) - tc) / $(tauC);
scalar newTag = $(c) * tagDecay;
```

To complete the sim code we calculate the depression case of Eq. 9 (here we use the *current* postsynaptic spike time as, if a postsynaptic and presynaptic spike occur in the same timestep, there should be no update).

```
const scalar dt = $(t) - $(sT_post);
if (dt > 0) {
    newTag -= ($(aMinus) * exp(-dt / $(tauMinus)));
}
$(c) = newTag;
""",
```

Finally we define the ‘learn post code’ which is called whenever a postsynaptic spike arrives at the synapse. Other than implementing the potentiation case of Eq. 9 and using the *current* presynaptic spike time when calculating the time since the last update of C_{ij} – in order to correctly handle presynaptic updates made in the same timestep – this code is very similar to the sim code:

```
learn_post_code=
"""
const scalar tc = fmax($(sT_pre),
                        $(prev_sT_post));

const scalar tagDecay = exp(-$(t) - tc) / $(tauC);
scalar newTag = $(c) * tagDecay;

const scalar dt = $(t) - $(sT_pre);
if (dt > 0) {
    newTag += ($(aPlus) * exp(-dt / $(tauPlus)));
}
$(c) = newTag;
""")
```

Adding the synaptic weight w_{ij} update described by Eq. 8 requires two further additions to the model. As well as the pre and postsynaptic spikes, the weight update model needs to receive events whenever dopamine is injected via DA. GeNN supports such events via the ‘spike-like event’ system which allows events to be triggered based on an expression evaluated on the presynaptic neuron. In this case, this expression simply tests an `injectDopamine` flag which gets set by the dopamine injection logic in our presynaptic neuron model:

```
event_threshold_condition_code="injectDopamine",
```

348 In order to extend our event-driven update of C_{ij} to include spike-like events we need to instruct GeNN to
 349 record the times at which they occur:

```
350     is_pre_spike_event_time_required=True,
351     is_prev_pre_spike_event_time_required=True,
```

352 The spike-like events can now be handled using a final ‘event code’ string:

```
353     event_code=
354         """
355         const scalar tc = fmax($(sT_pre), fmax($(prev_sT_post), $(prev_seT_pre)));
356         const scalar tagDecay = exp(-$(t) - tc) / $(tauC));
357         $(c) *= tagDecay;
358         """,
```

After updating the previously defined calculations of tc in the sim code and learn post code in the same way to also include the times of spike-like events, all that remains is to update w_{ij} . Mikaitis et al. (2018) showed how Eq. 8 could be solved algebraically, allowing w_{ij} to be updated in an event-driven manner with:

$$\Delta w_{ij} = \frac{C(t_c^{last})D(t_d^{last})}{-\left(\frac{1}{\tau_c} + \frac{1}{\tau_d}\right)} \left(e^{-\frac{t-t_c^{last}}{\tau_c}} e^{-\frac{t-t_d^{last}}{\tau_d}} - e^{-\frac{t_w^{last}-t_c^{last}}{\tau_c}} e^{-\frac{t_w^{last}-t_d^{last}}{\tau_d}} \right) \quad (11)$$

where t_c^{last} , t_w^{last} and t_d^{last} represent the last times at which C_{ij} , w_{ij} and D_j respectively were updated. Because we will always update w_{ij} and C_{ij} together when presynaptic, postsynaptic and spike-like events occur, $t_c^{last} = t_w^{last}$ and Eq. 11 can be simplified to:

$$\Delta w_{ij} = \frac{C(t_c^{last})D(t_d^{last})}{-\left(\frac{1}{\tau_c} + \frac{1}{\tau_d}\right)} \left(e^{-\frac{t-t_c^{last}}{\tau_c}} e^{-\frac{t-t_d^{last}}{\tau_d}} - e^{-\frac{t_c^{last}-t_d^{last}}{\tau_d}} \right) \quad (12)$$

359 and this update can now be added to each of our three event handling code strings to complete the
 360 implementation of the learning rule.

361 2.6.4 PyGeNN implementation of Pavlovian conditioning experiment

362 To perform the Pavlovian conditioning experiment described by Izhikevich (2007) using this model, we
 363 chose 100 random groups of 50 neurons (each representing stimuli $S_1 \dots S_{100}$) from amongst the two neural
 364 populations. Stimuli are presented to the network in a random order, separated by intervals sampled from
 365 $U(100, 300)$ ms. The neurons associated with an active stimulus are stimulated for a single 1 ms simulation
 366 timestep with a current of 40.0 nA, in addition to the random background current of $U(-6.5, 6.5)$ nA,
 367 delivered to each neuron via I_{ext_i} throughout the simulation. S_1 is arbitrarily chosen as the Conditional
 368 Stimuli (CS) and, whenever this stimuli is presented, a reward in the form of an increase in dopamine
 369 is delivered by setting $DA(t) = 0.5$ after a delay sampled from $U(0, 1000)$ ms. This delay period is large
 370 enough to allow a few irrelevant stimuli to be presented which act as distractors. The simplest way to
 371 implement this stimulation regime is to add a current source to the excitatory and inhibitory neuron
 372 populations which adds the uniformly-distributed input current to an externally-controllable per-neuron
 373 current. In PyGeNN, the following model can be defined to do just that:

```
374 stim_noise_model = create_custom_current_source_class(
```

```

375     "stim_noise",
376     param_names=["n"],
377     var_name_types=[("iExt", "scalar", VarAccess_READ_ONLY)],
378     injection_code=
379         """
380         $(injectCurrent, $(iExt) + ($(gennrand_uniform) * $(n) * 2.0) - $(n));
381         """

```

where the `n` parameter sets the magnitude of the background noise, the `$(injectCurrent, I)` function injects a current of I nA into the neuron and `$(gennrand_uniform)` samples from $U(0, 1)$ using the ‘XORWOW’ pseudo-random number generator provided by cuRAND (NVIDIA Corporation, 2019). Once a current source population using this model has been instantiated and a memory view to `iExt` obtained in the manner described in section 2.3, in timesteps when stimulus injection is required, current can be injected into the list of neurons contained in `stimuli_input_set` with:

```

388 curr_ext_view[stimuli_input_set] = 40.0
389 curr_pop.push_var_to_device("iExt")

```

The same approach can then be used to zero the current afterwards. However, as almost 20 000 stimuli will be injected over the course of a 1 h simulation, we can alternatively offload the stimulus delivery entirely to the GPU in order to reduce potential overheads, using the following slightly more complex model:

```

393 stim_noise_model = create_custom_current_source_class(
394     "stim_noise",
395     param_names=["n", "stimMagnitude"],
396     var_name_types=[("startStim", "unsigned int"),
397                     ("endStim", "unsigned int", VarAccess_READ_ONLY)],
398     extra_global_params=[("stimTimes", "scalar*")],
399     injection_code=
400         """
401         scalar current = ($(gennrand_uniform) * $(n) * 2.0) - $(n);
402         if($(startStim) != $(endStim) && $(t) >= $(stimTimes)[$(startStim)]) {
403             current += $(stimMagnitude);
404             $(startStim)++;
405         }
406         $(injectCurrent, current);
407         """

```

This model retains the same logic for generating background noise but adds a `stimTimes` array which contains the times at which each neuron should have current injected. This array is an ‘extra global parameter’ – a read-only memory area that can be allocated and populated from PyGeNN, in this case by ‘stacking’ together a list of lists of spike times:

```

412 curr_pop.set_extra_global_param("stimTimes", np.hstack(neuron_stimuli_times))

```

The `startStim` and `endStim` variables are then used to point to the subset of the `stimTimes` array corresponding to each neuron. Once the simulation time (`$(t)`) passes the time at `stimTimes[startStim]`, current is injected and `startStim` is advanced.

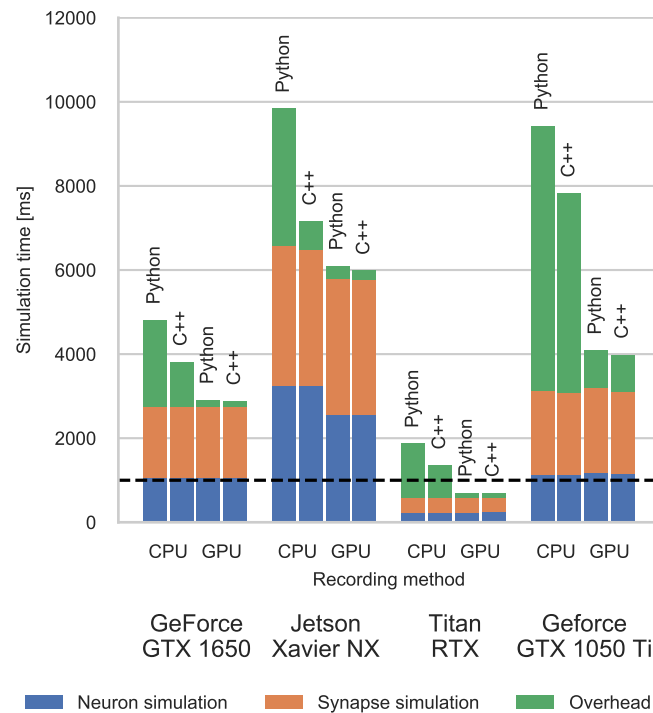


Figure 3. Simulation times of the microcircuit model running on various GPU hardware for 1 s of biological time. ‘Overhead’ refers to time spent in simulation loop but not within CUDA kernels. The dashed horizontal line indicates realtime performance

3 RESULTS

In the following subsections we will analyse the performance of the models introduced in sections 2.5 and 2.6 on a representative selection of NVIDIA GPU hardware:

- Jetson Xavier NX – a low-power embedded system with a GPU based on the Volta architecture with 8 GB of shared memory.
- GeForce GTX 1050Ti – a low-end desktop GPU based on the Pascal architecture with 4 GB of dedicated memory.
- GeForce GTX 1650 – a low-end desktop GPU based on the Turing architecture with 4 GB of dedicated memory.
- Titan RTX – a high-end workstation GPU based on the Turing architecture with 24 GB of dedicated memory.

All of these systems run Ubuntu 18 apart from the system with the GeForce 1050 Ti which runs Windows 10.

3.1 Cortical microcircuit model performance

Figure 3 shows the simulation times for the full-scale microcircuit model. We measured the total simulation time by querying the `std::chrono::high_resolution_clock` in C++ and the `time.perf_counter` in Python before and after the simulation loop; and used CUDA’s own event timing system (NVIDIA Corporation, 2021, Section 3.2.6.7) to record the time taken by the neuron and synapse kernels. As one might predict, the Jetson Xavier NX is slower than the three desktop GPUs but, considering

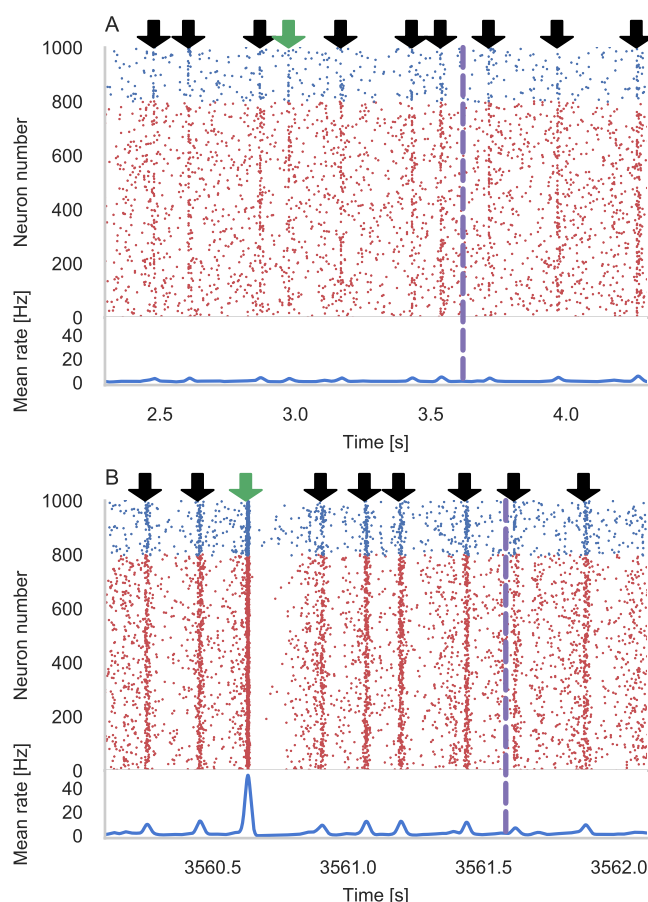


Figure 4. Results of Pavlovian conditioning experiment. Raster plot and spike density function (SDF) (Szücs, 1998) showing activity centred around first delivery of Conditional Stimulus (CS) during initial (A) and final (B) 50 s of simulation. Downward green arrows indicate times at which CS is delivered and downward black arrows indicate times when other, un-rewarded stimuli are delivered. Vertical dashed lines indicate times at which dopamine is delivered. The population SDF was calculated by convolving the spikes with a Gaussian kernel of $\sigma = 10$ ms width.

that it only consumes a maximum of 15 W compared to 75 W or 320 W for the GeForce cards and Titan RTX respectively, it still performs impressively. The time taken to actually simulate the models ('Neuron simulation' and 'Synapse simulation') are the same when using Python and C++ as all GeNN optimisation options are exposed to PyGeNN. Interestingly, when simulating *this* model, the larger L1 cache and architectural improvements present in the Turing-based GTX 1650 do not result in significantly improved performance over the Pascal-based GTX 1050Ti. Instead, the slightly improved performance of the GTX 1650 can probably be explained by its additional 128 CUDA cores.

Without the recording system described in section 2.4, the CPU and GPU need to be synchronised after every timestep to allow spike data to be copied off the GPU and stored in a suitable data structure. The 'overheads' shown in figure 3 indicate the time taken by these processes as well as the unavoidable overheads of launching CUDA kernels etc. Because Python is an interpreted language, updating the spike data structures is somewhat slower and this is particularly noticeable on devices with a slower CPU such as the Jetson Xavier NX. However, unlike the desktop GPUs, the Jetson Xavier NX's 8 GB of memory is shared between the GPU and the CPU meaning that data does not need to be copied between their memories and can instead be accessed by both. While, using this shared memory for recording spikes

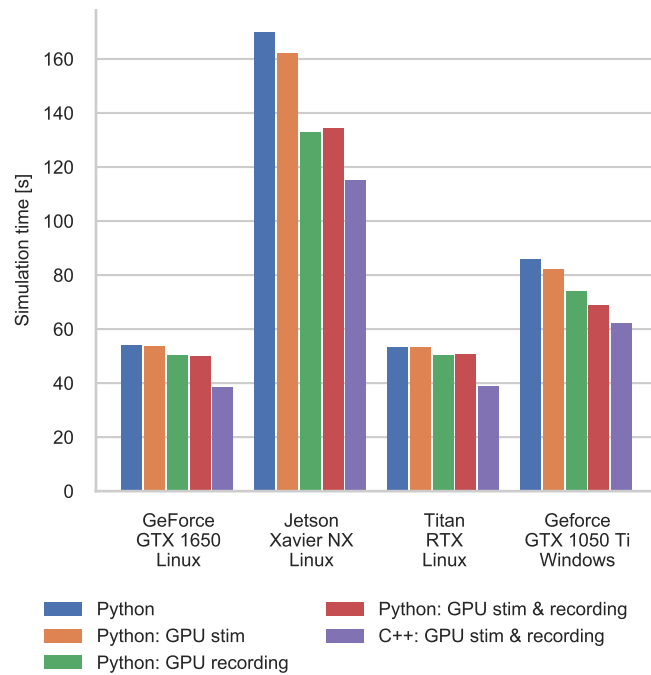


Figure 5. Simulation times of the Pavlovian Conditioning model running on various GPU hardware for 1 h of biological time. ‘GPU stim’ indicates simulations using the GPU stimulus delivery model and ‘GPU recording’ indicates simulations where the new recording system is employed.

reduces the overhead of copying data off the device, because the GPU and CPU caches are not coherent, caching must be disabled on this memory which reduces the performance of the neuron kernel. Although the Windows machine has a relatively powerful CPU, the overheads measured in both the Python and C++ simulations run on this system are extremely large due to additional queuing between the application and the GPU driver caused by the Windows Display Driver Model (WDDM). When small – in this case 0.1 ms – simulation timesteps are used, this makes per-timestep synchronisation disproportionately expensive.

However, when the spike recording system described in section 2.4 is used, spike data is kept in GPU memory until the end of the simulation and overheads are reduced by up to 10×. Because synchronisation with the CPU is no longer required every timestep, simulations run approximately twice as fast on the Windows machine. Furthermore, on the high-end desktop GPU, the simulation now runs faster than real-time in both Python and native C++ versions – significantly faster than other recently published GPU simulators (Golosio et al., 2021) and even specialised neuromorphic systems (Rhodes et al., 2020).

3.2 Pavlovian conditioning performance

Figure 4 shows the results of an example simulation of the Pavlovian conditioning model. At the beginning of each simulation (Figure 4A), the neurons representing every stimulus respond equally. However, after 1 h of simulation, the response to the CS becomes much stronger (Figure 4B) – showing that these neurons have been selectively associated with the stimulus even in the presence of the distractors and the delayed reward.

In figure 5, we show the runtime performance of simulations of the Pavlovian conditioning model, running on the GPUs described above using PyGeNN with and without the recording system described in section 2.4 and the optimized stimulus-delivery described in section 2.6. These PyGeNN results are

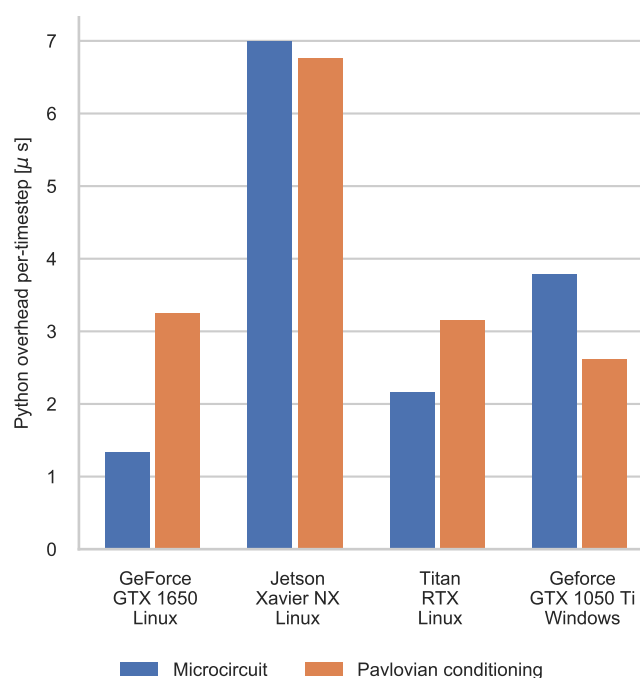


Figure 6. Comparison of the duration of individual timestep in Python and C++ simulation in microcircuit and Pavlovian conditioning experiments. Times are taken from averages calculated over 5 runs of the fastest version of each model i.e. the microcircuit using the GPU recording system and the Pavlovian conditioning model using the GPU recording system and the GPU stimulus delivery.

470 compared to a C++ simulation using both optimizations. Because each simulation timestep only takes a
 471 few μ s, the overhead of using CUDA timing events significantly alters the performance so, for this model,
 472 we only measure the duration of the simulation loop using the approaches described in the previous section.
 473 Although we only record the spiking activity during the first and last 50 s, using the recording system
 474 still significantly improves the overall performance on all devices – especially on the Jetson Xavier NX
 475 with its slower CPU. Interestingly the Titan RTX and GTX 1650 perform identically in this benchmark
 476 with speedups ranging from $62\times$ to $72\times$ real-time. This is because, as discussed previously, this model is
 477 simply not large enough to fill the 4608 CUDA cores present on the Titan RTX. Therefore, as the two GPUs
 478 share the same Turing architecture and have very similar clock speeds (1350 MHz–1770 MHz for the Titan
 479 RTX and 1485 MHz–1665 MHz for the GTX 1650), the two GPUs perform very similarly. Similarly to
 480 the simulations of the microcircuit model, the Jetson Xavier NX performs rather slower than the desktop
 481 GPUs but still achieves speedups of up to $31\times$.

482 Interestingly, unlike in the simulations of the microcircuit model, here the GTX 1050 Ti performs
 483 rather differently. Although the clock speed of this device is approximately the same as the other GPUs
 484 (1290 MHz–1392 MHz) and it has a similar number of CUDA cores to the GTX 1650, its performance
 485 is significantly worse. The difference in performance across all configurations is likely to be due to
 486 architectural differences between the older Pascal; and newer Volta and Turing architectures. Specifically,
 487 Pascal GPUs have one type of Arithmetic Logic Unit (ALU) which handles both integer and floating point
 488 arithmetic whereas, the newer Volta and Turing architectures have equal numbers of dedicated integer and
 489 floating point ALUs as well as significantly larger L1 caches. As discussed in our previous work (Knight
 490 and Nowotny, 2018), these architectural features are particularly beneficial for SNN simulations with
 491 STDP where a large amount of floating point computation is required to update the synaptic state *and*

additional integer arithmetic is required to calculate the indices into the sparse matrix data structures. Furthermore, due to the additional synchronisation overheads caused by the Windows Display Driver Model (WDDM) which we discussed in the previous section, offloading stimulus delivery to the GPU improves the performance significantly on the Windows machine. However, on the other devices, it only provides a minimal improvement.

The difference between the speeds of the Python and C++ simulations of the Pavlovian conditioning model (figure 5) *appear* much larger than those of the microcircuit model (figure 3). However, as figure 6 illustrates, for individual timesteps the excess time due to overheads is approximately the same for both models and consistent with the cost of a small number of Python to C++ function calls (Apache Crail, 2019). Depending on the size and complexity of the model as well as the hardware used, this overhead may or may not be important. For example, when simulating the microcircuit model for 1 s on the Titan RTX, the overhead of using Python is less than 0.2 % but, when simulating the Pavlovian conditioning model on the same device, the overhead of using Python is almost 31 %.

4 DISCUSSION

In this paper we have introduced PyGeNN, a Python interface to the C++ based GeNN library for GPU accelerated spiking neural network simulations.

Uniquely, the new interface provides access to all the features of GeNN, without leaving the comparative simplicity of Python and with, as we have shown, typically negligible overheads from the Python bindings. PyGeNN also allows bespoke neuron and synapse models to be defined from within Python, making PyGeNN much more flexible and broadly applicable than, for instance, the Python interface to NEST (Eppler et al., 2009) or the PyNN model description language used to expose CARLsim to Python (Balaji et al., 2020).

In many ways, the new interface resembles elements of the Python-based Brian 2 simulator (Stimberg et al., 2019) (and it's Brian2GeNN backend (Stimberg et al., 2020)) with two key differences. Unlike in Brian 2, bespoke models in PyGeNN are defined with 'C-like' code snippets. This has the advantage of unparalleled flexibility for the expert user, but comes at the cost of more complexity as the code for a timestep update needs to include a suitable solver as well as merely differential equations. The second difference lies in how data structures are handled. Whereas simulations run using the C++ or Brian2GeNN Brian 2 backends use files to exchange data with Python, the underlying GeNN data structures are directly accessible from PyGeNN meaning that no disk access is involved.

As we have demonstrated, the PyGeNN wrapper, exactly like native GeNN, can be used on a variety of hardware from data centre scale down to mobile devices such as the NVIDIA Jetson. This allows for the same codes to be used in large-scale brain simulations and embedded and embodied spiking neural network research. Supporting the popular Python language in this interface makes this ecosystem available to a wider audience of researchers in both Computational Neuroscience, bio-mimetic machine learning and autonomous robotics.

The new interface also opens up opportunities to support researchers that work with other Python based systems. In the Computational Neuroscience and Neuromorphic computing communities, we can now build a PyNN (Davison et al., 2008) interface on top of PyGeNN and, in fact, a prototype of such an interface is in development. Furthermore, for the burgeoning spike-based machine learning community, we can use PyGeNN as the basis for a spike-based machine learning framework akin to TensorFlow or PyTorch for rate-based models. A prototype interface of this sort called mlGeNN is in development and close to release.

In this work we have introduced a new spike recording system for GeNN and have shown that, using this system, we can now simulate the Potjans microcircuit model (Potjans and Diesmann, 2014) faster than real-time and, to the best of our knowledge, faster than any other system. Finally, the excellent performance we have demonstrated using low-end Turing architecture GPUs is very exciting in terms of increasing the accessibility of GPU accelerated Computational Neuroscience and SNN machine learning research.

CONFLICT OF INTEREST STATEMENT

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

AUTHOR CONTRIBUTIONS

JK and TN wrote the paper. TN is the original developer of GeNN. AK was the original developer of PyGeNN. JK is currently the primary developer of both GeNN and PyGeNN and was responsible for implementing the spike recording system. JK performed the experiments and the analysis of the results that are presented in this work.

FUNDING

This work was funded by the EPSRC (Brains on Board project, grant number EP/P006094/1 and ActiveAI project, grant number EP/S030964/1), the European Union's Horizon 2020 research and innovation program under Grant Agreement 945539 (HBP SGA3) and a Google Summer of Code grant to AK.

ACKNOWLEDGMENTS

We would like to thank Malin Sandström and everyone else at the International Neuroinformatics Coordinating Facility (INCF) for their hard work running the Google Summer of Code mentoring organisation every year. Without them, this and many other exciting Neuroinformatics projects would not be possible.

DATA AVAILABILITY STATEMENT

All models, data and analysis scripts used for this study can be found in https://github.com/BrainsOnBoard/pygenn_paper. All experiments were carried out using the GeNN 4.4.0 which is available from <https://doi.org/10.5281/zenodo.4419159>.

REFERENCES

- Akar, N. A., Cumming, B., Karakasis, V., Kusters, A., Klijn, W., Peyser, A., et al. (2019). Arbor — A Morphologically-Detailed Neural Network Simulation Library for Contemporary High-Performance Computing Architectures. In *2019 27th Euromicro International Conference on Parallel, Distributed and Network-Based Processing (PDP)* (IEEE), 274–282. doi:10.1109/EMPDP.2019.8671560
- [Dataset] Apache Crail (2019). Crail Python API: Python -> C/C++ call overhead
- Balaji, A., Adiraju, P., Kashyap, H. J., Das, A., Krichmar, J. L., Dutt, N. D., et al. (2020). PyCARL: A PyNN Interface for Hardware-Software Co-Simulation of Spiking Neural Network

- 561 Beazley, D. M. (1996). Using SWIG to control, prototype, and debug C programs with Python. In *Proc.*
 562 *4th Int. Python Conf*
- 563 Buzsáki, G. and Mizuseki, K. (2014). The log-dynamic brain: how skewed distributions affect network
 564 operations. *Nature reviews. Neuroscience* 15, 264–78. doi:10.1038/nrn3687
- 565 Carnevale, N. T. and Hines, M. L. (2006). *The NEURON book* (Cambridge University Press)
- 566 Chou, T.-s., Kashyap, H. J., Xing, J., Listopad, S., Rounds, E. L., Beyeler, M., et al. (2018). CARLsim 4:
 567 An Open Source Library for Large Scale, Biologically Detailed Spiking Neural Network Simulation
 568 using Heterogeneous Clusters. In *2018 International Joint Conference on Neural Networks (IJCNN)*
 569 (IEEE), 1–8. doi:10.1109/IJCNN.2018.8489326
- 570 Davison, A. P., Brüderle, D., Eppler, J., Kremkow, J., Müller, E., Pecevski, D., et al. (2008). PyNN: A
 571 Common Interface for Neuronal Network Simulators. *Frontiers in neuroinformatics* 2, 11. doi:10.3389/
 572 neuro.11.011.2008
- 573 Eppler, J. M., Helias, M., Müller, E., Diesmann, M., and Gewaltig, M. O. (2009). PyNEST: A convenient
 574 interface to the NEST simulator. *Frontiers in Neuroinformatics* 2, 1–12. doi:10.3389/neuro.11.012.2008
- 575 Gewaltig, M.-O. and Diesmann, M. (2007). NEST (NEural Simulation Tool). *Scholarpedia* 2, 1430
- 576 Givon, L. E. and Lazar, A. A. (2016). Neurokernel: An open source platform for emulating the fruit fly
 577 brain. *PLOS ONE* 11, 1–25. doi:10.1371/journal.pone.0146581
- 578 Golosio, B., Tiddia, G., De Luca, C., Pastorelli, E., Simula, F., and Paolucci, P. S. (2021). Fast Simulations
 579 of Highly-Connected Spiking Cortical Models Using GPUs. *Frontiers in Computational Neuroscience*
 580 15, 1–17. doi:10.3389/fncom.2021.627620
- 581 Hines, M. L., Davison, A. P., and Müller, E. (2009). NEURON and Python. *Frontiers in Neuroinformatics*
 582 3, 1–12. doi:10.3389/neuro.11.001.2009
- 583 Hopkins, M. and Furber, S. B. (2015). Accuracy and Efficiency in Fixed-Point Neural ODE Solvers.
 584 *Neural computation* 27, 2148–2182
- 585 Humphries, M. D. and Gurney, K. (2007). Solution Methods for a New Class of Simple Model Neurons M.
 586 *Neural Computation* 19, 3216–3225. doi:doi:10.1162/neco.2007.19.12.3216
- 587 Hunter, J. D. (2007). Matplotlib: A 2D graphics environment. *Computing in Science & Engineering* 9,
 588 90–95. doi:10.1109/MCSE.2007.55
- 589 Izhikevich, E. M. (2003). Simple model of spiking neurons. *IEEE Transactions on neural networks* 14,
 590 1569–72. doi:10.1109/TNN.2003.820440
- 591 Izhikevich, E. M. (2007). Solving the Distal Reward Problem through Linkage of STDP and Dopamine
 592 Signaling. *Cerebral Cortex* 17, 2443–2452. doi:10.1093/cercor/bhl152
- 593 Knight, J. C. and Nowotny, T. (2018). GPUs Outperform Current HPC and Neuromorphic Solutions
 594 in Terms of Speed and Energy When Simulating a Highly-Connected Cortical Model. *Frontiers in*
 595 *Neuroscience* 12, 1–19. doi:10.3389/fnins.2018.00941
- 596 Knight, J. C. and Nowotny, T. (2020). Larger GPU-accelerated brain simulations with procedural
 597 connectivity. *bioRxiv* doi:10.1101/2020.04.27.063693
- 598 Mikaitis, M., Pineda García, G., Knight, J. C., and Furber, S. B. (2018). Neuromodulated Synaptic
 599 Plasticity on the SpiNNaker Neuromorphic System 12, 1–13. doi:10.3389/fnins.2018.00105
- 600 Millman, K. J. and Aivazis, M. (2011). Python for scientists and engineers. *Computing in Science and*
 601 *Engineering* 13, 9–12. doi:10.1109/MCSE.2011.36
- 602 NVIDIA, Vingelmann, P., and Fitzek, F. H. (2020). *CUDA, developer.nvidia.com/cuda-toolkit*
- 603 NVIDIA Corporation (2019). *cuRAND Library, docs.nvidia.com/cuda/pdf/CURAND_Library.pdf*
- 604 NVIDIA Corporation (2021). *CUDA C Programming Guide,*
 605 *docs.nvidia.com/cuda/pdf/CUDA_C_Programming_Guide.pdf*

- 606 Pauli, R., Weidel, P., Kunkel, S., and Morrison, A. (2018). Reproducing Polychronization: A Guide to
607 Maximizing the Reproducibility of Spiking Network Models. *Frontiers in Neuroinformatics* 12, 1–21.
608 doi:10.3389/fninf.2018.00046
- 609 Plotnikov, D., Rumpe, B., Blundell, I., Ippen, T., Eppler, J. M., and Morrison, A. (2016). NESTML: a
610 modeling language for spiking neurons (Zenodo). doi:10.5281/zenodo.1412345
- 611 Potjans, T. C. and Diesmann, M. (2014). The Cell-Type Specific Cortical Microcircuit: Relating Structure
612 and Activity in a Full-Scale Spiking Network Model. *Cerebral Cortex* 24, 785–806. doi:10.1093/cercor/
613 bhs358
- 614 Rhodes, O., Peres, L., Rowley, A. G. D., Gait, A., Plana, L. A., Brenninkmeijer, C., et al. (2020). Real-time
615 cortical simulation on neuromorphic hardware. *Philosophical Transactions of the Royal Society A:
616 Mathematical, Physical and Engineering Sciences* 378, 20190160. doi:10.1098/rsta.2019.0160
- 617 Stimberg, M., Brette, R., and Goodman, D. F. (2019). Brian 2, an intuitive and efficient neural simulator.
618 *eLife* 8, 1–41. doi:10.7554/eLife.47314
- 619 Stimberg, M., Goodman, D. F., and Nowotny, T. (2020). Brian2GeNN: accelerating spiking neural network
620 simulations with graphics hardware. *Scientific Reports* 10, 1–12. doi:10.1038/s41598-019-54957-7
- 621 Szücs, A. (1998). Applications of the spike density function in analysis of neuronal firing patterns. *J*
622 *Neurosci Methods* 81, 159–167
- 623 Van Der Walt, S., Colbert, S. C., and Varoquaux, G. (2011). The NumPy array: A structure for efficient
624 numerical computation. *Computing in Science and Engineering* 13, 22–30. doi:10.1109/MCSE.2011.37
- 625 Vitay, J., Dinkelbach, H., and Hamker, F. (2015). ANNarchy: a code generation approach to neural
626 simulations on parallel hardware. *Frontiers in Neuroinformatics* 9, 19. doi:10.3389/fninf.2015.00019
- 627 Yavuz, E., Turner, J., and Nowotny, T. (2016). GeNN: a code generation framework for accelerated brain
628 simulations. *Scientific reports* 6, 18854. doi:10.1038/srep18854